

Workshop – Prediction Analysis, Frequency Response Analysis (SOL 111)

AN MSC NASTRAN MACHINE LEARNING WEB APP TUTORIAL

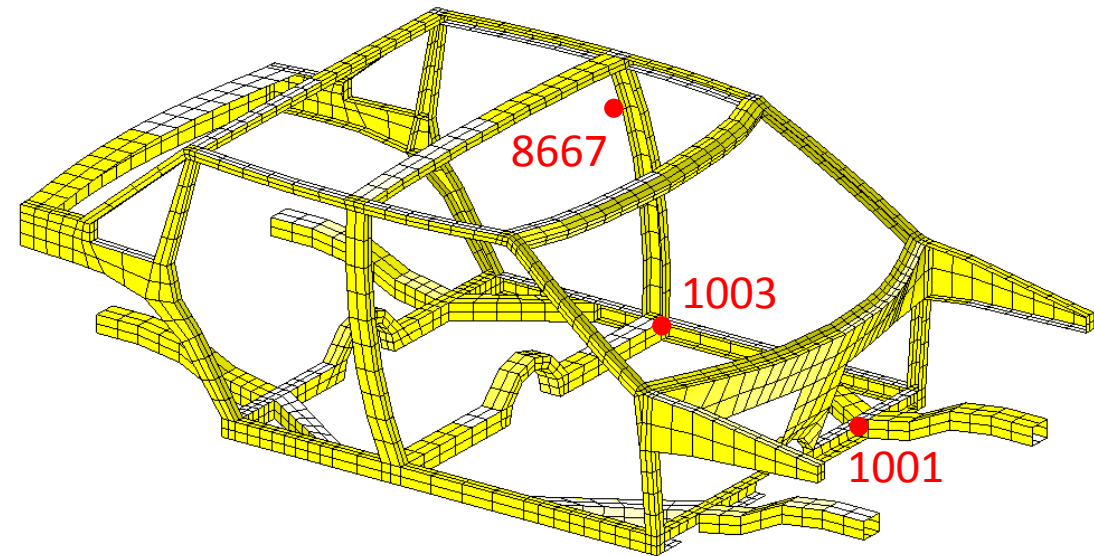
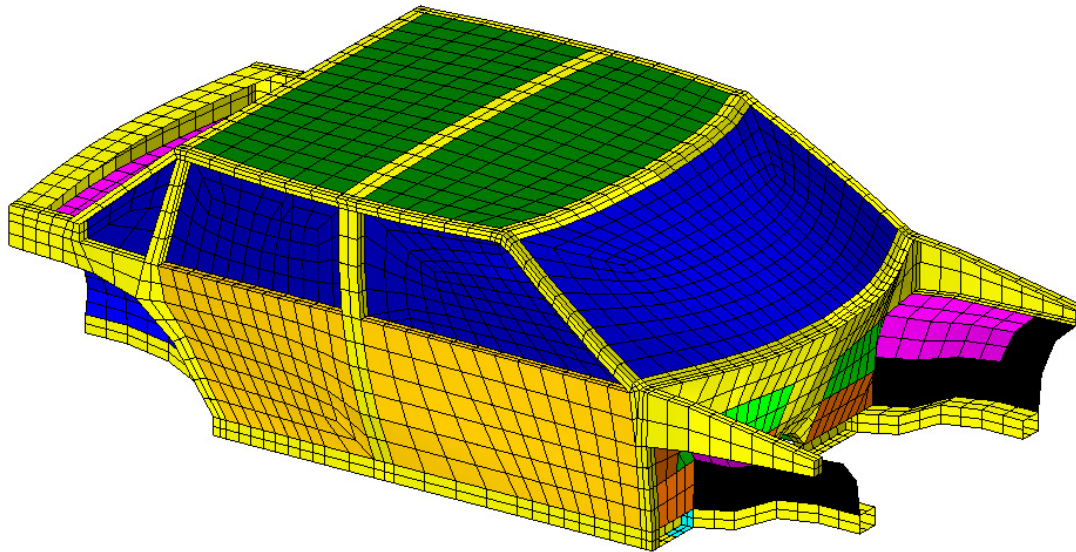
Goal: Prediction Analysis

This tutorial consists of multiple parts

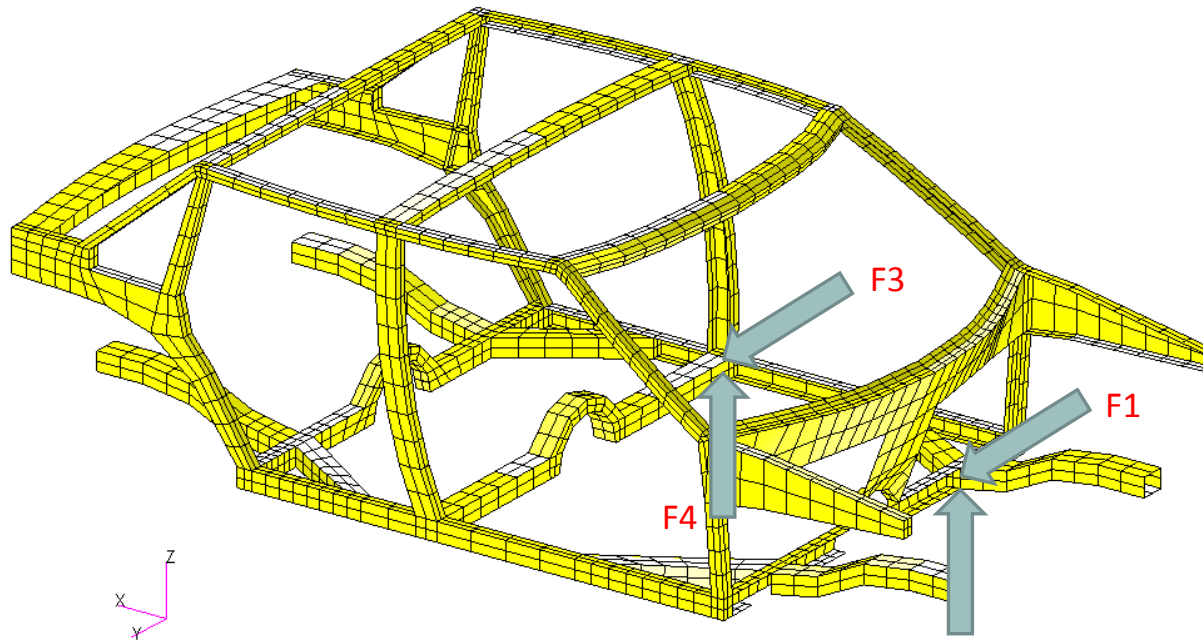
1. Configuring The Problem Statement
 - In this tutorial, we configure the parameters and the responses to monitor.
2. Configuring Multiple Batch Runs
 - This section discusses how to configure and execute multiple MSC Nastran runs.
3. Determining Parameter Relevance (Parameter/Variable Screening)
 - This example starts with 11 parameters. Automatic relevance determination (ARD) is used to identify important parameters and reduce the problem to 4 parameters.
4. Performing Predictions
 - Gaussian process (GP) regression is used to train a surrogate model and perform predictions.
5. Creating Response vs. Frequency Plots with the HDF5 Explorer
 - The HDF5 Explorer web app is used to create Response vs. Frequency Plots.

Details of the Structural Model

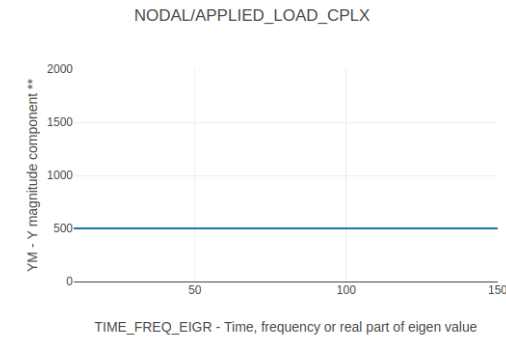
1. Perform a frequency response analysis for different thickness values
2. Create XYPLOTs for nodes 1001, 1003, and 8667



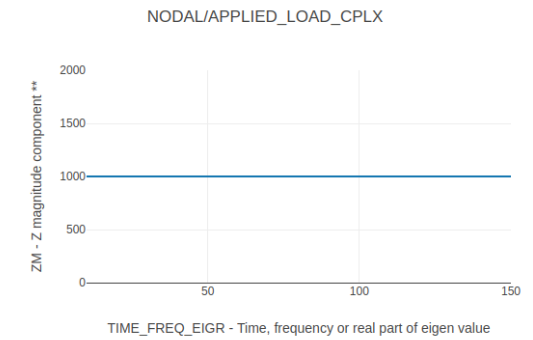
Details of the Structural Model



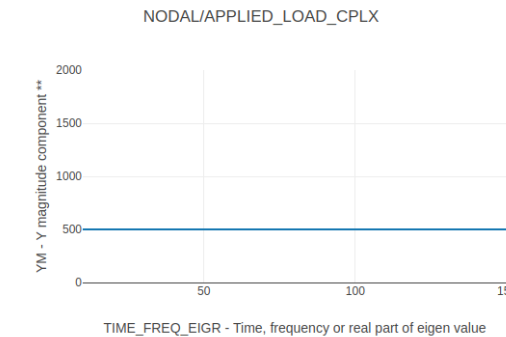
F1 – Load at node 1001, y direction,
Subcase 12



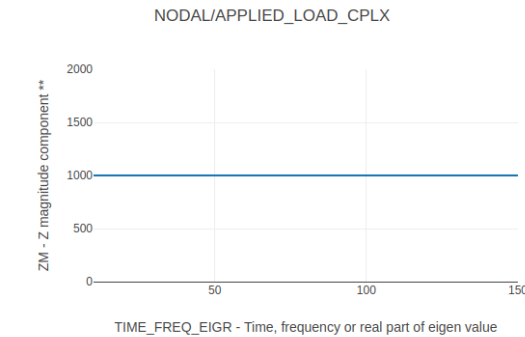
F2 – Load at node 1001, z direction,
Subcase 13



F3 – Load at node 1003, y direction,
Subcase 32



F4 – Load at node 1003, z direction,
Subcase 33



Problem Statement

Design Variables

x1: The thickness of PSHELL 1

x2: The thickness of PSHELL 2

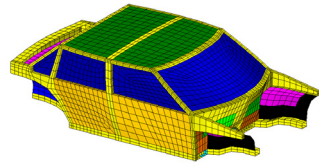
...

x11: The thickness of PSHELL 11

$1.0 < x1, x2, \dots, x11, < 6.0$

Samples

- Batch set 1 – 55 run LHS Design
- Batch set 2 – 40 run LHS Design
- Batch set 3 – 8 run LHS Design



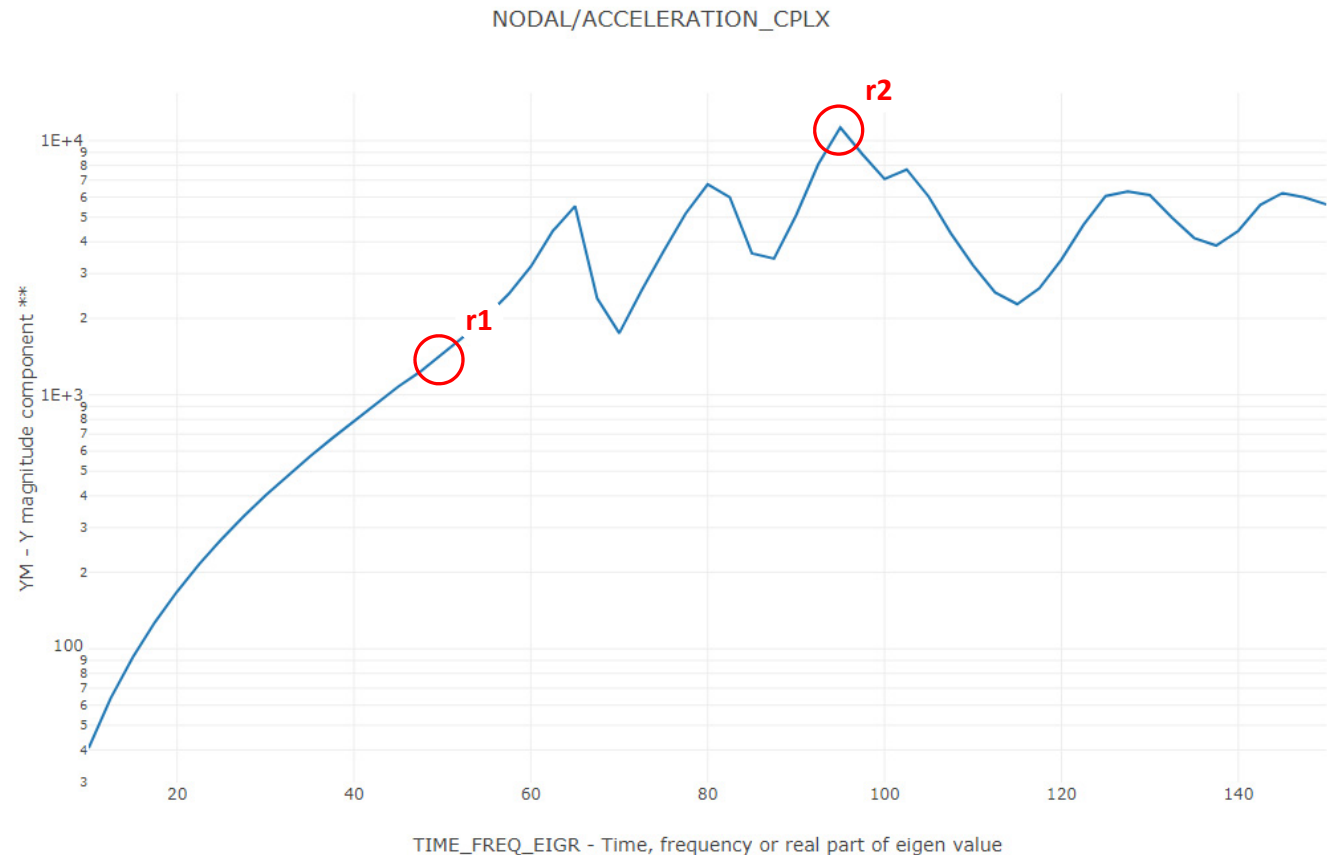
Monitored Responses

| Label | Dataset Name | Field | Field Description | Node ID | SUBCASE | Frequency |
|-------|--------------|-------|----------------------------------|---------|---------|-----------|
| r1 | Acceleration | YM | Y magnitude component | 1001 | 12 | 50 Hz |
| r2 | Acceleration | YM | Y magnitude component | 1001 | 12 | Max Value |
| r3 | Acceleration | ZM | Z magnitude component | 1001 | 13 | Max Value |
| r4 | Acceleration | YM | Y magnitude component | 1003 | 32 | Max Value |
| r5 | Acceleration | ZM | Z magnitude component | 1003 | 33 | Max Value |
| r6 | Pressure | PM | Sound pressure level - magnitude | 8667 | 12 | Max Value |
| r7 | Pressure | PM | Sound pressure level - magnitude | 8667 | 13 | Max Value |
| r8 | Pressure | PM | Sound pressure level - magnitude | 8667 | 32 | Max Value |
| r9 | Pressure | PM | Sound pressure level - magnitude | 8667 | 33 | Max Value |

Problem Statement, Continued

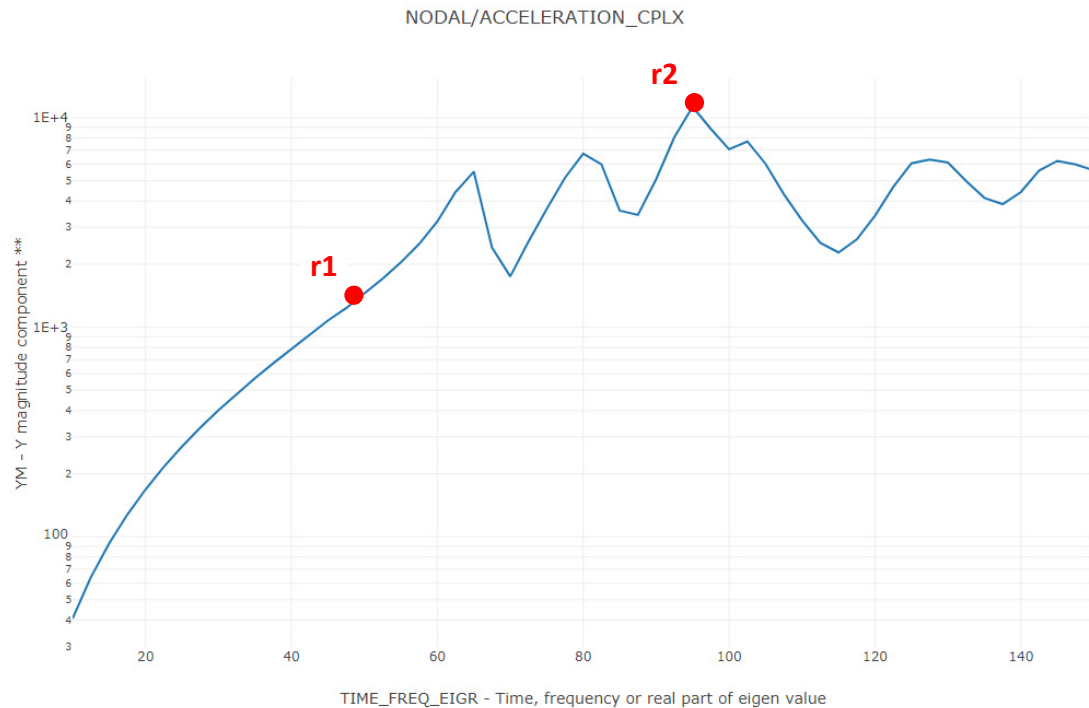
The responses defined in this tutorial correspond to points on frequency response plots

- Response r1 is the acceleration at 50 Hz
- Response r2 is the max acceleration for the forcing frequency range
- Other responses correspond to different node ID, component, subcase number and frequency

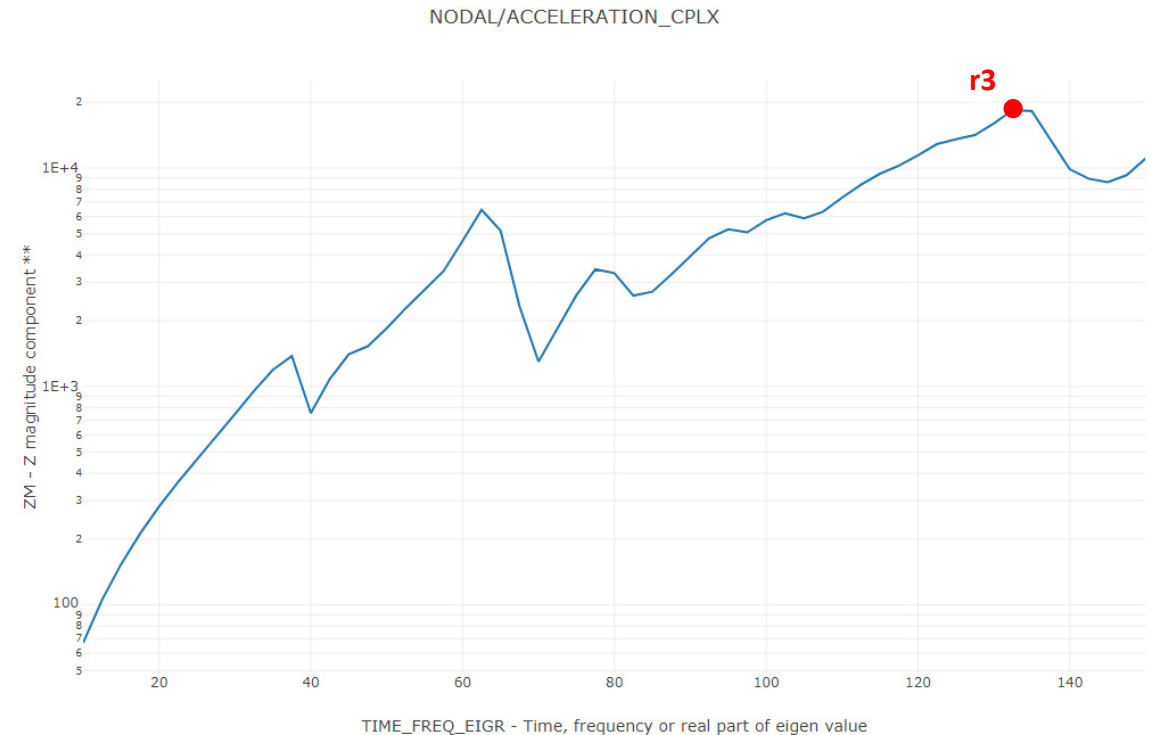


Monitored Responses

r1, r2, r3



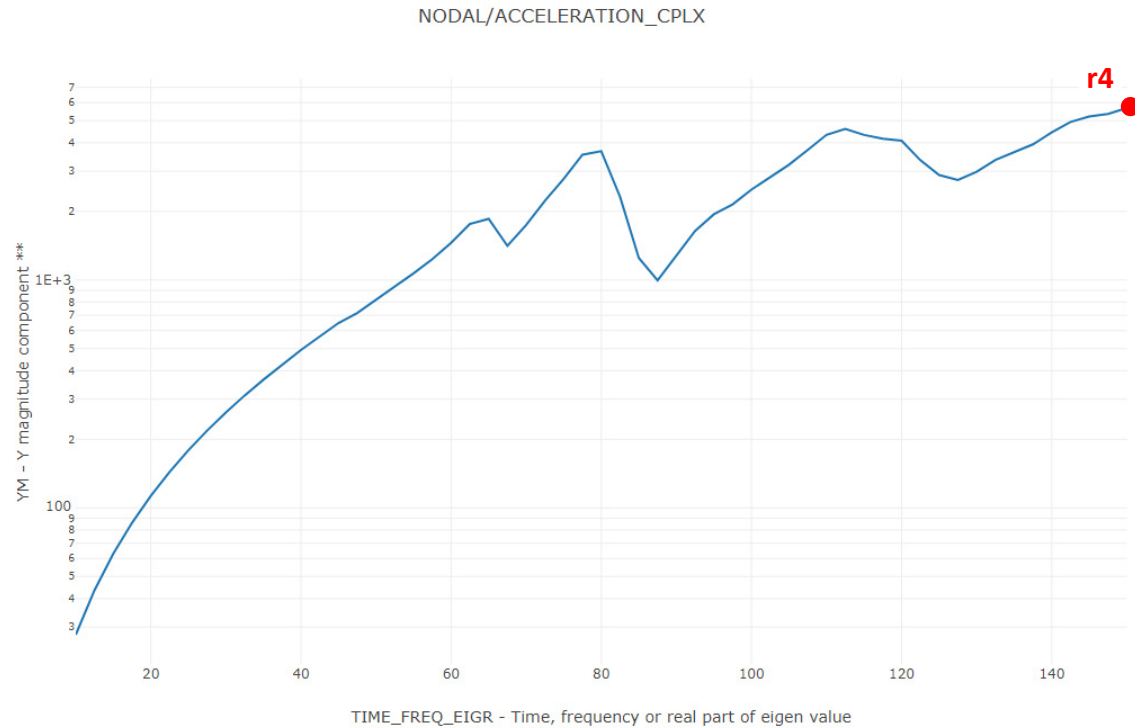
ID: 1001 | SUBCASE: 12 | YM vs. TIME_FREQ_EIGR



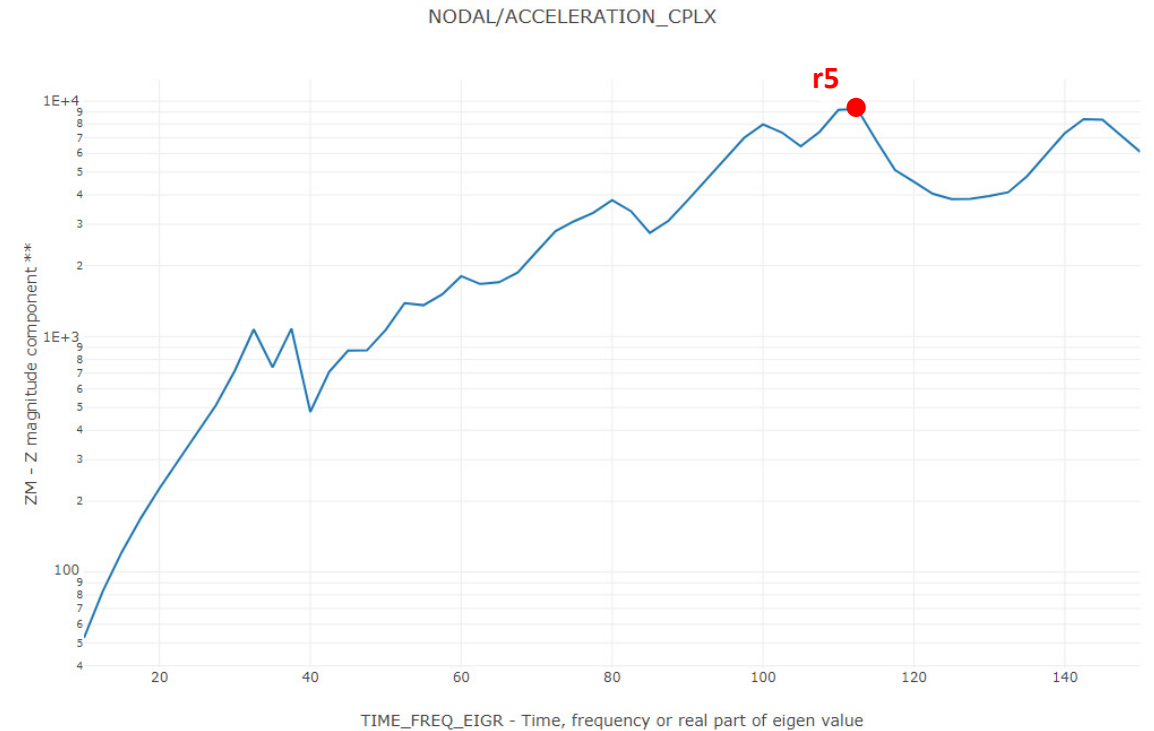
ID: 1001 | SUBCASE: 13 | ZM vs. TIME_FREQ_EIGR

Monitored Responses

r4, r5



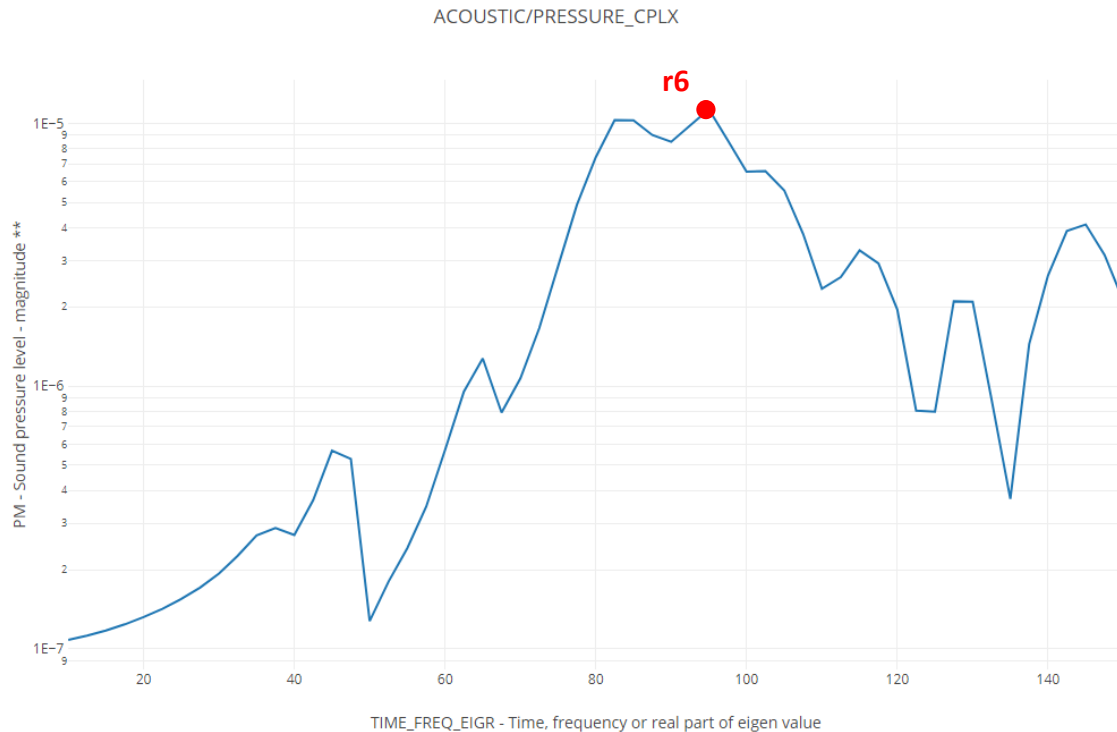
ID: 1003 | SUBCASE: 32 | YM vs. TIME_FREQ_EIGR



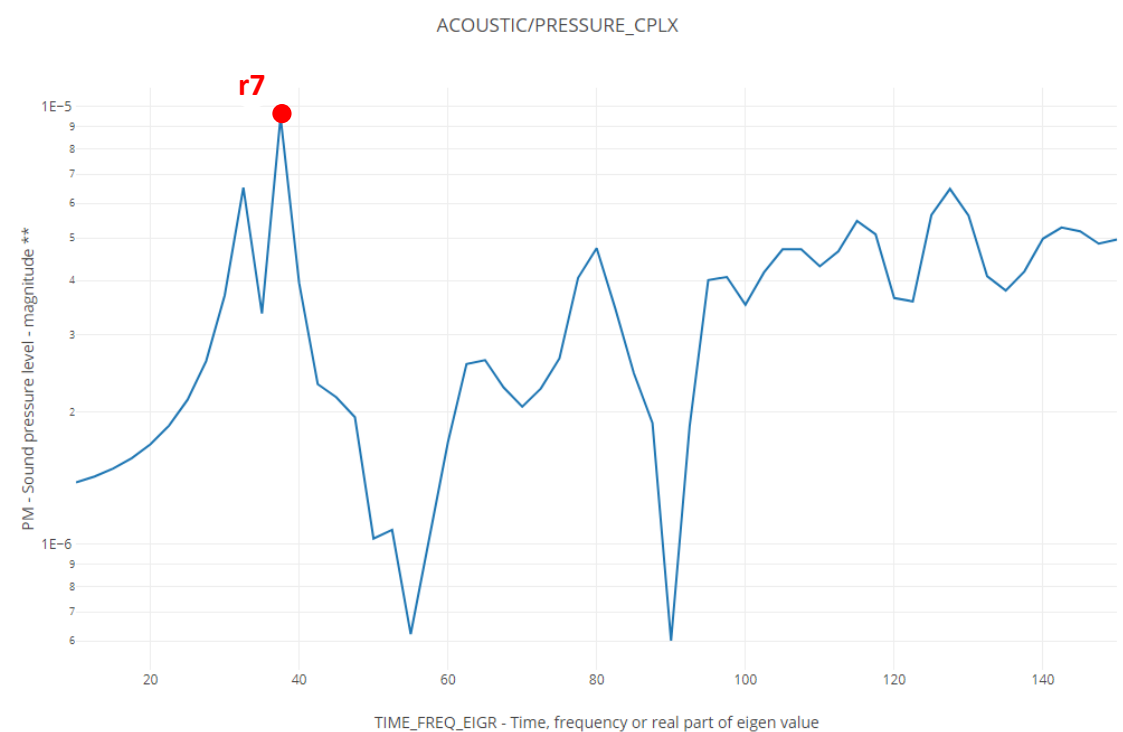
ID: 1003 | SUBCASE: 33 | ZM vs. TIME_FREQ_EIGR

Monitored Responses

r6, r7



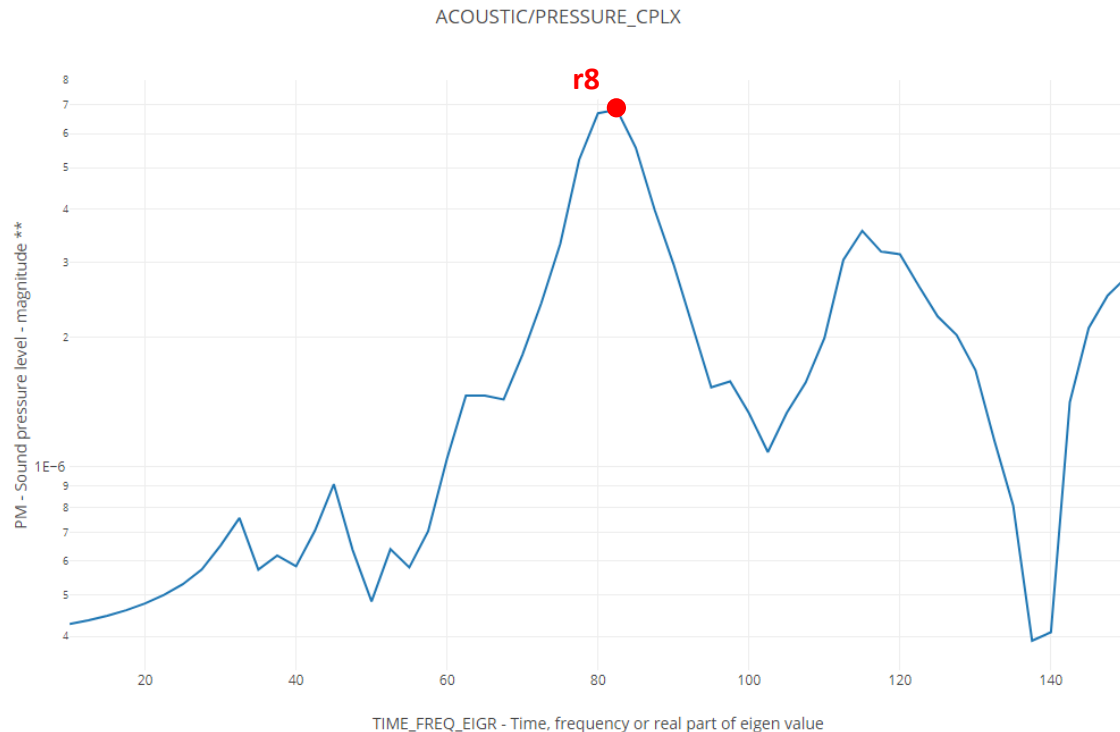
ID: 8667 | SUBCASE: 12 | PM vs. TIME_FREQ_EIGR



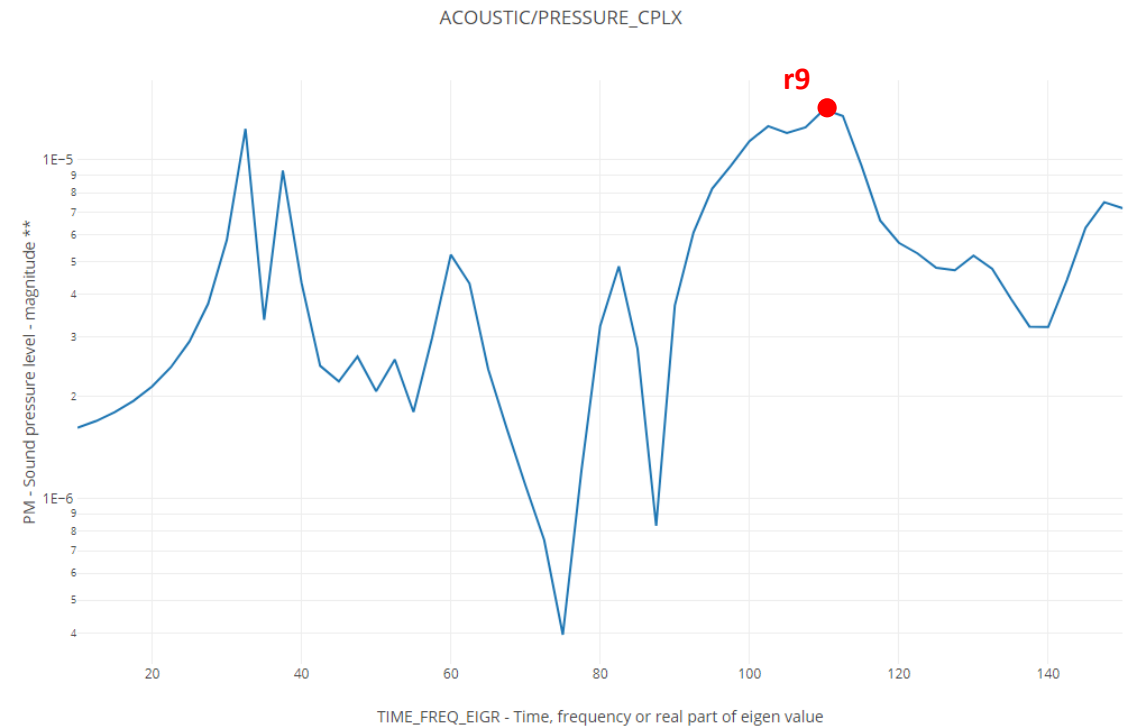
ID: 8667 | SUBCASE: 13 | PM vs. TIME_FREQ_EIGR

Monitored Responses

r8, r9



ID: 8667 | SUBCASE: 32 | PM vs. TIME_FREQ_EIGR

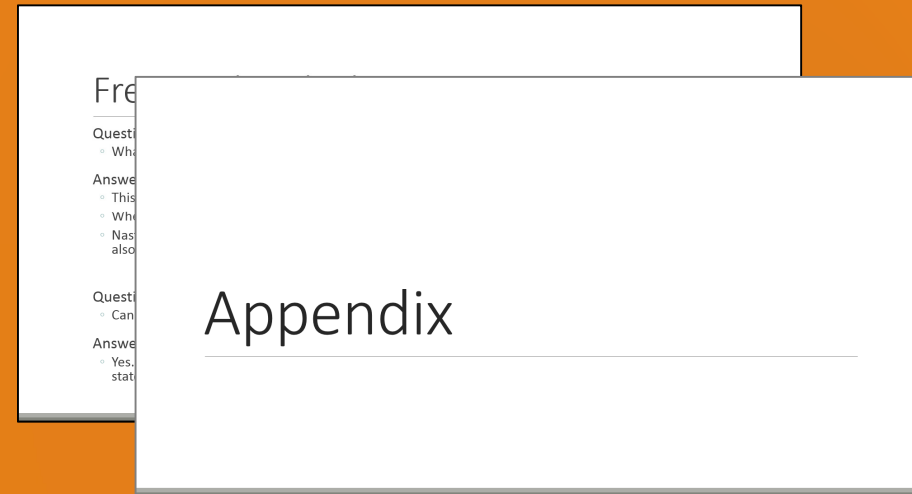


ID: 8667 | SUBCASE: 33 | PM vs. TIME_FREQ_EIGR

More Information Available in the Appendix

The Appendix includes information regarding the following:

- Response Configuration
 - Monitor the maximum or minimum response, whichever has the greatest absolute value: Yes, No or blank
- How to import and edit files
- What is Gaussian Process Regression?



Contact me

- Nastran SOL 200 training
- Nastran SOL 200 questions
- Structural or mechanical optimization questions
- Access to the SOL 200 Web App

[christian@ the-engineering-lab.com](mailto:christian@the-engineering-lab.com)

Tutorial

Tutorial Overview

1. Start with a .bdf or .dat file
2. Use the Machine Learning web app to:
 1. Configure the problem statement
 2. Configure multiple batch runs
3. Use the Prediction Analysis web app to:
 1. Determine parameter relevance (parameter/variable screening)
 2. Perform predictions
4. Use the HDF5 Explorer to:
 1. Create response vs. frequency plots

Special Topics Covered

Training Data – The training data consists of the parameter inputs and respective output responses for multiple MSC Nastran runs. This tutorial describes how to configure multiple MSC Nastran runs, each with different parameter inputs, and how to monitor each response.

Gaussian process regression – This tutorial describes the procedure to use Gaussian process regression to train a surrogate model and make predictions.

Automatic Response Extraction – Often responses are manually or automatically extracted from the F06 file. This becomes challenging when extracting responses from multiple F06 files. This tutorial highlights the web app's ability to automatically extract responses from multiple H5 files with minimal user effort.

Automatic Plots - Multiple plots must be created. This traditionally involves extracting data from result files, for example the F06 file, and using Excel to create the plots. This tutorial highlights the automatic generation of these plots that require minimal user effort.

SOL 200 Web App Capabilities

The Post-processor Web App and HDF5 Explorer are free to MSC Nastran users.

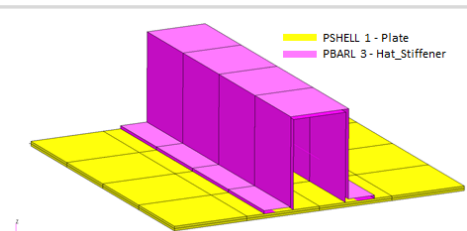
Compatibility

- Google Chrome, Mozilla Firefox or Microsoft Edge
- Windows and Red Hat Linux
- Installable on a company laptop, workstation or server. All data remains within your company.

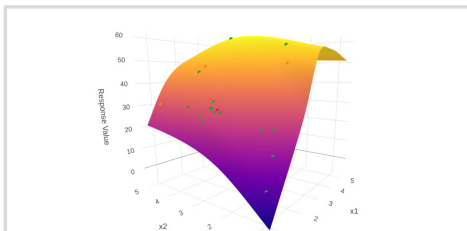
Benefits

- REAL TIME error detection. 200+ error validations.
- REAL TIME creation of bulk data entries.
- Web browser accessible
- Free Post-processor web apps
- +80 tutorials

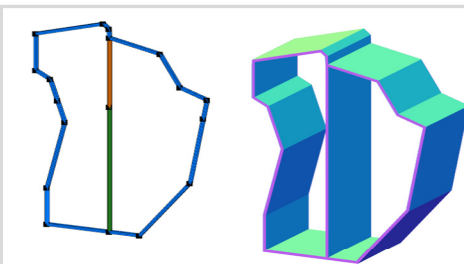
Web Apps



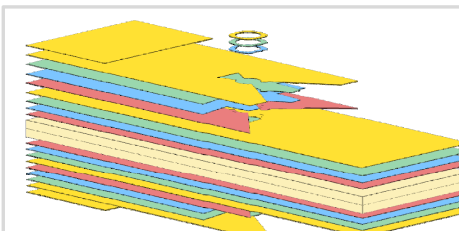
Web Apps for MSC Nastran SOL 200
Pre/post for MSC Nastran SOL 200.
Support for size, topology, topometry, topography, multi-model optimization.



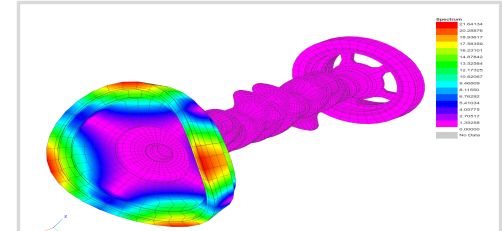
Machine Learning Web App
Bayesian Optimization for nonlinear response optimization (SOL 400)



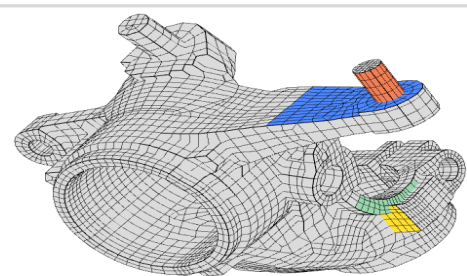
PBMSECT Web App
Generate PBMSECT and PBRSECT entries graphically



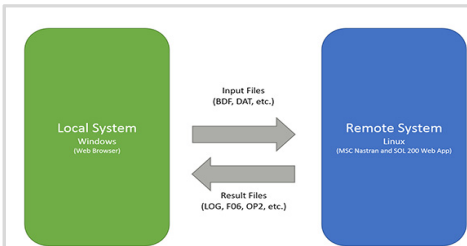
Ply Shape Optimization Web App
Optimize composite ply drop-off locations, and generate new PCOMPG entries



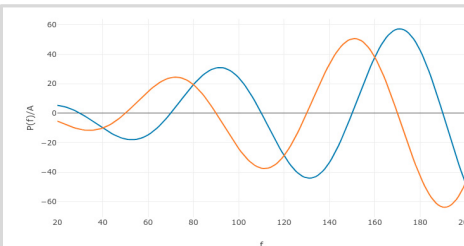
Post-processor Web App
View MSC Nastran results in a web browser on Windows and Linux



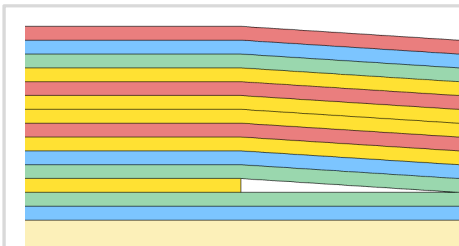
Shape Optimization Web App
Use a web application to configure and perform shape optimization.



Remote Execution Web App
Run MSC Nastran jobs on remote Linux or Windows systems available on the local network



Dynamic Loads Web App
Generate RLOAD1, RLOAD2 and DLOAD entries graphically



Stacking Sequence Web App
Optimize the stacking sequence of composite laminate plies



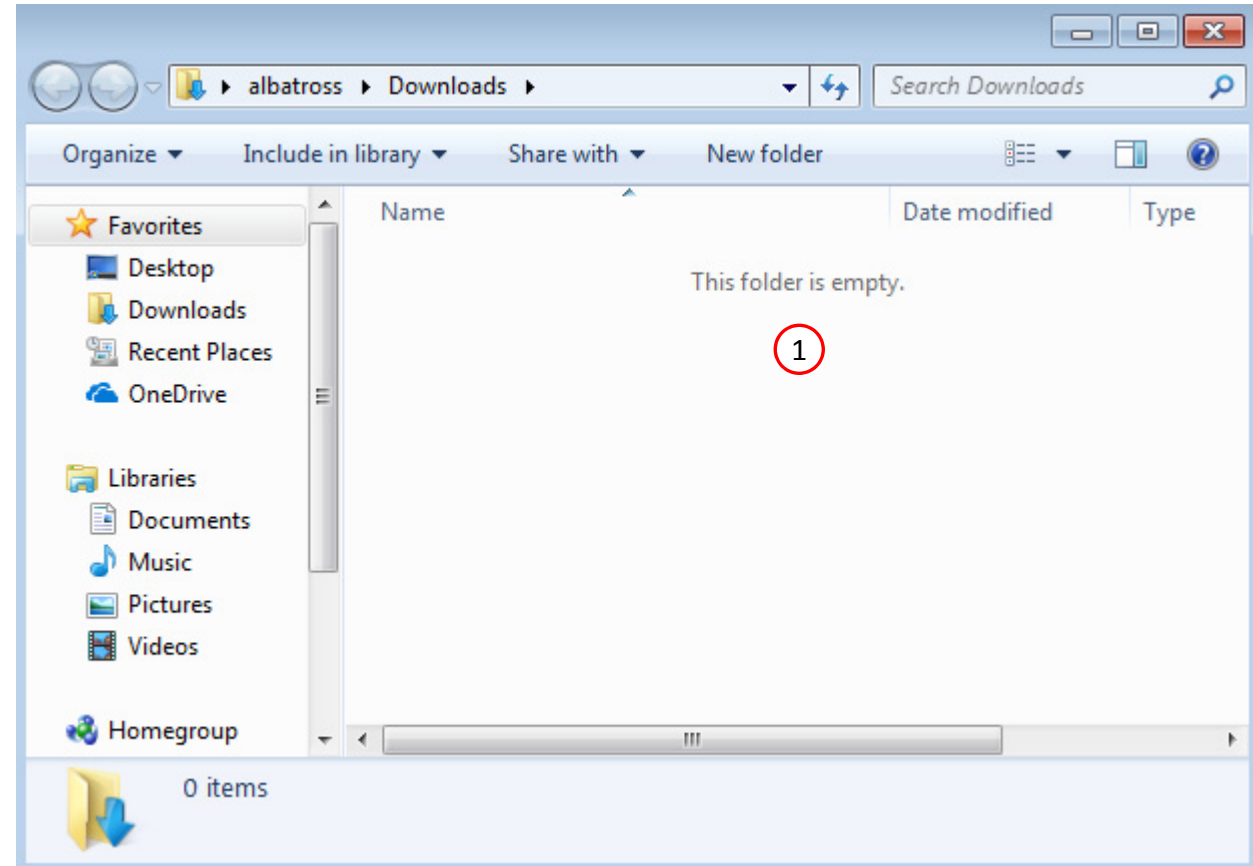
HDF5 Explorer Web App
Create graphs (XY plots) using data from the H5 file

Configuring The Problem Statement

Before Starting

1. Ensure the Downloads directory is empty in order to prevent confusion with other files

- Throughout this workshop, you will be working with multiple file types and directories such as:
 - .bdf/.dat
 - nastran_working_directory
 - .f06, .log, .pch, .h5, etc.
- To minimize confusion with files and folders, it is encouraged to start with a clean directory.



Go to the User's Guide

1. Click on the indicated link

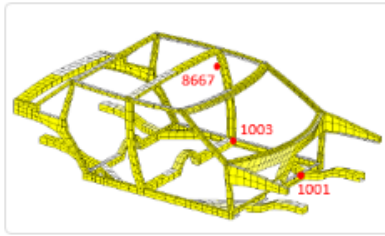
- The necessary BDF files for this tutorial are available in the Tutorials section of the User's Guide.



Obtain Starting Files

1. Find the indicated example
2. Click Link
3. The starting file has been downloaded

- When starting the procedure, all the necessary BDF, or DAT, files must be collected and uploaded together. Relevant INCLUDE files must also be collected and uploaded.

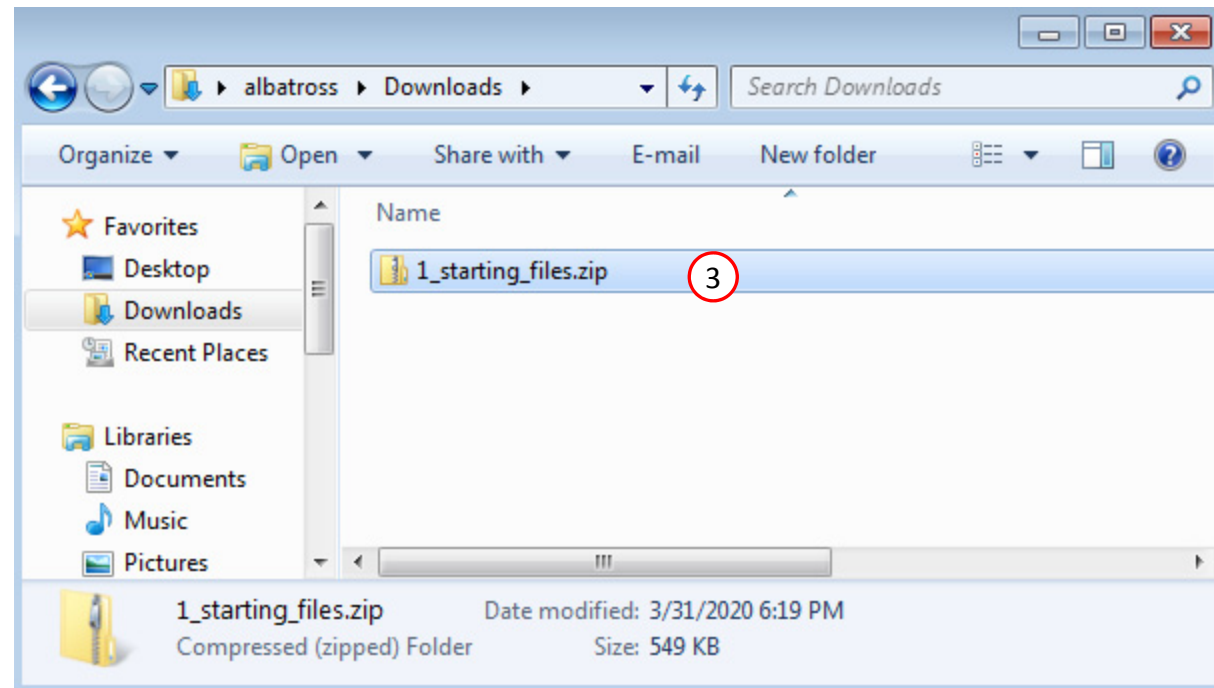


Prediction Analysis, Frequency Response Analysis (SOL 111) 1

Consider a frequency response analysis of a ground vehicle. For different configurations of the ground vehicle, there is a desire to rapidly determine the frequency responses, including accelerations and pressures, while keeping the number of Finite Element (FE) solver runs to a minimum.

This tutorial describes the procedure to use Gaussian process regression as a surrogate model for computationally expensive Finite Element (FE) based simulations. This tutorial walks users through the process of acquiring training data, fitting the surrogate model, making predictions and quantifying uncertainty. In addition, the process to screen variables/parameters via Automatic relevance determination (ARD) is discussed.

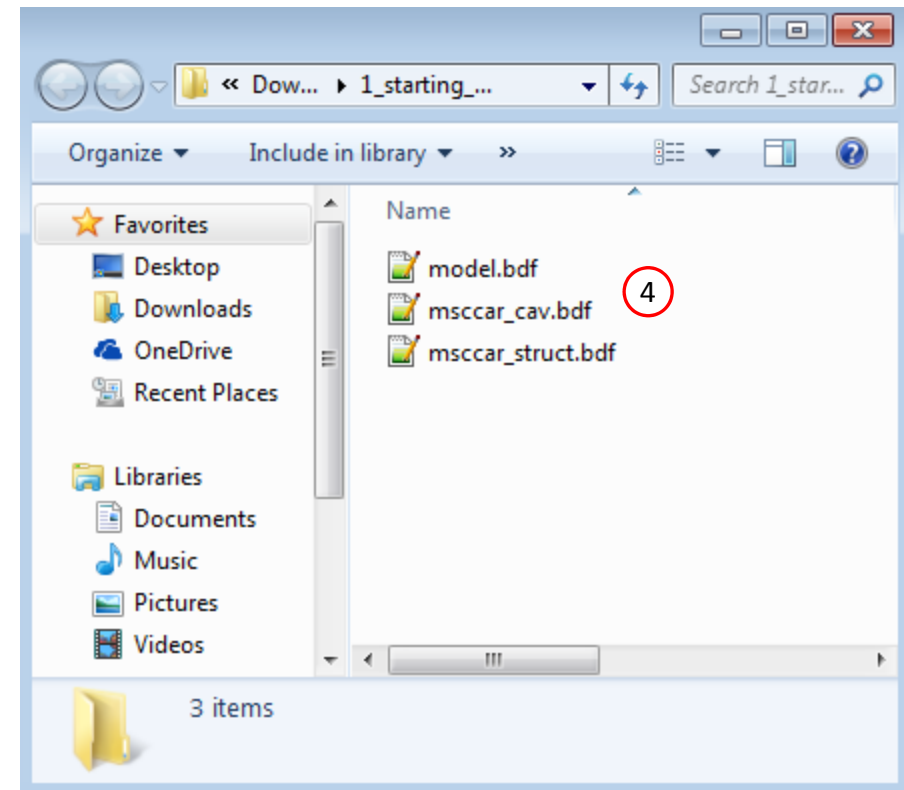
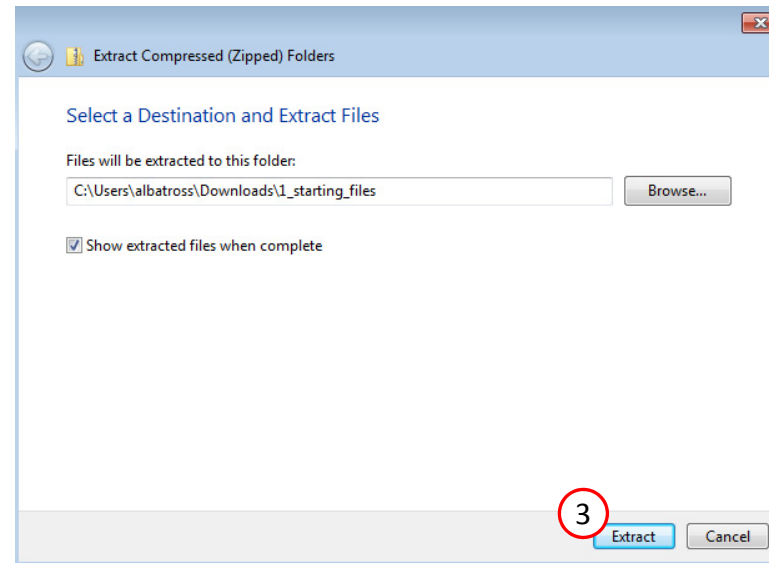
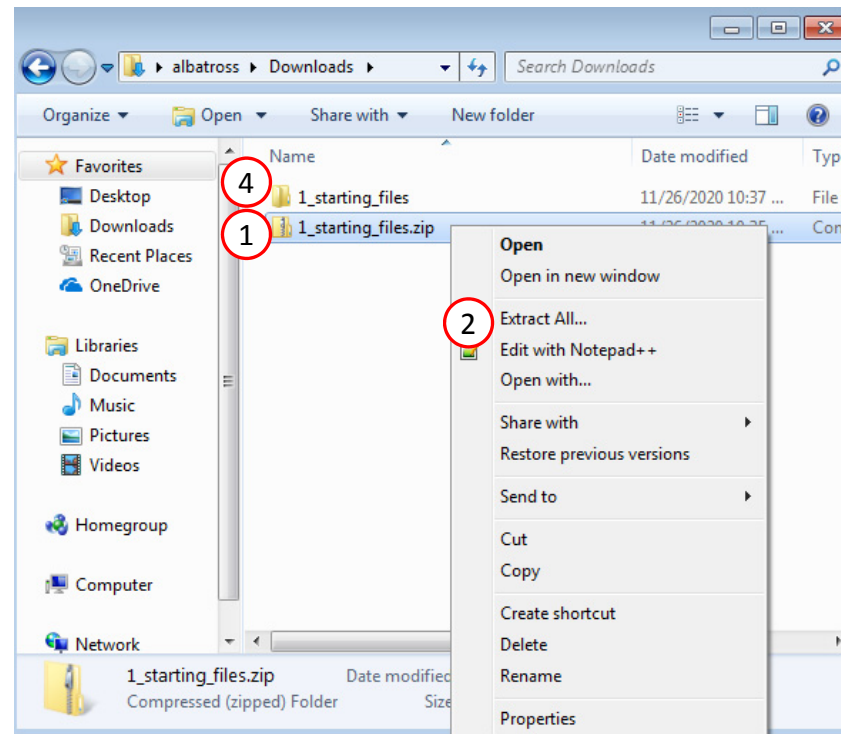
Starting Files: [Link](#) 2
Solution BDF Files: [Link](#)



Obtain Starting Files

1. Right click on the zip file
2. Select Extract All...
3. Click Extract
4. The starting files are now available in a folder

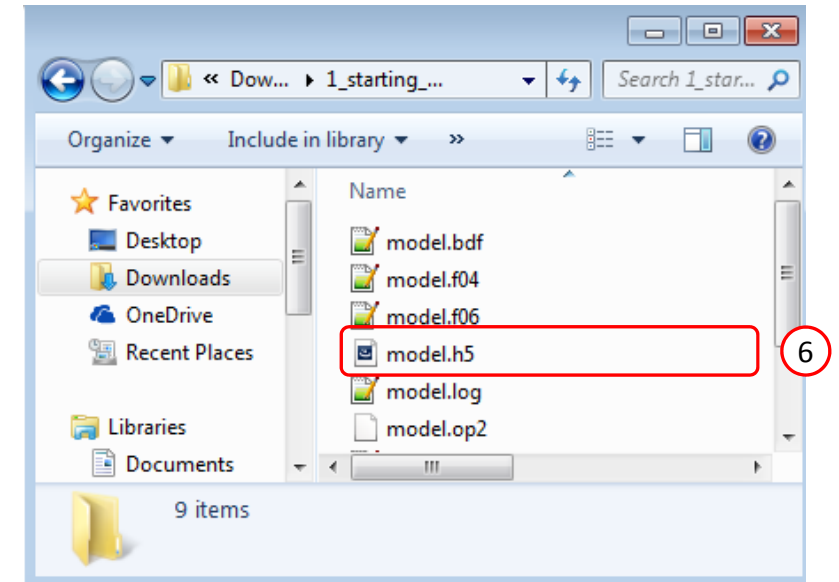
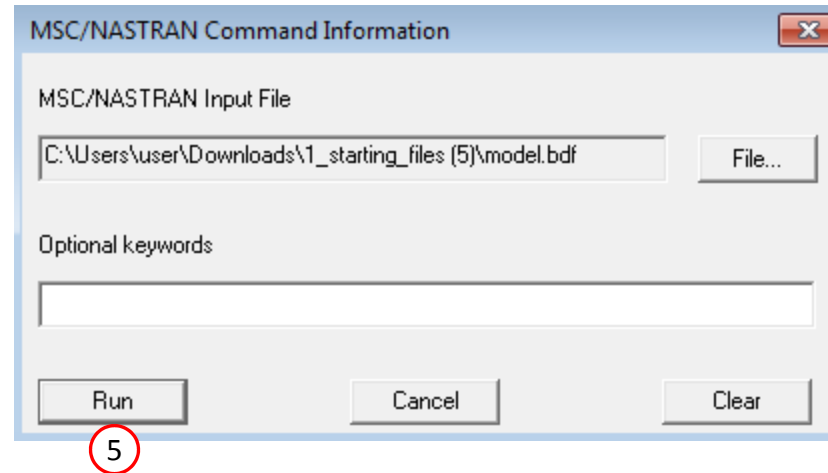
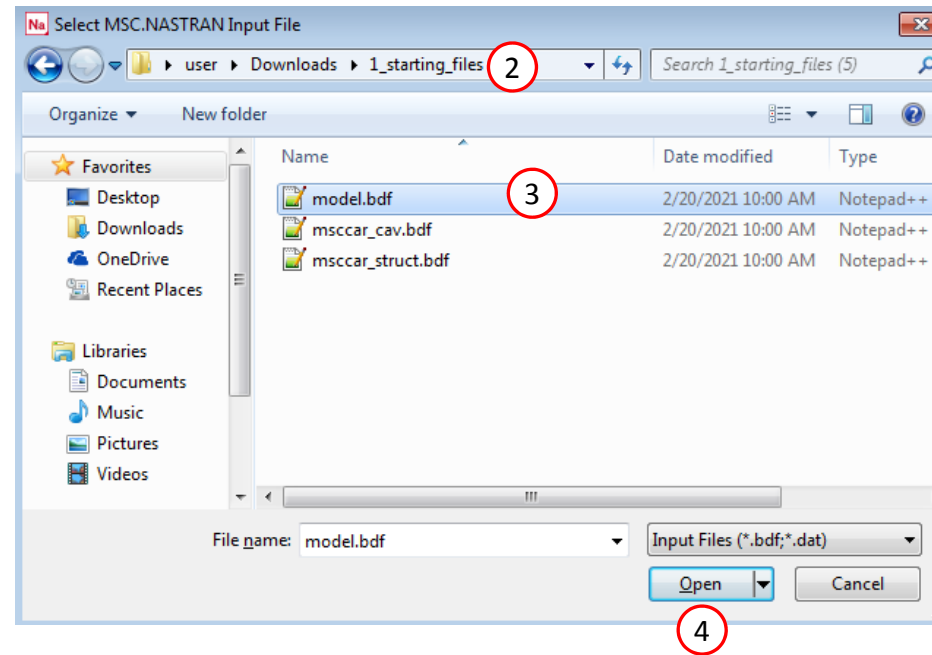
- The starting files for this tutorial are contained in a ZIP file and must be extracted as shown.



Create the Starting H5 File

A starting H5 file must be created. This H5 file will be used to configure the responses later on.

1. Double click the MSC Nastran desktop shortcut
2. Navigate to the directory named 1_starting_files
3. Select the indicated file
4. Click Open
5. Click Run
6. The starting H5 file is created



Use the same MSC Nastran version throughout this exercise

The following applies if you have multiple versions of MSC Nastran installed.

To ensure compatibility, use the same MSC Nastran version throughout this exercise. For example, scenario 1 is OK but scenario 2 is NOT OK.

- Scenario 1 - OK
 - MSC Nastran 2021 is used to create the starting H5 file.
 - MSC Nastran 2021 is used for each run during Machine Learning or Parameter study.
- Scenario 2 – NOT OK
 - MSC Nastran 2018.2 is used to create the starting H5 file.
 - MSC Nastran 2021 is used for each run during Machine Learning or Parameter study.

Using the same MSC Nastran version is critical for consistent response extraction from the H5 file. A response configured for Nastran version X may not match in Nastran version Y, which leads to unsuccessful response extraction from the H5 files. The goal is to make sure all H5 files generated are from the same MSC Nastran version.

Open the Correct Page

1. Click on the indicated link

- MSC Nastran can perform many optimization types. The SOL 200 Web App includes dedicated web apps for the following:
 - Optimization for SOL 200 (Size, Topology, Topometry, Topography, Local Optimization, Sensitivity Analysis and Global Optimization)
 - Multi Model Optimization
 - Machine Learning
- The web app also features the HDF5 Explorer, a web application to extract results from the H5 file type.



Select BDF Files

1. Select files 3 files selected

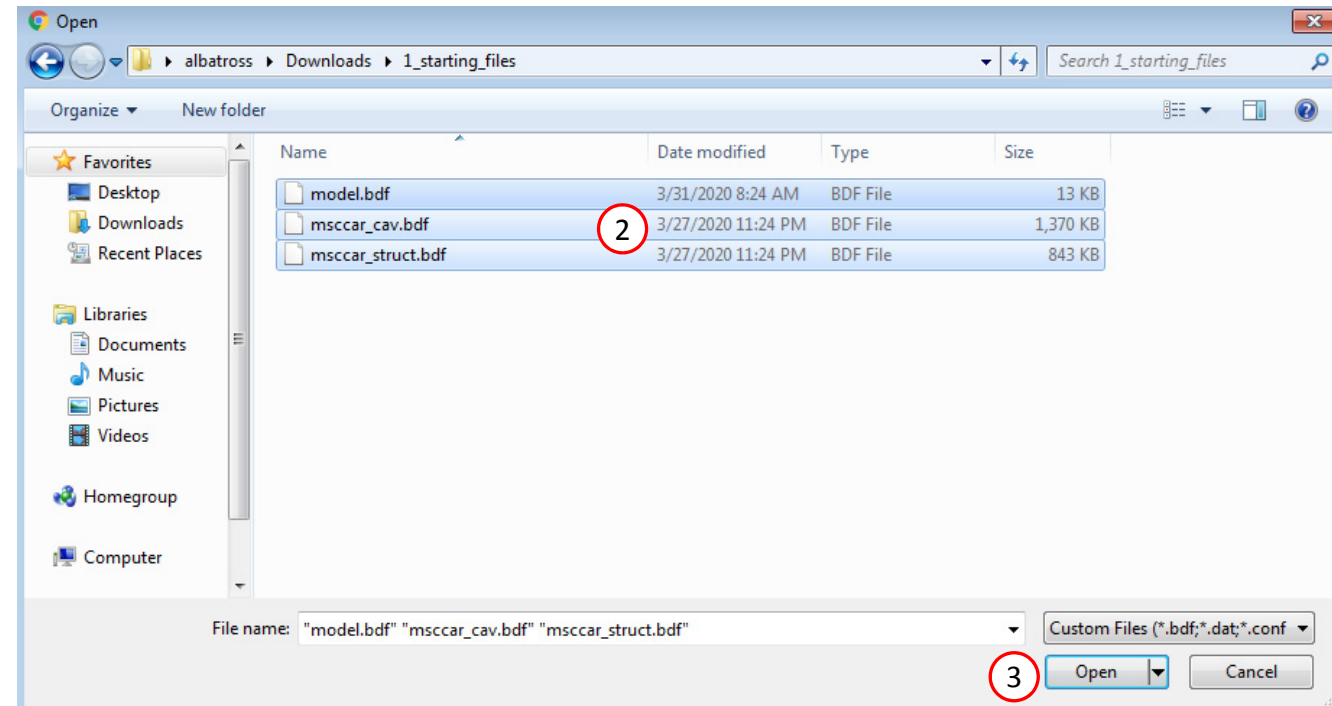
Inspecting: 100%

4. Upload files

Uploading: 100 %

Select BDF Files

1. Click Select files
2. Select the indicated files
3. Click Open
4. Click Upload files



Parameters

- Set the following fields as parameters
 - x1: The thickness of PSHELL 1
 - x2: The thickness of PSHELL 2
 - ...
 - x11: The thickness of PSHELL 11
- Parameters have been created for the selected fields
- For each parameter, use the following settings:
 - Low: 1.
 - High: 6.

- Bulk data entries will always be displayed in the small field format.
- Only fields that have real or integer data entries may be selected as parameters. If the field is blank or contains only characters, the field may not be selected.

Select Parameters

| \$ _1_ _2_ _3_ _4_ _5_ _6_ | | | | | |
|---|--------|---------|------------------|--------|----------|
| EIGRL | 1 | | 225. | | |
| EIGRL | 2 | | 300. | | |
| FORCE | 212 | 1001 | | 500. | 0.0 |
| FORCE | 213 | 1001 | | 1000. | 0.0 |
| FORCE | 232 | 1003 | | 500. | 0.0 |
| FORCE | 233 | 1003 | | 1000. | 0.0 |
| FREQ1 | 5 | 10. | 2.5 | 56 | |
| MAT1 | 7 | 21000.0 | | 0.3 | 7.90E-06 |
| MAT1 | 8 | 62000.0 | | 0.24 | 2.30E-06 |
| MAT10 | 6 | | 1.23E-12340000.0 | | |
| PARAM | G | 0.06 | | | |
| PARAM | GFL | 0.12 | | | |
| PARAM | LFREQ | 0.1 | | | |
| PARAM | PREFDB | 2.E-11 | | | |
| PARAM | WTMASS | .001 | | | |
| PSHELL | 1 | 7 | %x1% | 7 | 1.0 |
| PSHELL | 2 | 7 | %x2% | 7 | 1.0 |
| PSHELL | 3 | 7 | %x3% | 7 | 1.0 |
| PSHELL | 4 | 7 | %x4% | 7 | 1.0 |
| PSHELL | 5 | 7 | %x5% | 7 | 1.0 |
| PSHELL | 6 | 7 | %x6% | 7 | 1.0 |
| PSHELL | 7 | 7 | %x7% | 7 | 1.0 |
| PSHELL | 8 | 7 | %x8% | 7 | |
| PSHELL | 9 | 7 | %x9% | 7 | |
| PSHELL | 10 | 7 | %x10% | 7 | |
| PSHELL | 11 | 8 | %x11% | 8 | |
| RBE3 | 1501 | | 1001 | 123456 | 1.0 |
| | 3646 | 2685 | 5709 | 2697 | 3819 |

Configure Parameters

| Delete | Parameter | Status | Low | High | Comments |
|--------|-----------|--------|-----|------|----------------------|
| | x1 | | 1. | 6. | Field 4 of PSHELL 1 |
| | x2 | | 1. | 6. | Field 4 of PSHELL 2 |
| | x3 | | 1. | 6. | Field 4 of PSHELL 3 |
| | x4 | | 1. | 6. | Field 4 of PSHELL 4 |
| | x5 | | 1. | 6. | Field 4 of PSHELL 5 |
| | x6 | | 1. | 6. | Field 4 of PSHELL 6 |
| | x7 | | 1. | 6. | Field 4 of PSHELL 7 |
| | x8 | | 1. | 6. | Field 4 of PSHELL 8 |
| | x9 | | 1. | 6. | Field 4 of PSHELL 9 |
| | x10 | | 1. | 6. | Field 4 of PSHELL 10 |
| | x11 | | 1. | 6. | Field 4 of PSHELL 11 |

Responses

1. Click Responses
2. Click Select files
3. Select the indicated file
4. Click Open
5. Click Upload files

- On this page, the H5 file is uploaded to the web app.

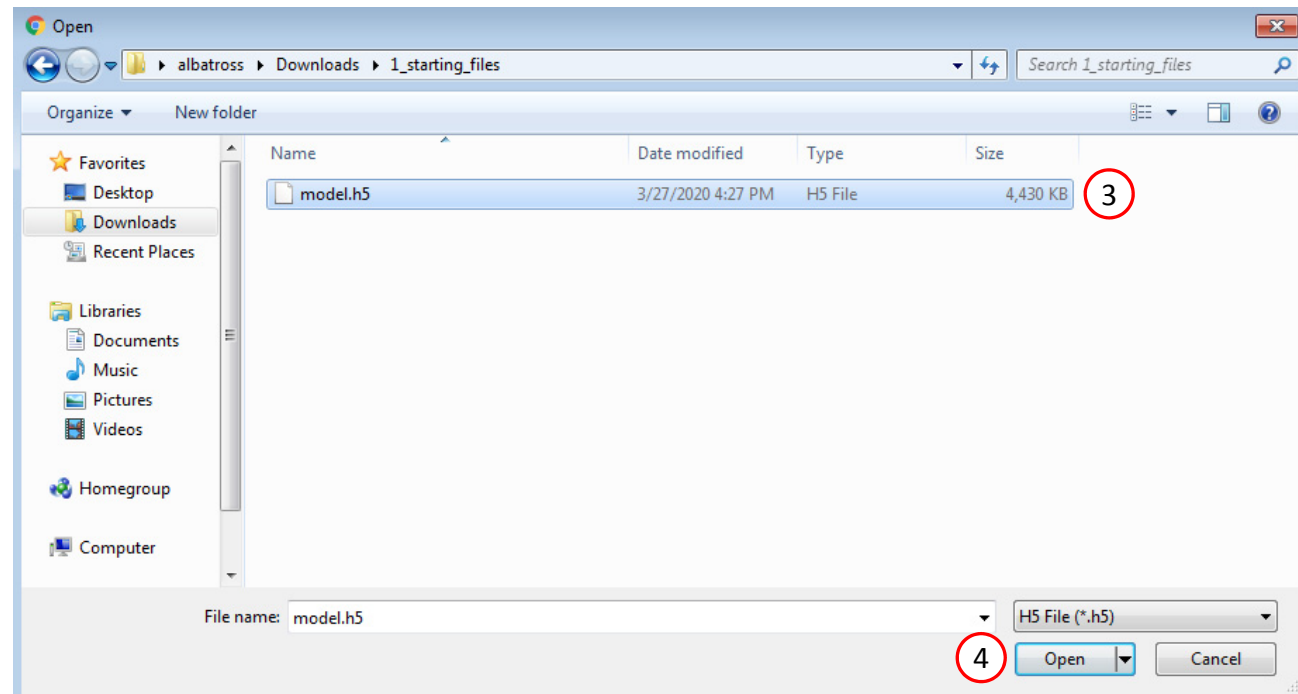
Upload .h5 File

2 1. Select files model.h5

5 2. Upload files

Uploading

Loading



Adjust the Column Width

- 1. Optional - Use at your liking the buttons at the top right hand corner to adjust the width of the left and right columns

SOL 200 Web App - Machine LearningParametersSamplesResponsesDownloadResultsConnectionSettingsHome

Select Responses to MonitorSession ID: 3710HDF5

Select Dataset

NODAL/ACCELERATION

NODAL/DISPLACEMENT

NODAL/GRID_WEIGHT

NODAL/VELOCITY_CPLX

SUMMARY/EIGENVALUE

Acquired Dataset

NODAL/GRID_WEIGHT - 0

Reset Filters

| SAMPLE | DOMAIN_ID | SUBCASE | STEP | ANA |
|--------|-----------|---------|------|-----|
|--------|-----------|---------|------|-----|

View Responses to Monitor

Monitored Responses

Hide/Show Columns

Reset Filters

Download CSV

| Delete | Label | Status | Objective | Lower Bound | Upper Bound | Monitor th of the Fil cycle (SO |
|--------------|-------|--------------|--------------|-------------|-------------|---------------------------------|
| <div>✕</div> | r1 | <div>⬆</div> | <div>⌵</div> | Lower | Upper | |

SOL 200 Web App - Machine LearningParametersSamplesResponsesDownloadResultsConnectionSettingsHome

Select Responses to MonitorSession ID: 3710HDF5

Select Dataset

NODAL/ACCELERATION_CPLX

NODAL/DISPLACEMENT_CPLX

NODAL/GRID_WEIGHT

NODAL/VELOCITY_CPLX

SUMMARY/EIGENVALUE

Specify Entities

0

(ID)

Examples: 0, etc.

Acquired Dataset

NODAL/GRID_WEIGHT - 0

Reset Filters

| SAMPLE | DOMAIN_ID | SUBCASE | STEP | ANALYSIS | TIME_FREQ_EIGR | |
|-------------------|-----------|----------------|-------------|---------------|---|----------------------|
| | | | | | | Im eig ap |
| lame of H5 File** | | Subcase number | Step number | Analysis type | Time, frequency or real part of eigen value | |
| model | | 0 | 0 | 0 | 0 | |

View Responses to Monitor

Monitored Responses

Hide/Show Columns

Reset Filters

Download CSV

| Delete | Label | Status | Objective | L B |
|--------------|-------|--------------|--------------|-----|
| <div>✕</div> | r1 | <div>⬆</div> | <div>⌵</div> | Lc |

5

10

20

30

50

100

Select Responses

1. Select the following dataset:
NODAL/ACCELERATION_CPLX
2. Use the horizontal scroll bar until the column TIME_FREQ_EIGR is visible
3. Use the vertical scroll bar until the value 50 is visible
4. Select the value 50 to only display rows that correspond to 50 Hz
5. Search for the column YM and click the indicated cell
6. A new response r1 is created
7. Set the following option:
 - Monitor the maximum or minimum response, whichever has the greatest absolute value [...] response : No

- The responses defined in this tutorial correspond to points on frequency response plots
- Refer to the Appendix for an explanation on the use of the following:
 - Use MAX absolute value of response: Yes, No or blank

Select Responses to Monitor

Session ID: 1918 HDF5

Select Dataset

- ACOLUSTIC/PRESSURE_CPLX
- NODAL/ACCELERATION_CPLX** (1)
- NODAL/DISPLACEMENT_CPLX
- NODAL/GRID_WEIGHT
- NODAL/VELOCITY_CPLX
- SUMMARY/EIGENVALUE

Acquired Dataset

| | YM | ZM |
|----------------|--------------------------|--------------------------|
| | Y magnitude component ** | Z magnitude component ** |
| 1443.47629... | 477.077968... | |
| 954.136... | 1845.58292... | |
| 819.3563119... | 176.530483... | |
| 353.060967... | 1068.88874... | |

Specify Entities

1001, 1003

Grid identifier (ID)
Examples: 1001, 1003, etc.

☒ Auto Execute

Acquire Dataset

✓ Acquisition complete and successful

Time, frequency or real part of eigen value

47.5
50 (4)
52.5
55
57.5

View Responses to Monitor

Monitored Responses

| Delete | Label | Status | Objective | Lower Bound | Upper Bound | Monitor the response of the FINAL design cycle (SOL 200 only) | Monitor the maximum or minimum response, whichever has the greatest absolute value |
|-------------------------------------|--------|--------|-----------|-------------|-------------|---|--|
| <input checked="" type="checkbox"/> | r1 (6) | | | Lower | Upper | | No - Monitor response of correspor (7) |

Select Responses

1. Use the horizontal scroll bar until the column TIME_FREQ_EIGR is visible
2. Select the value 10 to only display rows that correspond to 10 Hz
3. Search for the column YM and click the 4 indicated cells
4. Four (4) new response r2, r3, r4 and r5 have been created
5. Set the following option for these 4 new responses:
 - Monitor the maximum or minimum response, whichever has the greatest absolute value [...] response : Yes

- The responses defined in this tutorial correspond to points on frequency response plots
- Refer to the Appendix for an explanation on the use of the following:
 - Use MAX absolute value of response: Yes, No or blank

Select Responses to Monitor

Session ID: 1918

HDF5

View Responses to Monitor

Select Dataset

ACOUSTIC/PRESSURE_C
NODAL/ACCELERATION
NODAL/DISPLACEMENT
NODAL/GRID_WEIGHT
NODAL/VELOCITY_CPLX
SUMMARY/EIGENVALUE

Specify Entities

1001, 1003

Grid identifier (ID)

Examples: 1001, 1003, etc.

☒ Auto Execute

Acquire Dataset

☒ Acquisition complete and successful

Acquired Dataset

NODAL/ACCELERATION_CPLX - 1001, 1003

| YM | ZM |
|--------------------------|--------------------------|
| Y magnitude component ** | Z magnitude component ** |
| 40.6942001... | 12.6812822... |
| 25.3625645... | 66.9888923... |
| 27.7756523... | 4.59164346... |
| 9.18328692... | 52.4694803... |

Reset Filters

| TIME_FREQ_EIGR |
|---|
| Time, frequency or real part of eigen value |
| 10 |
| 12.5 |
| 15 |
| 17.5 |
| 20 |

Monitored Responses

| Delete | Label | Status | Objective | Lower Bound | Upper Bound | Monitor the response of the FINAL design cycle (SOL 200 only) | Monitor the maximum or minimum response, whichever has the greatest absolute value |
|-------------------------------------|-------|-------------------------------------|-----------|-------------|-------------|---|--|
| <input checked="" type="checkbox"/> | r1 | <input checked="" type="checkbox"/> | | Lower | Upper | | No - Monitor response of correspor |
| <input checked="" type="checkbox"/> | r2 | <input checked="" type="checkbox"/> | | Lower | Upper | | Yes - Monitor the maximum respon |
| <input checked="" type="checkbox"/> | r3 | <input checked="" type="checkbox"/> | | Lower | Upper | | Yes - Monitor the maximum respon |
| <input checked="" type="checkbox"/> | r4 | <input checked="" type="checkbox"/> | | Lower | Upper | | Yes - Monitor the maximum respon |
| <input checked="" type="checkbox"/> | r5 | <input checked="" type="checkbox"/> | | Lower | Upper | | Yes - Monitor the maximum respon |

| Design cycle (SOL 200 only) | Monitor the maximum or minimum response, whichever has the greatest absolute value |
|-----------------------------|--|
| | No - Monitor response of correspor |
| | Yes - Monitor the maximum respon |
| | Yes - Monitor the maximum respon |
| | Yes - Monitor the maximum respon |
| | Yes - Monitor the maximum respon |

Select Responses

1. Select the following dataset:
ACOUSTIC/PRESSURE_CPLX
2. Use the horizontal scroll bar until the column TIME_FREQ_EIGR is visible
3. Select the value 10 to only display rows that correspond to 10 Hz
4. Search for the column PM and click the 4 indicated cells
5. Four (4) new response r6, r7, r8 and r9 have been created
6. Set the following option for these 4 new responses:
 - Monitor the maximum or minimum response, whichever has the greatest absolute value [...]
response: Yes

- The responses defined in this tutorial correspond to points on frequency response plots
- Refer to the Appendix for an explanation on the use of the following:
 - Monitor the maximum or minimum response, whichever has the greatest absolute value :
Yes, No or blank

Select Responses to Monitor

Session ID: 8345

HDF5

Select Dataset 1

ACOUSTIC/PRESSURE_CPLX

Specify Entities

8667

Examples: 8667, etc.

☒ Auto Execute

Acquire Dataset

Acquisition complete and successful

Acquired Dataset

ACOUSTIC/PRESSURE_CPLX - 8667

| PM | PRMSM |
|-------------------------------------|---|
| Sound pressure level - magnitude ** | RMS Sound pressure level - magnitude ** |
| 1.08079395... | 7.64236737... |
| 0.00000138... | 9.77244792... |
| 4.27705612... | 3.02433538... |
| 0.00000161... | 0.000001142... |

TIME_FREQ_EIGR

Time, frequency or real part of eigen value

10

2

View Responses to Monitor

Monitored Responses

| Delete | Label | Status | Objective | Lower Bound | Upper Bound | Monitor the response of the FINAL design cycle (SOL 200 only) | Monitor the maximum or minimum response, whichever has the greatest absolute value |
|--------|-------|--------|-----------|-------------|-------------|---|--|
| | r1 | | | | | | NO YES |
| | r2 | | | | | | No - Monitor response of correspo |
| | r3 | | | | | | Yes - Monitor the maximum respon |
| | r4 | | | | | | Yes - Monitor the maximum respon |
| | r5 | | | | | | Yes - Monitor the maximum respon |
| | r6 | | | | | | Yes - Monitor the maximum respon |
| | r7 | | | | | | Yes - Monitor the maximum respon |
| | r8 | | | | | | Yes - Monitor the maximum respon |
| | r9 | | | | | | Yes - Monitor the maximum respon |

5

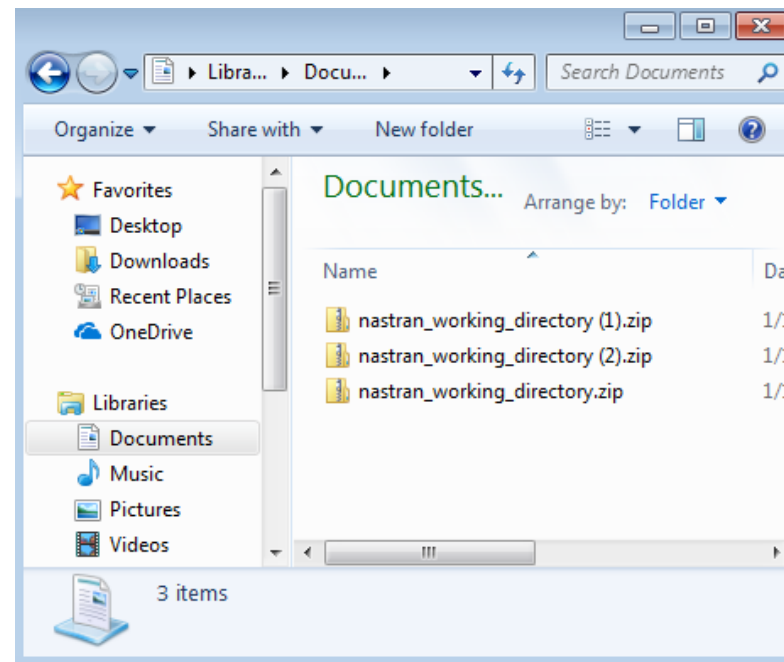
6

| |
|----------------------------------|
| Yes - Monitor the maximum respon |
| Yes - Monitor the maximum respon |
| Yes - Monitor the maximum respon |
| Yes - Monitor the maximum respon |

Configuring Multiple Batch Runs

Samples

In the following slides, we will configure 3 batches to run.



| Batch | File Name | Number of Runs | Number of Parameters | Purpose |
|-------|-----------------------------------|----------------|----------------------|---|
| 1 | nastran_working_directory.zip | 55 | 11 | This configuration includes 11 parameters. The goal is to use the data from the 55 run set to screen parameters and reduce the problem to 4 parameters. Automatic relevance determination (ARD) is used to identify the 4 most relevant parameters. |
| 2 | nastran_working_directory (1).zip | 40 | 4 | This configuration includes 4 parameters. The goal of this 40 run set is to produce training data to fit the surrogate model and make predictions. |
| 3 | nastran_working_directory (2).zip | 8 | 4 | This is an 8 run configuration. This set is used to compare the predicted responses with MSC Nastran responses. |

Samples

1. Click Samples
2. Ensure the following design is selected:
Latin Hypercube, Reproducible
3. Set Number of Samples to 55
4. The samples have been updated, note that samples 1, 2, 3, ..., 55 are visible
5. The indicated controls can be used to display the other samples

- An initial 55 MSC Nastran runs will be executed to generate training data. The training data will be used for parameter/variable screening, via ARD, to reduce the dimensionality of the problem from 11 to 4 parameters.
- For parameter screening purposes, 5 runs per parameter are used. Since there are 11 parameters configured, a total of 55 MSC Nastran runs have been configured for later execution.
- Later on, when the goal is to fit the surrogate model for prediction purposes, 10 runs per parameter is used.

SOL 200 Web App - Machine Learning

Parameters Samples Responses Download Results Connection Settings Home

1

Configure Samples

Design

Latin Hypercube, Reproducible 2

+ Info

Number of Samples

55 3

→

Samples to Run

+ Options

4

| | Parameters | | | |
|---------------|------------|----------|----------|----------|
| Sample Number | x1 | x2 | x3 | x4 |
| 1 | 3.308001 | 3.912181 | 2.622108 | 3.752609 |
| 2 | 2.788307 | 3.581974 | 4.839418 | 2.475032 |
| 3 | 3.783668 | 4.265475 | 3.415489 | 3.857485 |
| 4 | 3.130653 | 4.519993 | 2.208596 | 2.868824 |
| 5 | 2.843559 | 4.133313 | 2.918711 | 5.1189 |

5

« 1 2 3 4 5 6 7 ... 11 »

5 10 20 30 40 50

◀ ▶

Download

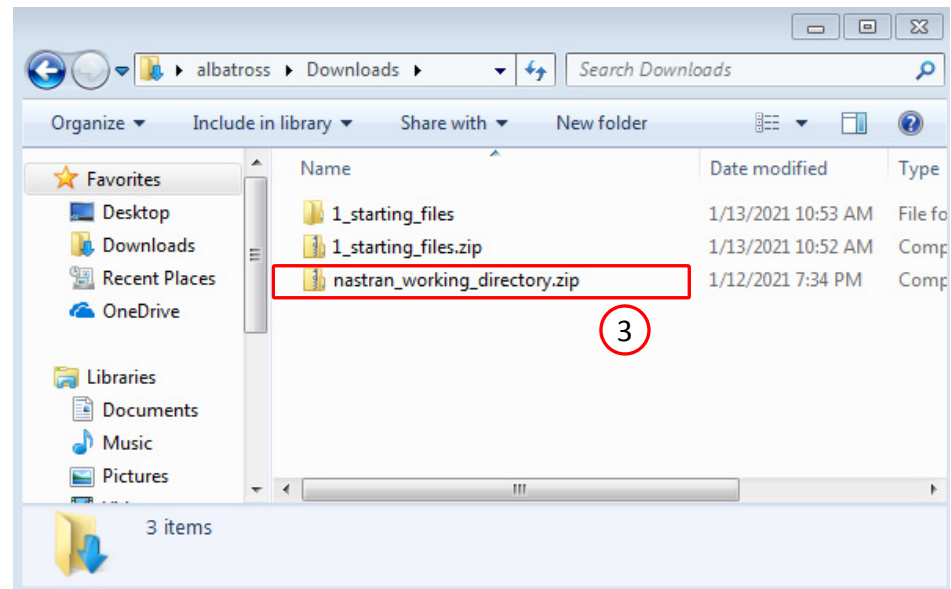
1. Click Download
2. Click Download BDF Files
3. A new ZIP file has been downloaded

1

Download

Download BDF Files

2



Parameters

1. Click Parameters
2. Deselect the following fields to delete parameters: x3, x4, x5, x6, x7, x9, x10
3. The following 4 parameters should remain: x1, x2, x8, x11

- In a later part of this tutorial, it is described how automatic relevance determination (ARD) is used to reduce the problem from 11 to those 4 parameters.

1

Select Parameters

| \$ _1 _ _2 _ _3 _ _4 _ _5 _ _6 _ _7 _ _8 _ _9 _ _10 _ | | | | | | | | | | |
|--|---------|----------|------------------|--------|----------|----------|------|-----|--|--|
| EIGRL | 1 | | 225. | | | | | | | |
| EIGRL | 2 | | 300. | | | | | | | |
| FORCE | 212 | 1001 | | 500. | 0.0 | 1.0 | 0.0 | | | |
| FORCE | 213 | 1001 | | 1000. | 0.0 | 0.0 | 1.0 | | | |
| FORCE | 232 | 1003 | | 500. | 0.0 | 1.0 | 0.0 | | | |
| FORCE | 233 | 1003 | | 1000. | 0.0 | 0.0 | 1.0 | | | |
| FREQ1 | 5 | 10. | 2.5 | 56 | | | | | | |
| MAT1 | 7 | 210000.0 | | 0.3 | 7.90E-06 | | | | | |
| MAT1 | 8 | 62000.0 | | 0.24 | 2.30E-06 | | | | | |
| MAT10 | 6 | | 1.23E-12340000.0 | | | | | | | |
| PARAM | G | 0.06 | | | | | | | | |
| PARAM | GFL | 0.12 | | | | | | | | |
| PARAM | LFREQ | 0.1 | | | | | | | | |
| PARAM | PREFDB | 2.E-11 | | | | | | | | |
| PARAM | WITMASS | .001 | | | | | | | | |
| PSHELL | 1 | 7 | %x1% | 7 | 1.0 | 0.833333 | | | | |
| PSHELL | 2 | 7 | %x2% | 7 | 1.0 | 0.833333 | | | | |
| PSHELL | 3 | 7 | 1.905 | 7 | 1.0 | 0.833333 | | | | |
| PSHELL | 4 | 7 | 1.27 | 7 | 1.0 | 0.833333 | | | | |
| PSHELL | 5 | 7 | 6.35 | 7 | 1.0 | 0.833333 | | | | |
| PSHELL | 6 | 7 | 3.81 | 7 | 1.0 | 0.833333 | | | | |
| PSHELL | 7 | 7 | 2.54 | 7 | 1.0 | 0.833333 | | | | |
| PSHELL | 8 | 7 | %x8% | 7 | 7 | | | | | |
| PSHELL | 9 | 7 | 3.0 | 7 | 7 | | | | | |
| PSHELL | 10 | 7 | 5.0 | 7 | 7 | | | | | |
| PSHELL | 11 | 8 | %x11% | 8 | 8 | | | | | |
| RBE3 | 1501 | | 1001 | 123456 | 1.0 | 123 | 7047 | 263 | | |

2



Configure Parameters

| Delete | Parameter | Status | Low | High | Comments |
|-------------------------------------|-----------|-------------------------------------|-----|------|------------------|
| <input checked="" type="checkbox"/> | x1 | <input checked="" type="checkbox"/> | 1. | 6. | Field 4 of PSHEL |
| <input checked="" type="checkbox"/> | x2 | <input checked="" type="checkbox"/> | 1. | 6. | Field 4 of PSHEL |
| <input checked="" type="checkbox"/> | x8 | <input checked="" type="checkbox"/> | 1. | 6. | Field 4 of PSHEL |
| <input checked="" type="checkbox"/> | x11 | <input checked="" type="checkbox"/> | 1. | 6. | Field 4 of PSHEL |

3

Samples

1. Click Samples
2. Set the Design as Latin Hypercube, Reproducible
3. Set the Number of Samples as 40
4. The table now has 40 samples

SOL 200 Web App - Machine Learning Parameters **Samples** Responses Download Results Connection Settings Home

1

Configure Samples

Design

Latin Hypercube, Reproducible 2

+ Info

Number of Samples

40 3

→

Samples to Run

+ Options

4

| Sample Number | x1 | x2 | x8 | x11 |
|---------------|----------|----------|----------|----------|
| 1 | 1. | 4.333333 | 3.051282 | 4.717949 |
| 2 | 1.128205 | 2.538462 | 3.435897 | 3.051282 |
| 3 | 1.25641 | 4.076923 | 5.102564 | 1.897436 |
| 4 | 1.384615 | 5.102564 | 2.794872 | 2.282051 |
| 5 | 1.512821 | 2.025641 | 3.692308 | 5.487179 |

5 10 20 30 40 50

« 1 2 3 4 5 6 7 8 »

Download

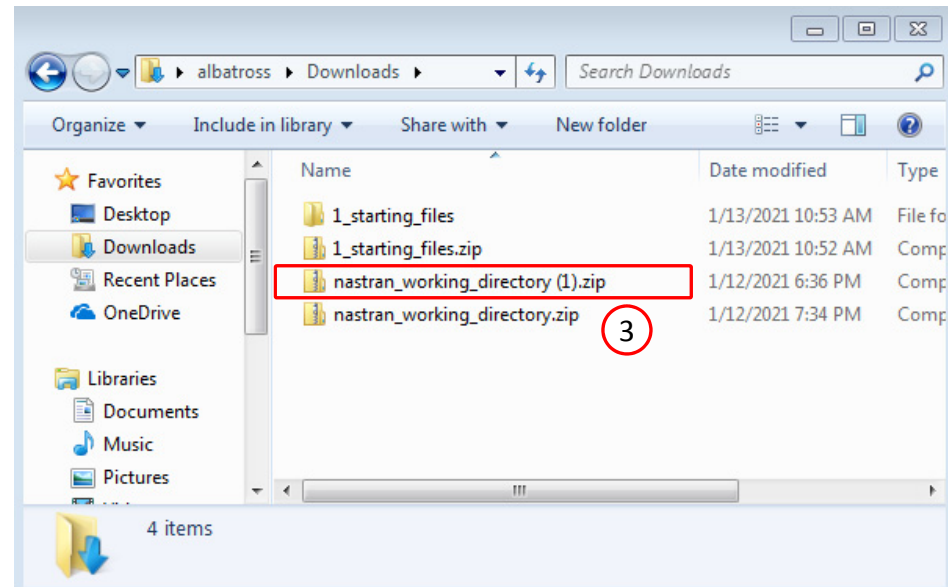
1. Click Download
2. Click Download BDF Files
3. A new ZIP file has been downloaded

1

Download

Download BDF Files

2



Samples

1. Click Samples
2. Set the Design as Latin Hypercube, Reproducible
3. Set the Number of Samples as 8
4. The table now has 8 samples
5. Click +Options
6. Click Export
7. A CSV file has been downloaded and contains the values from the table with 8 samples

1

Configure Samples

Design

Latin Hypercube, Reproducible 2

+ Info

Number of Samples

8 3



Samples to Run

+ Options 5

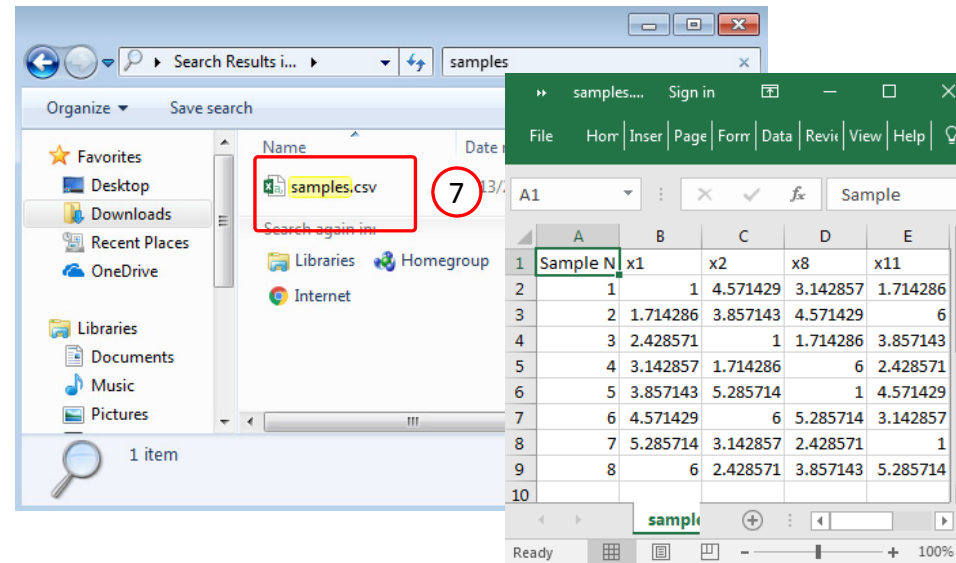
CSV
Export

Export 6

| 4 Parameters | | | | |
|---------------|----------|----------|----------|----------|
| Sample Number | x1 | x2 | x8 | x11 |
| 1 | 1. | 4.571429 | 3.142857 | 1.714286 |
| 2 | 1.714286 | 3.857143 | 4.571429 | 6. |
| 3 | 2.428571 | 1. | 1.714286 | 3.857143 |
| 4 | 3.142857 | 1.714286 | 6. | 2.428571 |
| 5 | 3.857143 | 5.285714 | 1. | 4.571429 |

« 1 2 »

5 10 20 30 40 50



Download

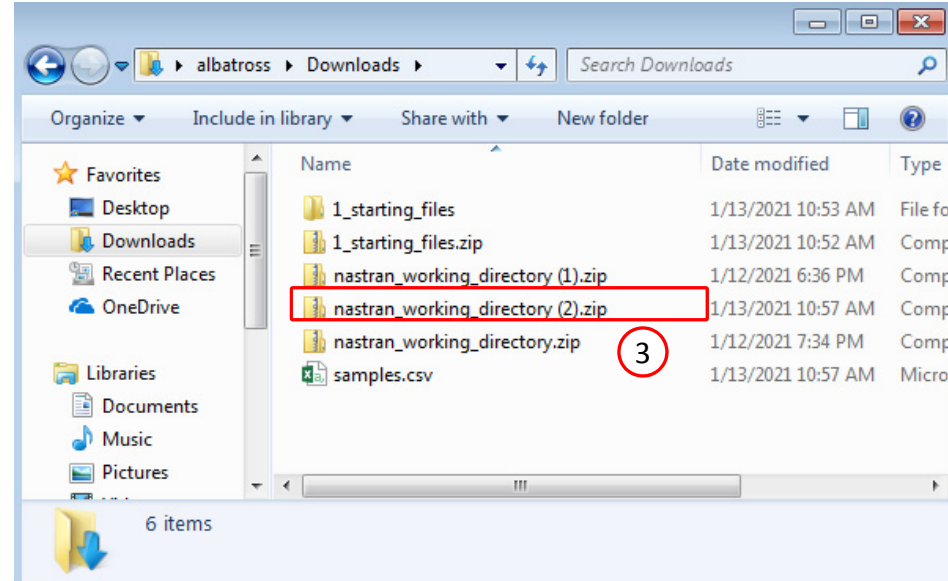
1. Click Download
2. Click Download BDF Files
3. A new ZIP file has been downloaded

1

Download

Download BDF Files

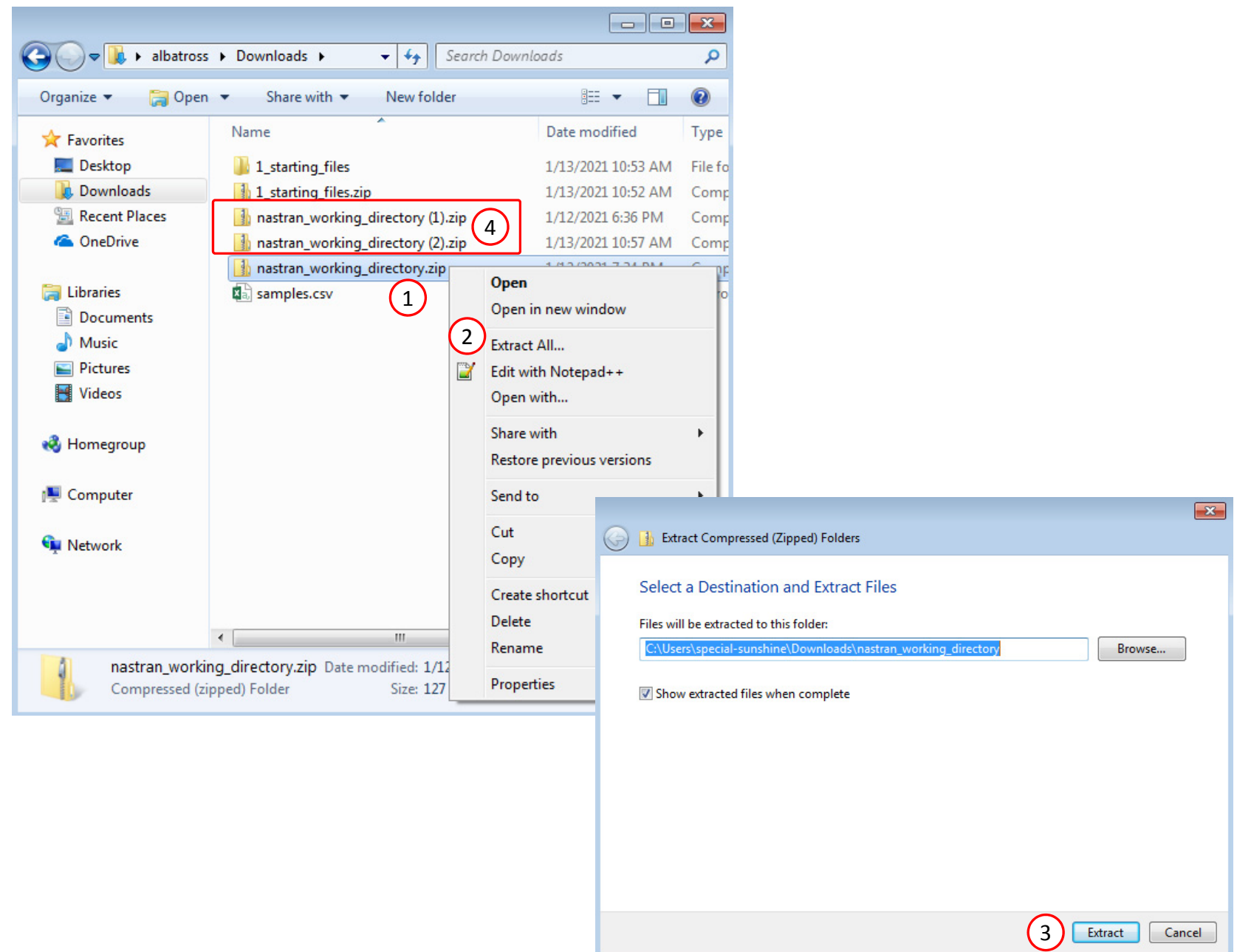
2



Start Desktop App

1. Right click on the indicated file
2. Click Extract All
3. Click Extract on the following window
4. Repeat steps 1-3 for the indicated files

- Always extract the contents of the ZIP file to a new, empty folder.



Start Desktop App

1. Open this folder:
nastran_working_directory
2. Inside of the new folder, double click on
Start Desktop App
3. Click Open, Run or Allow Access on any
subsequent windows
4. MSC Nastran will now start

- One can run the Nastran job on a remote machine as follows:
1) Copy the BDF files and the INCLUDE files to a remote machine. 2) Run the MSC Nastran job on the remote machine. 3) After completion, copy the BDF, F06, LOG, H5 files to the local machine. 4) Click "Start Desktop App" to display the results.

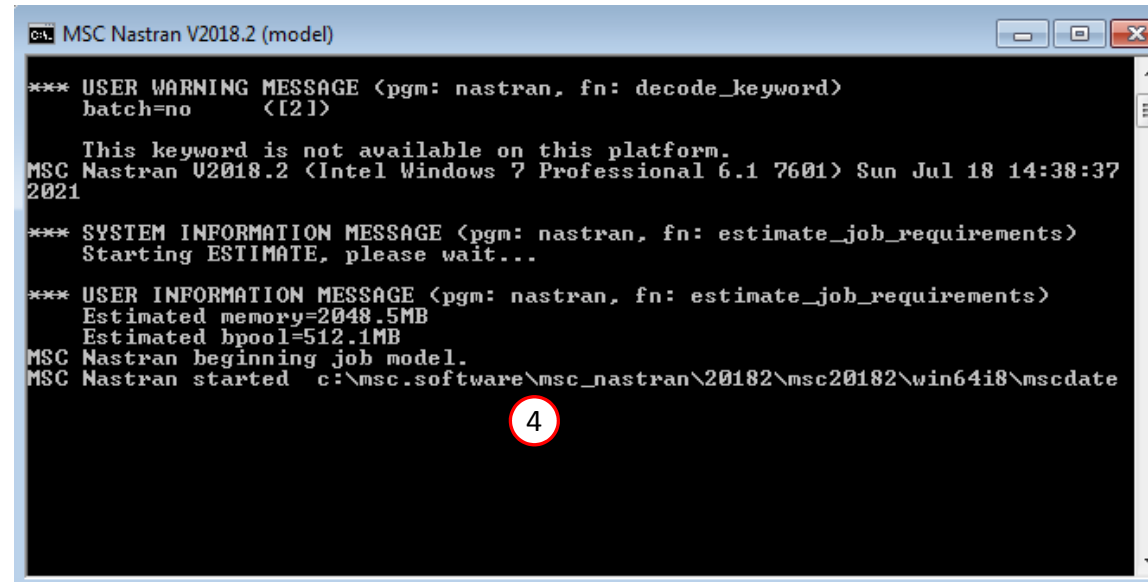
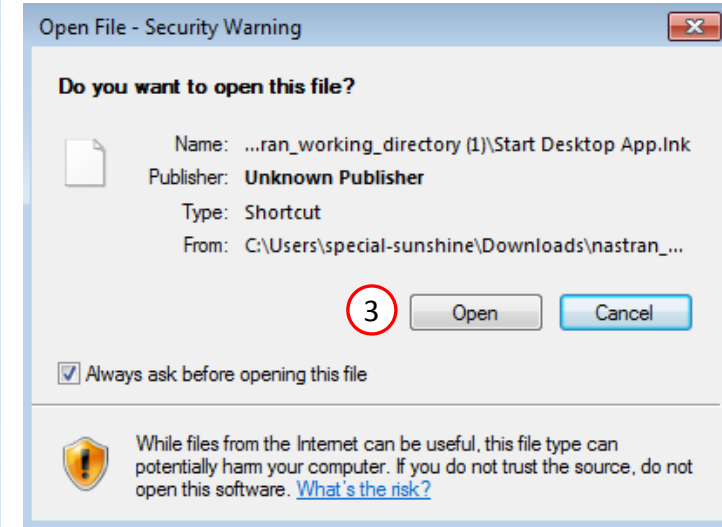
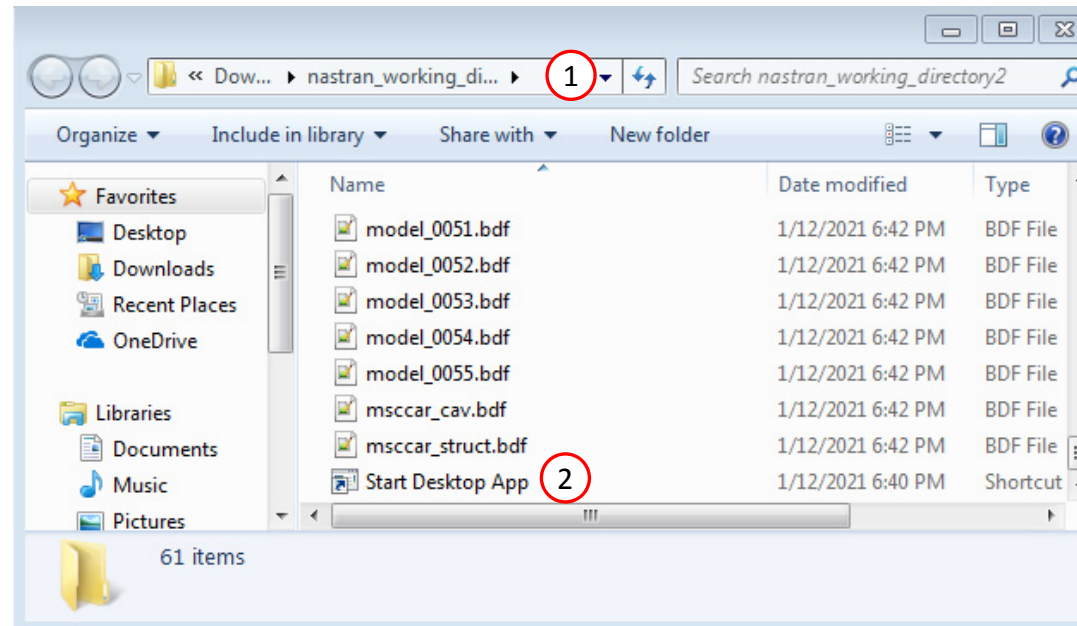
Using Linux?

Follow these instructions:

- 1) Open Terminal
- 2) Navigate to the nastran_working_directory
`cd ./nastran_working_directory`
- 3) Use this command to start the process
`./Start_MSC_Nastran.sh`

In some instances, execute permission must be granted to the directory. Use this command. This command assumes you are one folder level up.

```
sudo chmod -R u+x ./nastran_working_directory
```



Status

- While MSC Nastran is running, a status page will show the current state of MSC Nastran

SOL 200 Web App - Status

 Python

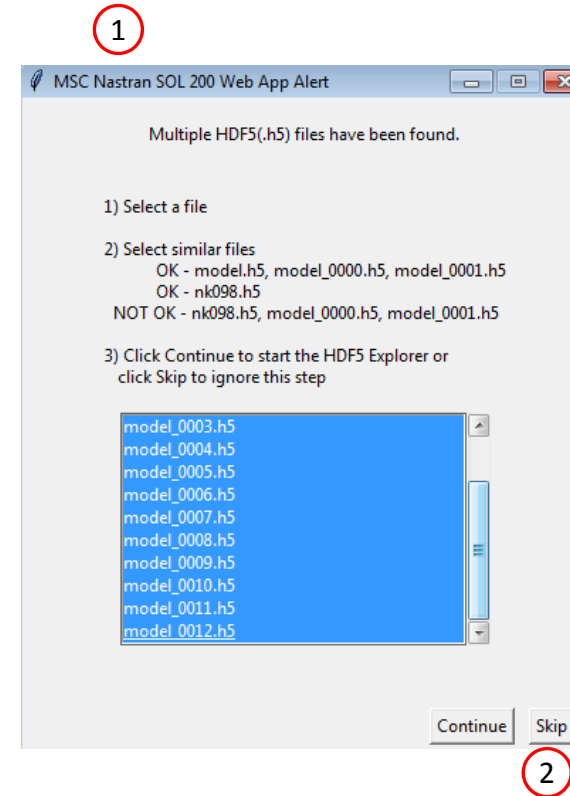
 MSC Nastran

Status

| Name | Status of Job | Design Cycle | RUN TERMINATED DUE TO |
|-----------|---------------|--------------|-----------------------|
| model.bdf | Running | None | |

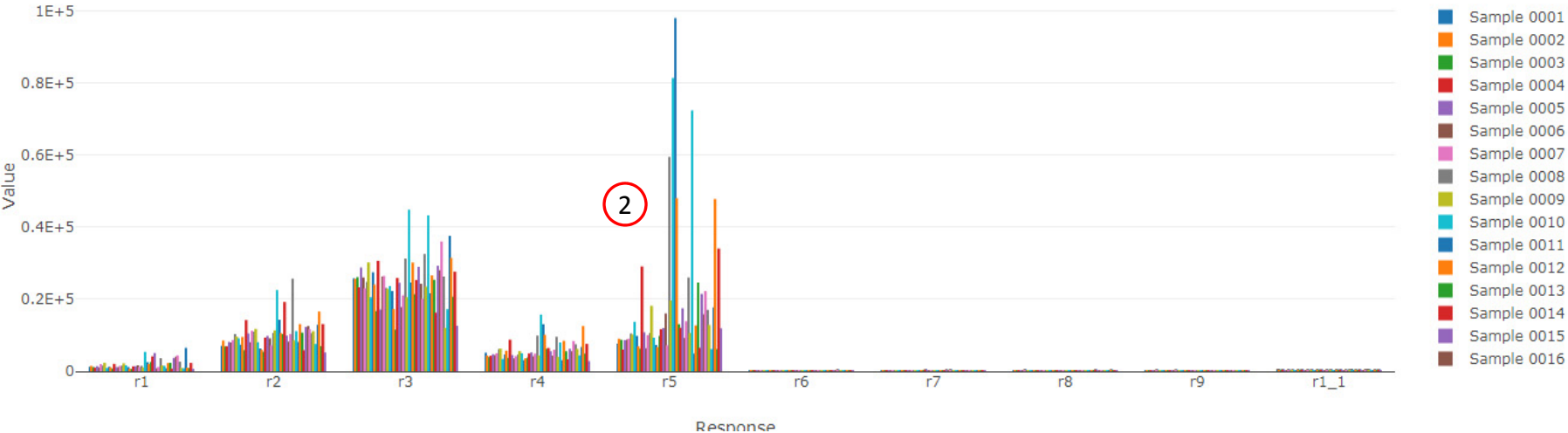
Review Results

1. A window appears asking to start the HDF5 Explorer
2. Click Skip to not open the HDF5 Explorer



Review Results

- 1. The Monitored Responses web app is opened
- 2. The value of each response and for each sample is displayed in a bar chart
- 3. A table lists the values for each response and sample.



Monitored Responses

A

Display MAX and MIN Download CSV Reset Filters

B

| Label | Dataset Name | Field | Field Description |
|------------------------------------|---|-----------------|---|
| r1 r1_1 r1_2 r1_3 r1_4 | ACOUSTIC/PRESSURE_CPLX NODAL/ACCELERATION_CPLX | DBM YM ZM | Sound pressure level in dB - magnit Y magnitude component ** Z magnitude component ** |
| r1 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |
| r2 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |
| r3 | NODAL/ACCELERATION_CPLX | ZM | Z magnitude component ** |
| r4 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |
| r5 | NODAL/ACCELERATION_CPLX | ZM | Z magnitude component ** |

Monitored Responses from Each Sample

3

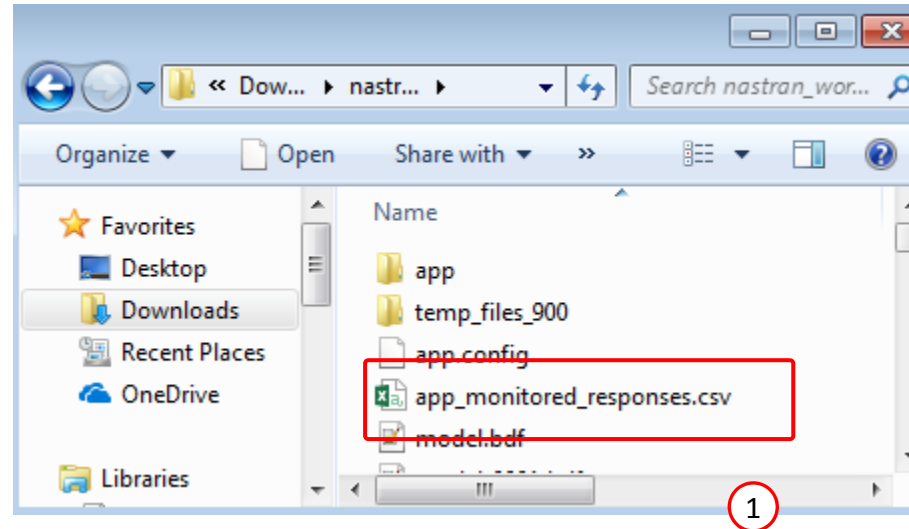
| 0001 | 0002 | 0003 | 0004 | |
|--------------------|--------------------|--------------------|--------------------|----|
| 1217.2174281739094 | 1505.0063820207042 | 1138.4266356161363 | 1014.9415601970021 | 13 |
| 7053.423907396364 | 8540.089784757196 | 6955.113624520879 | 6958.81401718346 | 81 |
| 25842.419807507038 | 25683.634954437166 | 26141.29227999461 | 23340.53010843421 | 28 |
| 5181.517140493611 | 4366.0019120235875 | 3893.0039254598646 | 4311.814597794899 | 47 |
| 7655.088567255526 | 9054.831254535718 | 8777.484906180196 | 6015.679440337792 | 86 |

- A. The table titled Monitored Response can be interacted with. Each column in the table contains filters. Once a filter is modified, the Bar Chart will instantly update.
- B. Additional functions include the ability to highlight the MAX and MIN bars, download a CSV file and reset the filters.

Review Results

1. The monitored responses are contained in the CSV file named `app_monitored_responses.csv`

The responses in this CSV file will be used to train the surrogate model.

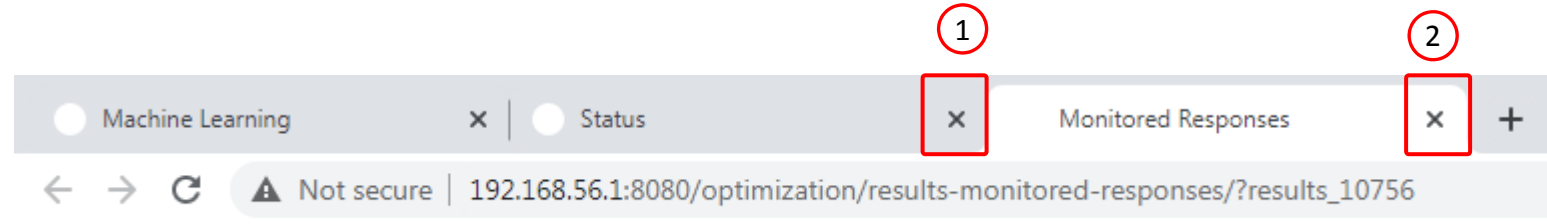


A screenshot of an Excel spreadsheet titled 'app_monitored_responses.csv - Excel'. The spreadsheet shows a table with columns A through J. Row 1 is the header row with labels 'Sample', 'r1', 'r2', 'r3', 'r4', 'r5', 'r6', 'r7', 'r8', 'r9'. Rows 2 through 6 contain numerical data. The spreadsheet is highlighted with a red border.

| | A | B | C | D | E | F | G | H | I | J |
|---|--------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 1 | Sample | r1 | r2 | r3 | r4 | r5 | r6 | r7 | r8 | r9 |
| 2 | 1 | 1217.217 | 7053.424 | 25842.42 | 5181.517 | 7655.089 | 7.54E-06 | 2.38E-05 | 3.73E-06 | 1.53E-05 |
| 3 | 2 | 1505.006 | 8540.09 | 25683.63 | 4366.002 | 9054.831 | 1.05E-05 | 2.47E-05 | 7.78E-06 | 1.97E-05 |
| 4 | 3 | 1138.427 | 6955.114 | 26141.29 | 3893.004 | 8777.485 | 9.88E-06 | 2.60E-05 | 4.92E-06 | 2.19E-05 |
| 5 | 4 | 1014.942 | 6958.814 | 23340.53 | 4311.815 | 6015.679 | 5.89E-06 | 1.29E-05 | 5.46E-06 | 1.10E-05 |
| 6 | 5 | 1379.038 | 8133.175 | 28819.79 | 4774.837 | 8635.851 | 9.60E-06 | 2.08E-05 | 5.52E-06 | 1.57E-05 |

Close Pages

1. The Status page can be closed
2. The Monitored Responses page can be closed



Start Desktop App

1. Open this folder:
nastran_working_directory (1)
2. Inside of the new folder, double click on
Start Desktop App
3. Click Open, Run or Allow Access on any
subsequent windows
4. MSC Nastran will now start

- One can run the Nastran job on a remote machine as follows:
1) Copy the BDF files and the INCLUDE files to a remote machine. 2) Run the MSC Nastran job on the remote machine. 3) After completion, copy the BDF, F06, LOG, H5 files to the local machine. 4) Click "Start Desktop App" to display the results.

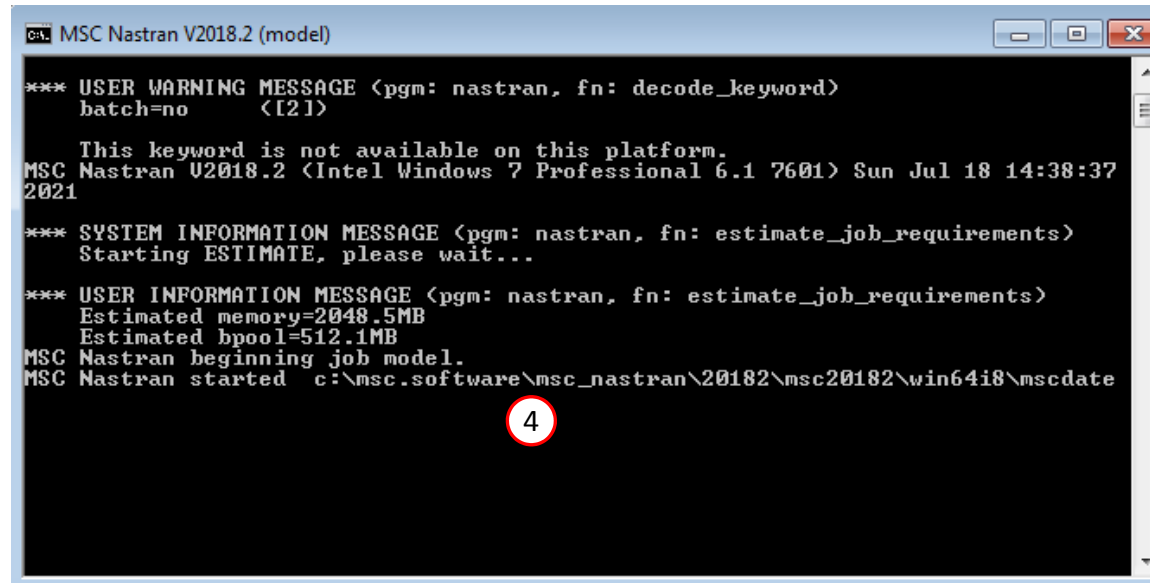
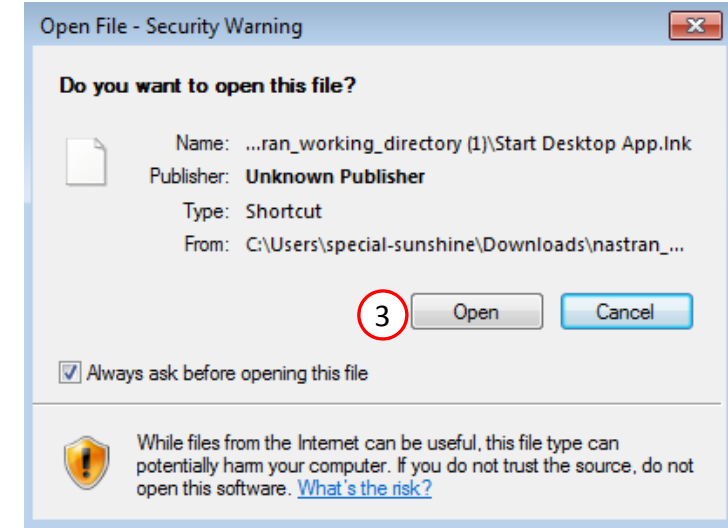
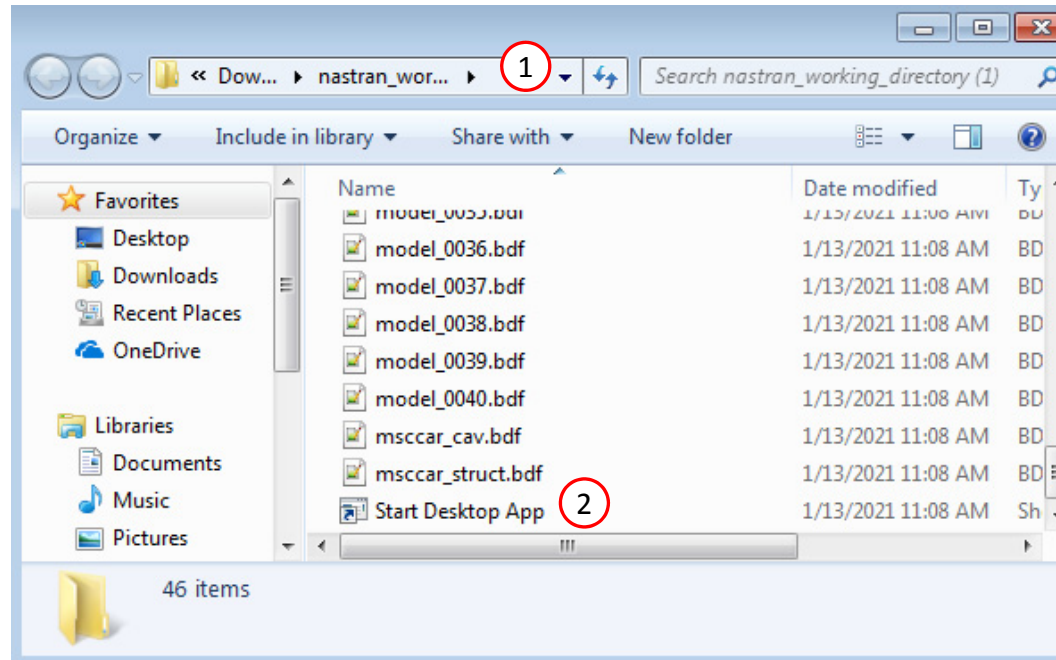
Using Linux?

Follow these instructions:

- 1) Open Terminal
- 2) Navigate to the nastran_working_directory
`cd ./nastran_working_directory`
- 3) Use this command to start the process
`./Start_MSC_Nastran.sh`

In some instances, execute permission must be granted to the directory. Use this command. This command assumes you are one folder level up.

```
sudo chmod -R u+x ./nastran_working_directory
```



Status

- While MSC Nastran is running, a status page will show the current state of MSC Nastran

SOL 200 Web App - Status

 Python

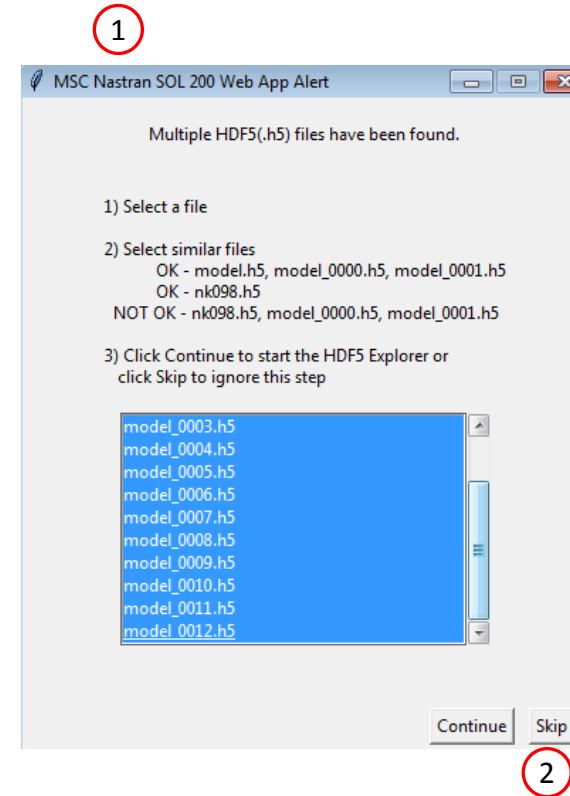
 MSC Nastran

Status

| Name | Status of Job | Design Cycle | RUN TERMINATED DUE TO |
|-----------|---------------|--------------|-----------------------|
| model.bdf | Running | None | |

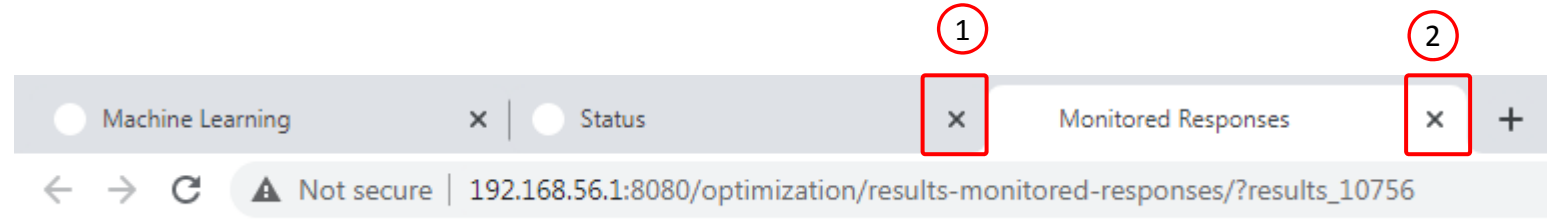
Review Results

1. A window appears asking to start the HDF5 Explorer
2. Click Skip to not open the HDF5 Explorer



Close Pages

1. The Status page can be closed
2. The Monitored Responses page can be closed



Start Desktop App

1. Open this folder:
nastran_working_directory (2)
2. Inside of the new folder, double click on
Start Desktop App
3. Click Open, Run or Allow Access on any
subsequent windows
4. MSC Nastran will now start

- One can run the Nastran job on a remote machine as follows:
1) Copy the BDF files and the INCLUDE files to a remote machine. 2) Run the MSC Nastran job on the remote machine. 3) After completion, copy the BDF, F06, LOG, H5 files to the local machine. 4) Click "Start Desktop App" to display the results.

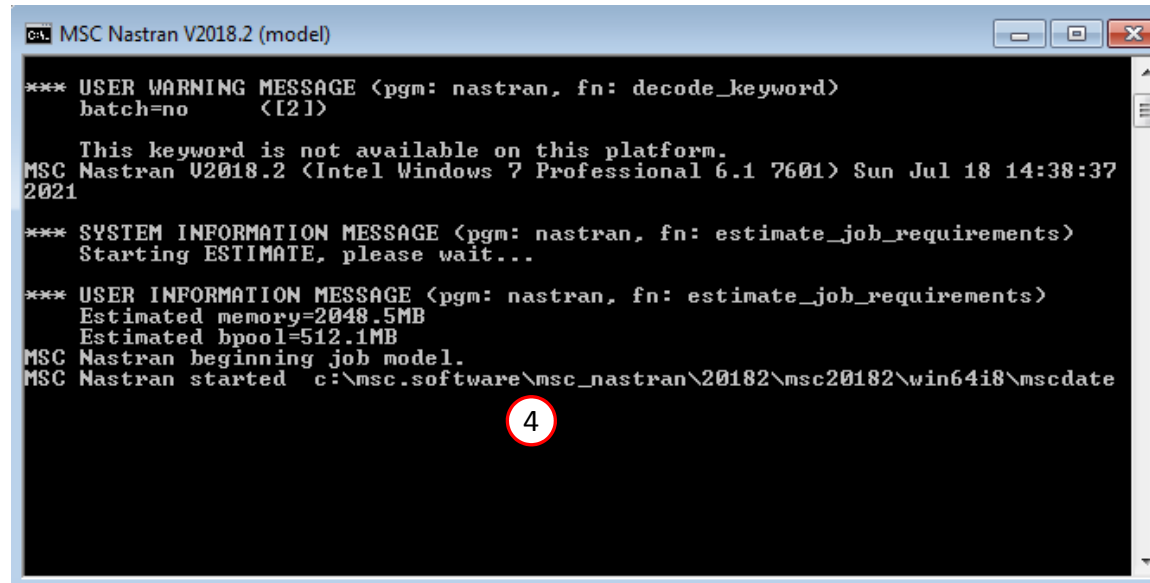
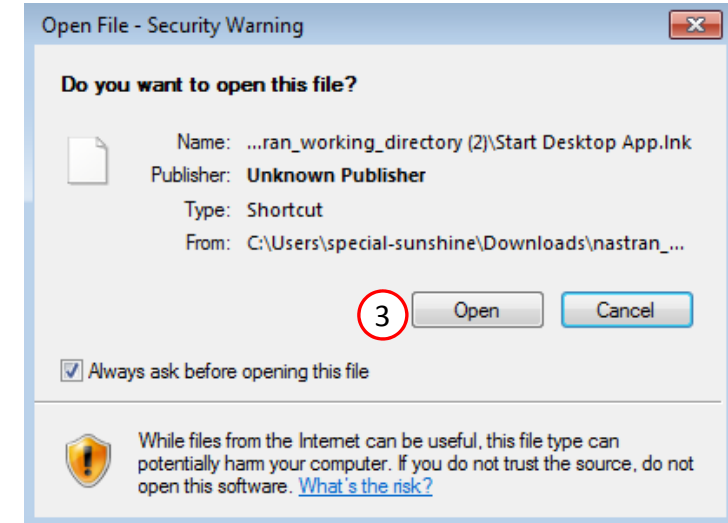
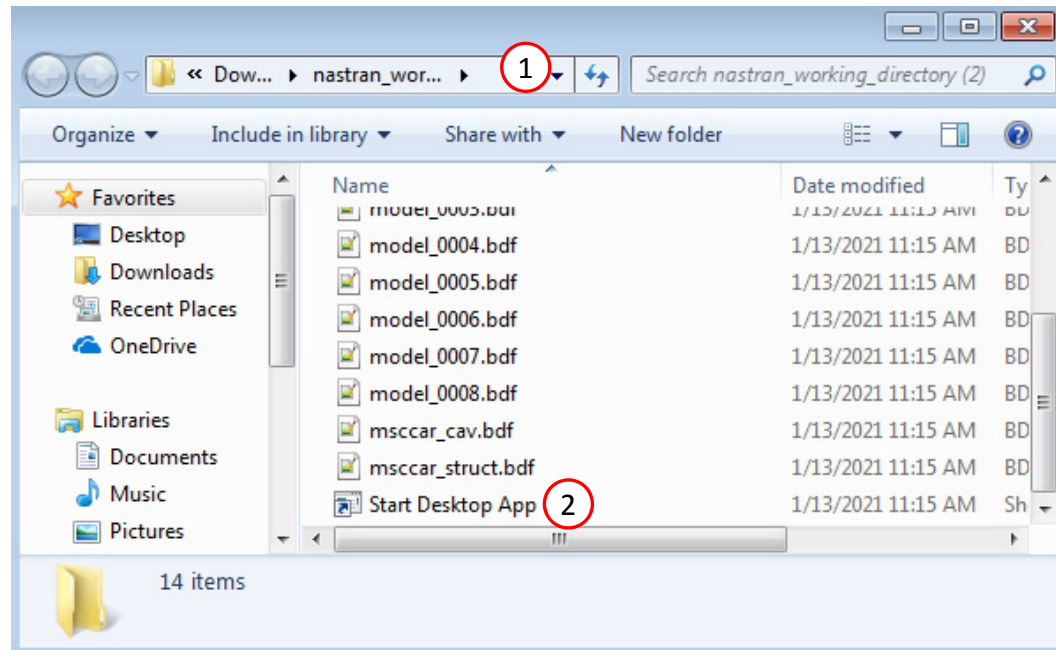
Using Linux?

Follow these instructions:

- 1) Open Terminal
- 2) Navigate to the nastran_working_directory
`cd ./nastran_working_directory`
- 3) Use this command to start the process
`./Start_MSC_Nastran.sh`

In some instances, execute permission must be granted to the directory. Use this command. This command assumes you are one folder level up.

```
sudo chmod -R u+x ./nastran_working_directory
```



Status

- While MSC Nastran is running, a status page will show the current state of MSC Nastran

SOL 200 Web App - Status

 Python

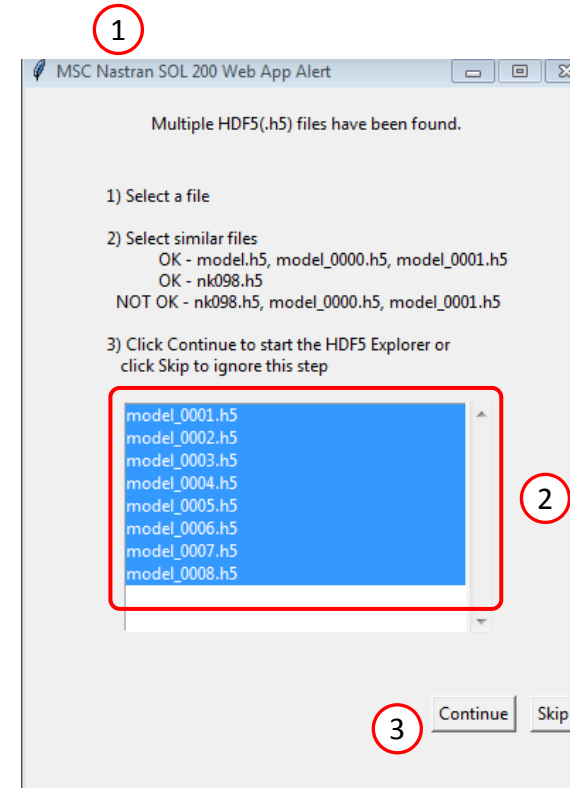
 MSC Nastran

Status

| Name | Status of Job | Design Cycle | RUN TERMINATED DUE TO |
|-----------|---------------|--------------|-----------------------|
| model.bdf | Running | None | |

Review Results

1. A window appears asking to start the HDF5 Explorer
2. Select all 8 H5 files
3. Click Continue



HDF5 Explorer

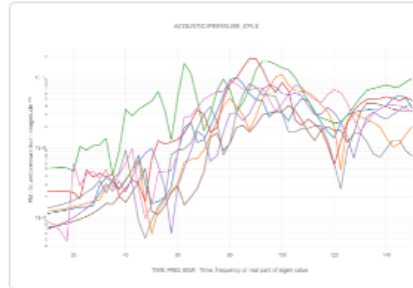
1. Navigate to the Plots Browser section
2. Click the indicated icon

1

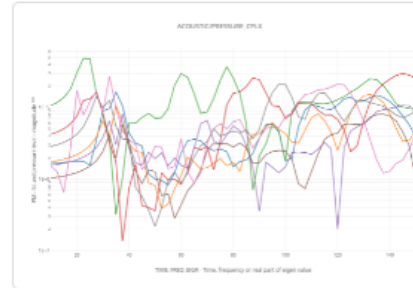
Plots Browser

ACOUSTIC/PRESSURE_CPLX

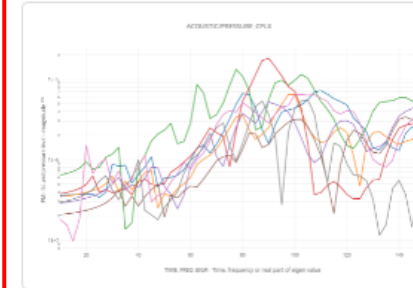
Download CSV



Plot #: 1 - ID: 8667 | SAMPLE:
model_0001, model_0002,
model_0003, ... | SUBCASE: 12 | PM
vs. TIME_FREQ_EIGR



Plot #: 2 - ID: 8667 | SAMPLE:
model_0001, model_0002,
model_0003, ... | SUBCASE: 13 | PM
vs. TIME_FREQ_EIGR



Plot #: 3 - ID: 8667 | SAMPLE:
model_0001, model_0002,
model_0003, ... | SUBCASE: 32 | PM
vs. TIME_FREQ_EIGR



Plot #: 4 - ID: 8667 | SAMPLE:
model_0001, model_0002,
model_0003, ... | SUBCASE: 33 | PM
vs. TIME_FREQ_EIGR

2

HDF5 Explorer

1. Click Display None to hide all the plotted traces
2. Set the Vertical Axis Format to Linear
3. Select only the 2nd trace which corresponds to the pressure at grid 8867, subcase 32, sample 2
4. The corresponding trace is now plotted

This trace will be used to compare the MSC Nastran response and predicted responses

Plot - ACOUSTIC/PRESSURE_CPLX

- Plot #: 3 - ID: 8667 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 32 | PM vs. TIME_FREQ_EIGR



Vertical Axis



PM - Sound pressure lev

Horizontal Axis

TIME_FREQ_EIGR - Titr

+ Options

Plot Type

Scatter Plot

Vertical Axis Format

Linear

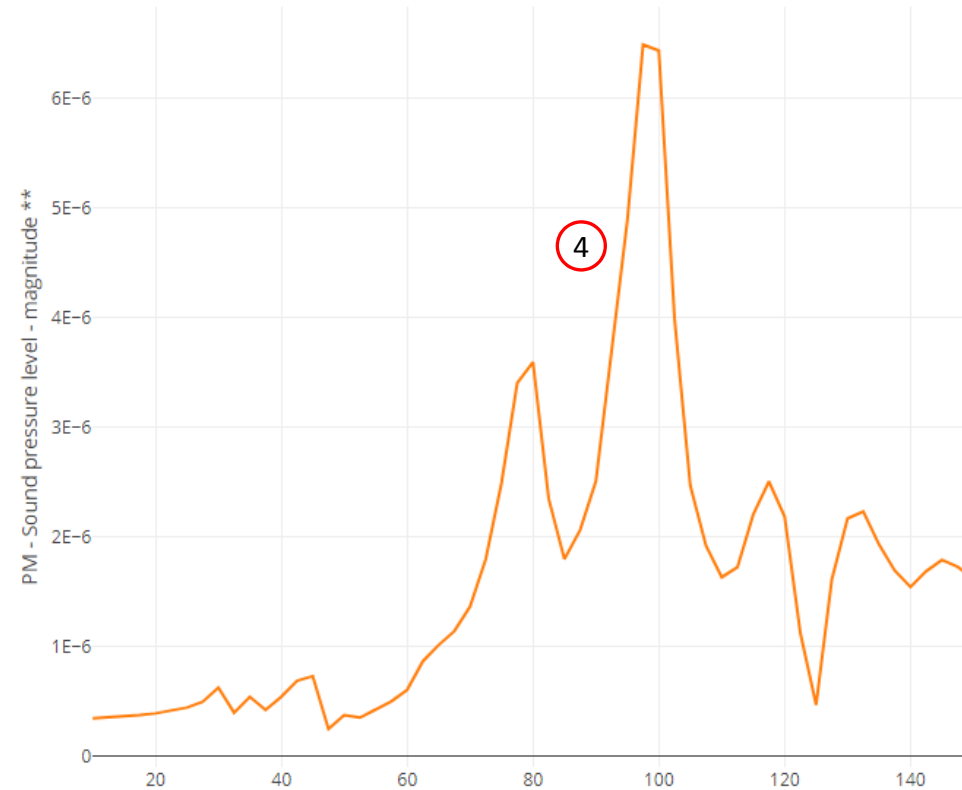
Separate By



SAMPLE

SUBCASE

ACOUSTIC/PRESSURE_CPLX



1

☐ Display None ☒ Display All

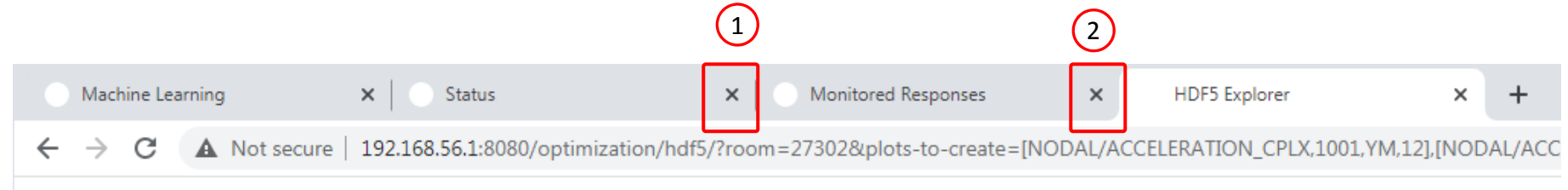
| Display | Color | Name |
|-------------------------------------|--------|---|
| <input type="checkbox"/> | Blue | 0 - ID: 8667 SAMPLE: model_0001 SUBCASE: 32 |
| <input checked="" type="checkbox"/> | Orange | 1 - ID: 8667 SAMPLE: model_0002 SUBCASE: 32 |
| <input type="checkbox"/> | Green | 2 - ID: 8667 SAMPLE: model_0003 SUBCASE: 32 |
| <input type="checkbox"/> | Red | 3 - ID: 8667 SAMPLE: model_0004 SUBCASE: 32 |
| <input type="checkbox"/> | Purple | 4 - ID: 8667 SAMPLE: model_0005 SUBCASE: 32 |
| <input type="checkbox"/> | Brown | 5 - ID: 8667 SAMPLE: model_0006 SUBCASE: 32 |
| <input type="checkbox"/> | Pink | 6 - ID: 8667 SAMPLE: model_0007 SUBCASE: 32 |
| <input type="checkbox"/> | Grey | 7 - ID: 8667 SAMPLE: model_0008 SUBCASE: 32 |

3

4

Close Pages

1. The Status page can be closed
2. The Monitored Responses page can be closed



Determining Parameter Relevance (Parameter/Variable Screening)

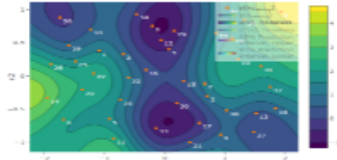
Prediction Analysis Web App

1. Return to the Machine Learning web app
2. Click Results
3. Click Prediction Analysis
4. The Prediction Analysis web app is now open
5. Ensure it says Connected

SOL 200 Web App - Machine LearningParametersSamplesResponsesDownloadResultsConnectionSettingsHome

12

Select a Results App




3

SOL 200 Web App - Prediction AnalysisHome

4

Gaussian Process (GP) App Connection Status

 Connected

5

Session ID: 8207

Output

GP App Update - Starting the Gaussian Process (GP) app on the server
- Session ID: 8207
- Address: http://localhost:8080/optimization
Desktop App Update - Connecting to the SOL 200 Web App...
GP App Update - Connection successful between the Node JS server and GP ap

Warnings and Errors

Warnings can be ignored

Training Data

1. Navigate to the Training and Testing Data section
2. Delete any previous table data by clicking the four (4) buttons named Delete all rows

- **x_training, y_training** - This specifies the x inputs and y outputs used to train the surrogate model.
- **x_testing, y_testing** - This specifies the x inputs and y outputs used to calculate the Normalized Root Mean Square Error (NRMSE) between the predicted values and actual MSC Nastran responses. This testing data is optional.
- **x_prediction** – The x inputs at which to make predictions.

Training and Testing Data 1

x_training

CSV Export



CSV Import



Select a CSV File



CSV

imported

2

✕ Delete all rows

y_training

CSV Export



CSV Import



Select a CSV File



✕ Delete all rows

sample

y1

x_testing

CSV Export



CSV Import



Select a CSV File



✕ Delete all rows

sample

x1

x2

y_testing

CSV Export



CSV Import



Select a CSV File



✕ Delete all rows

sample

y1


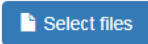
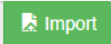

Training Data

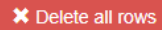
1. Navigate to the section titled x_training
2. Click Select files
3. Navigate to the folder named nastran_working_directory which contains data for 55 runs
4. Select the file app.config
5. Click Open
6. Click Import
7. The table is now loaded with the x inputs for all 55 runs

Training and Testing Data

x_training ¹

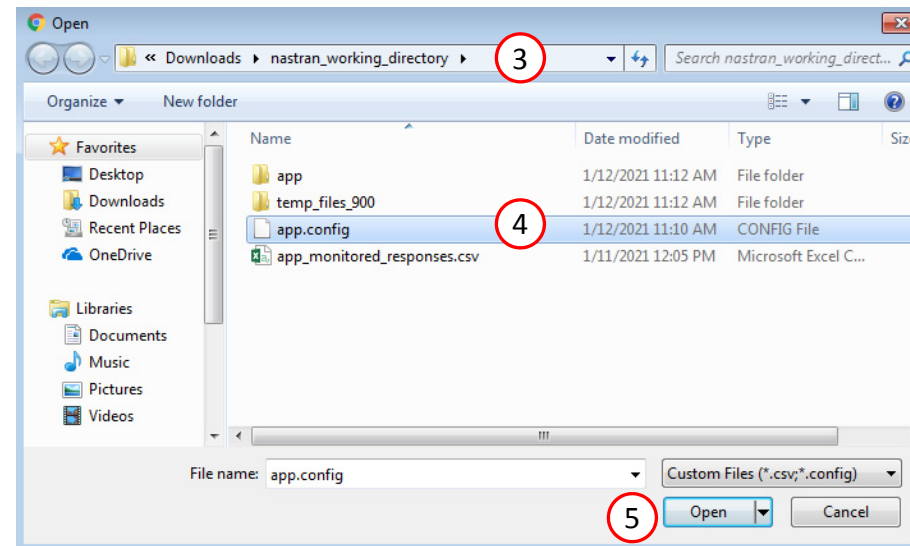
CSV Export CSV Import ⁶

²   app.config  

⁷ 

| sample | x1 | x2 | x8 | x11 |
|--------|----------|----------|----------|----------|
| 1 | 1. | 4.333333 | 3.051282 | 4.717949 |
| 2 | 1.128205 | 2.538462 | 3.435897 | 3.051282 |
| 3 | 1.25641 | 4.076923 | 5.102564 | 1.897436 |
| 4 | 1.384615 | 5.102564 | 2.794872 | 2.282051 |
| 5 | 1.512821 | 2.025641 | 3.692308 | 5.487179 |
| 6 | 1.641026 | 2.923077 | 5.615385 | 4.205128 |
| 7 | 1.769231 | 2.153846 | 1.384615 | 4.333333 |
| 8 | 1.897436 | 1.512821 | 5.230769 | 1.769231 |
| 9 | 2.025641 | 3.435897 | 1.128205 | 2.025641 |
| 10 | 2.153846 | 5.358974 | 4.974359 | 3.692308 |

« 1 2 3 4 5 6 » 10 25 50 100



Training Data

1. Navigate to the section titled y_training
2. Click Select files
3. Navigate to the folder named nastran_working_directory which contains data for 55 runs
4. Select the file app_monitored_responses.csv
5. Click Open
6. Click Import
7. The table is now loaded with the y outputs (monitored responses) for all 55 runs

y_training 1

CSV Export CSV Import 6

2 Export Select files app_monitored_responses.csv Import CSV imported

7 Delete all rows

| sample | y1 | y2 | y3 | y4 | y5 |
|--------|------------------|------------------|------------------|------------------|-----------------|
| 0001 | 1217.2174281... | 7053.4239073... | 25842.419807... | 5181.5171404... | 7655.0885672... |
| 0002 | 1505.0063820... | 8540.0897847... | 25683.634954... | 4366.0019120... | 9054.8312545... |
| 0003 | 1138.42663561... | 6955.11362452... | 26141.292279... | 3893.0039254... | 8777.4849061... |
| 0004 | 1014.9415601... | 6958.8140171... | 23340.530108... | 4311.81459779... | 6015.6794403... |
| 0005 | 1379.03821311... | 8133.1753262... | 28819.790379... | 4774.8375075... | 8635.8513076... |
| 0006 | 1047.6175683... | 7973.2957981... | 26054.675419... | 4523.9543601... | 8849.2091520... |
| 0007 | 1981.5433834... | 8692.3242639... | 23054.2571136... | 4995.6044695... | 9071.9554061... |
| 0008 | 1598.2086637... | 10324.491827... | 24808.673325... | 6146.4902246... | 10474.352170... |
| 0009 | 2351.7355373... | 9636.5472108... | 30268.013988... | 6305.1596798... | 10217.706642... |
| 0010 | 923.115645225... | 9180.8271441... | 20546.846849... | 3444.3692147... | 13782.262157... |

« 1 2 3 4 5 6 » 10 25 50 100

Open

« Downloads » nastran_working_directory 3 Search nastran_working_direct...

Organize New folder

| Name | Date modified | Type | Size |
|-----------------------------|--------------------|----------------------|------|
| app | 1/12/2021 11:12 AM | File folder | |
| temp_files_900 | 1/12/2021 11:12 AM | File folder | |
| app.config | 1/12/2021 11:10 AM | CONFIG File | |
| app_monitored_responses.csv | 1/11/2021 12:05 PM | Microsoft Excel C... | |

File name: app_monitored_responses.csv 5 Custom Files (*.csv;*.config) Open Cancel

Perform Regression

1. Click Perform Regression and the surrogate model will be fitted
2. The regression is complete when the following status message is visible:
 - Process complete
3. The output will be used on the next page

SOL 200 Web App - Prediction Analysis

[Home](#)

Regression

| Data | Link to Table | Status | Status Description |
|----------------------|----------------------|--------|--------------------|
| x_training | Link | ✓ | Ready |
| y_training | Link | ✓ | Ready |
| x_testing (Optional) | Link | ⓘ | Ready |
| y_testing (Optional) | Link | ⓘ | Ready |

[Perform Regression](#)[Process complete](#)[Click here to view the Regression Results section](#)

3

Output

```
GP App Update - Saving initial data
GP App Update - Summary of Automatic Relevance Determination (ARD)
ARD measures predictive relevance of parameters and is used for parameter selection
- High Value: The parameter xi is relevant
- Low Value: The parameter xi is irrelevant and could potentially be set to zero

Kernel: MaternS2
| Response | x1 | x2 | x3 | x4 | x5 |
|:-----:|:---:|:---:|:---:|:---:|:---:|
| y1 | 4.41523 | 11.181 | 0.659106 | 2.17256e-09 | 3.3067e-09 | 1.8521e-09 |
| y2 | 2.6569 | 3.0316 | 3.96957 | 1.37152e-07 | 1.21214 | 0.0482e-07 |
| y3 | 1.43826 | 5.22752 | 9.84035e-07 | 1.20974e-06 | 0.433083 | 1.4890e-06 |
| y4 | 0.0857389 | 22.2011 | 2.80218 | 0.0084688 | 1.54202e-09 | 0.0129e-09 |
| y5 | 0.00394936 | 73.9887 | 0.0320619 | 0.119963 | 0.248584 | 4.7087e-05 |
| y6 | 0.532546 | 8.6371 | 0.777735 | 5.41834e-05 | 2.99273 | 0.0472e-05 |
| y7 | 0.383766 | 31.5844 | 3.9199e-09 | 0.616215 | 5.33463e-09 | 0.0254e-09 |
| y8 | 0.0615319 | 49.5679 | 2.03028e-08 | 1.21104 | 2.07824e-08 | 2.2841e-08 |
| y9 | 0.31014 | 7.12581 | 1.19458 | 4.37308e-08 | 0.289277 | 0.0793e-08 |
Parameters listed in decreasing order of relevance: x2, x8, x1, x11, x3, x5, x9, x4.

Kernel: Exponential
| Response | x1 | x2 | x3 | x4 | x5 |
|:-----:|:---:|:---:|:---:|:---:|:---:|
| y1 | 0.633904 | 3.97626 | 8.68101e-10 | 5.9275e-10 | 9.24688e-10 | 6.455e-10 |
| y2 | 0.119435 | 0.338008 | 0.102887 | 4.80711e-10 | 4.06709e-10 | 0.049e-10 |
| y3 | 0.0342023 | 0.391405 | 2.72361e-09 | 6.14333e-09 | 0.0271812 | 8.122e-09 |
| y4 | 0.00116244 | 0.155004 | 0.0221579 | 5.60043e-11 | 4.89368e-11 | 1.120e-11 |
| y5 | 3.82391e-11 | 0.41135 | 2.14606e-11 | 2.50395e-11 | 1.47319e-11 | 3.482e-11 |
| y6 | 9.32315e-06 | 1.35509 | 0.0606396 | 1.84373e-06 | 0.230813 | 3.064e-06 |
| y7 | 0.0097128 | 1.41159 | 4.10616e-10 | 3.07655e-10 | 1.83933e-10 | 3.214e-10 |
| y8 | 0.0515579 | 7.13954 | 5.35455e-08 | 3.83144e-07 | 6.88943e-08 | 4.176e-08 |
| y9 | 0.00201582 | 0.273497 | 2.67888e-10 | 2.10806e-10 | 0.0241915 | 2.522e-10 |
Parameters listed in decreasing order of relevance: x2, x1, x8, x11, x10, x3, x6, x4.

Kernel: RBF
```

Automatic Relevance Determination (ARD)

1. Click and hold the bottom right corner of the output window (gray color) and vertically drag to adjust the height of the window. This will make more text visible.
2. For the Output window, move the scroll bar to the very bottom
3. Ensure the following section is visible: Summary of Automatic Relevance Determination (ARD)
4. ARD values for each response with respect to each parameter have been computed

Output

GP App Update - Saving initial data

GP App Update - Summary of Automatic Relevance Determination (ARD) 3

ARD measures predictive relevance of parameters and is used for parameter selection

- High Value: The parameter x_i is relevant
- Low Value: The parameter x_i is irrelevant and could potentially be set to zero

Kernel: Matern52

| Response | x1 | x2 | x3 | x4 | x5 |
|----------|------------|---------|-------------|-------------|-------------|
| y1 | 4.41523 | 11.181 | 0.659106 | 2.17256e-09 | 3.3067e-09 |
| y2 | 2.6569 | 3.0316 | 3.96957 | 1.37152e-07 | 1.21214 |
| y3 | 1.43826 | 5.22752 | 9.84035e-07 | 1.20974e-06 | 0.433083 |
| y4 | 0.0857389 | 22.2011 | 2.80218 | 0.0084688 | 1.54202e-09 |
| y5 | 0.00394936 | 73.9887 | 0.0320619 | 0.119963 | 0.248584 |
| y6 | 0.532546 | 8.6371 | 0.777735 | 5.41834e-05 | 2.99273 |
| y7 | 0.383766 | 31.5844 | 3.9199e-09 | 0.616215 | 5.33463e-09 |
| y8 | 0.0615319 | 49.5679 | 2.03028e-08 | 1.21104 | 2.07824e-08 |
| y9 | 0.31014 | 7.12581 | 1.19458 | 4.37308e-08 | 0.289277 |

Parameters listed in decreasing order of relevance: x2, x8, x1, x11, x3, x5, x9, x4.

Kernel: Exponential

| Response | x1 | x2 | x3 | x4 | x5 |
|----------|-------------|----------|-------------|-------------|-------------|
| y1 | 0.633904 | 3.97626 | 8.68101e-10 | 5.9275e-10 | 9.24688e-10 |
| y2 | 0.119435 | 0.338008 | 0.102887 | 4.80711e-10 | 4.06709e-10 |
| y3 | 0.0342023 | 0.391405 | 2.72361e-09 | 6.14333e-09 | 0.0271812 |
| y4 | 0.00116244 | 0.155004 | 0.0221579 | 5.60043e-11 | 4.89368e-11 |
| y5 | 3.82391e-11 | 0.41135 | 2.14606e-11 | 2.50395e-11 | 1.47319e-11 |
| y6 | 9.32315e-06 | 1.35509 | 0.0606396 | 1.84373e-06 | 0.230813 |
| y7 | 0.0097128 | 1.41159 | 4.10616e-10 | 3.07655e-10 | 1.83933e-10 |
| y8 | 0.0515579 | 7.13954 | 5.35455e-08 | 3.83144e-07 | 6.88943e-08 |
| y9 | 0.00201582 | 0.273497 | 2.67888e-10 | 2.10806e-10 | 0.0241915 |

Parameters listed in decreasing order of relevance: x2, x1, x8, x11, x10, x3, x6, x11

Kernel: RBF

4 2 1

Automatic Relevance Determination (ARD)

1. A single line lists the most relevant parameters, in decreasing order, across all responses. Parameters x1, x2, x8 and x11 are the most relevant, and the other parameters can be optionally removed.
2. During the regression, 3 different kernel functions are used. As a result, there will be 3 sets of ARD values. As shown, the Exponential kernel function has produced a similar list of relevant parameters x1, x2, x8 and x11.
3. If desired, more relevant parameters can be determined, but it is expected some disagreement may occur as indicated. The parameter selection process is left to your judgement. For example, when you repeat this example, you may find these parameters as the most relevant: x1, x2 x3 and x8.

- For large dimension problems, i.e. problems with 10 or more parameters, the training data to fit the surrogate model may require 10-20 runs per parameter, possibly more. There is a need to reduce the dimensionality of the problem.
- As an example, suppose computation constraints limit us to 40 runs and the goal is to use 10 runs per parameter, the problem needs to be reduced to 4 parameters. This page demonstrates the parameter selection process.

Output

```
GP App Update - Saving initial data
GP App Update - Summary of Automatic Relevance Determination (ARD)
ARD measures predictive relevance of parameters and is used for parameter selection
- High Value: The parameter xi is relevant
- Low Value: The parameter xi is irrelevant and could potentially be removed

Kernel: Matern52
| Response | x1 | x2 | x3 | x4 | x5 |
|:-----:|:---:|:---:|:---:|:---:|:---:|
| y1 | 4.41523 | 11.181 | 0.659106 | 2.17256e-09 | 3.3067e-09 | 1.8521e-09 |
| y2 | 2.6569 | 3.0316 | 3.96957 | 1.37152e-07 | 1.21214 | 0.04821 |
| y3 | 1.43826 | 5.22752 | 9.84035e-07 | 1.20974e-06 | 0.433083 | 1.48908 |
| y4 | 0.0857389 | 22.2011 | 2.80218 | 0.0084688 | 1.54202e-09 | 0.01294 |
| y5 | 0.00394936 | 73.9887 | 0.0320619 | 0.119963 | 0.248584 | 4.70871 |
| y6 | 0.532546 | 8.6371 | 0.777735 | 5.41834e-05 | 2.99273 | 0.04721 |
| y7 | 0.383766 | 31.5844 | 3.9199e-09 | 0.616215 | 5.33463e-09 | 0.02544 |
| y8 | 0.0615319 | 49.5679 | 2.03028e-08 | 1.21104 | 2.07824e-08 | 2.28411 |
| y9 | 0.31014 | 7.12581 | 1.19458 | 4.37308e-08 | 0.289277 | 0.07938 |

Parameters listed in decreasing order of relevance: x2, x8, x1, x11, x3, x5, x9, x4

Kernel: Exponential
| Response | x1 | x2 | x3 | x4 | x5 |
|:-----:|:---:|:---:|:---:|:---:|:---:|
| y1 | 0.633904 | 3.97626 | 8.68101e-10 | 5.9275e-10 | 9.24688e-10 | 6.4551e-10 |
| y2 | 0.119435 | 0.338008 | 0.102887 | 4.80711e-10 | 4.06709e-10 | 0.0491e-10 |
| y3 | 0.0342023 | 0.391405 | 2.72361e-09 | 6.14333e-09 | 0.0271812 | 8.1221e-10 |
| y4 | 0.00116244 | 0.155004 | 0.0221579 | 5.60043e-11 | 4.89368e-11 | 1.1201e-11 |
| y5 | 3.82391e-11 | 0.41135 | 2.14606e-11 | 2.50395e-11 | 1.47319e-11 | 3.4811e-12 |
| y6 | 9.32315e-06 | 1.35509 | 0.0606396 | 1.84373e-06 | 0.230813 | 3.0641e-06 |
| y7 | 0.0097128 | 1.41159 | 4.10616e-10 | 3.07655e-10 | 1.83933e-10 | 3.2141e-10 |
| y8 | 0.0515579 | 7.13954 | 5.35455e-08 | 3.83144e-07 | 6.88943e-08 | 4.1761e-08 |
| y9 | 0.00201582 | 0.273497 | 2.67888e-10 | 2.10806e-10 | 0.0241915 | 2.5221e-10 |

Parameters listed in decreasing order of relevance: x2, x1, x8, x11, x10, x3, x6, x4

Kernel: RBF
| Response | x1 | x2 | x3 | x4 | x5 |
|:-----:|:---:|:---:|:---:|:---:|:---:|
| y1 | 0.633904 | 3.97626 | 8.68101e-10 | 5.9275e-10 | 9.24688e-10 | 6.4551e-10 |
| y2 | 0.119435 | 0.338008 | 0.102887 | 4.80711e-10 | 4.06709e-10 | 0.0491e-10 |
| y3 | 0.0342023 | 0.391405 | 2.72361e-09 | 6.14333e-09 | 0.0271812 | 8.1221e-10 |
| y4 | 0.00116244 | 0.155004 | 0.0221579 | 5.60043e-11 | 4.89368e-11 | 1.1201e-11 |
| y5 | 3.82391e-11 | 0.41135 | 2.14606e-11 | 2.50395e-11 | 1.47319e-11 | 3.4811e-12 |
| y6 | 9.32315e-06 | 1.35509 | 0.0606396 | 1.84373e-06 | 0.230813 | 3.0641e-06 |
| y7 | 0.0097128 | 1.41159 | 4.10616e-10 | 3.07655e-10 | 1.83933e-10 | 3.2141e-10 |
| y8 | 0.0515579 | 7.13954 | 5.35455e-08 | 3.83144e-07 | 6.88943e-08 | 4.1761e-08 |
| y9 | 0.00201582 | 0.273497 | 2.67888e-10 | 2.10806e-10 | 0.0241915 | 2.5221e-10 |

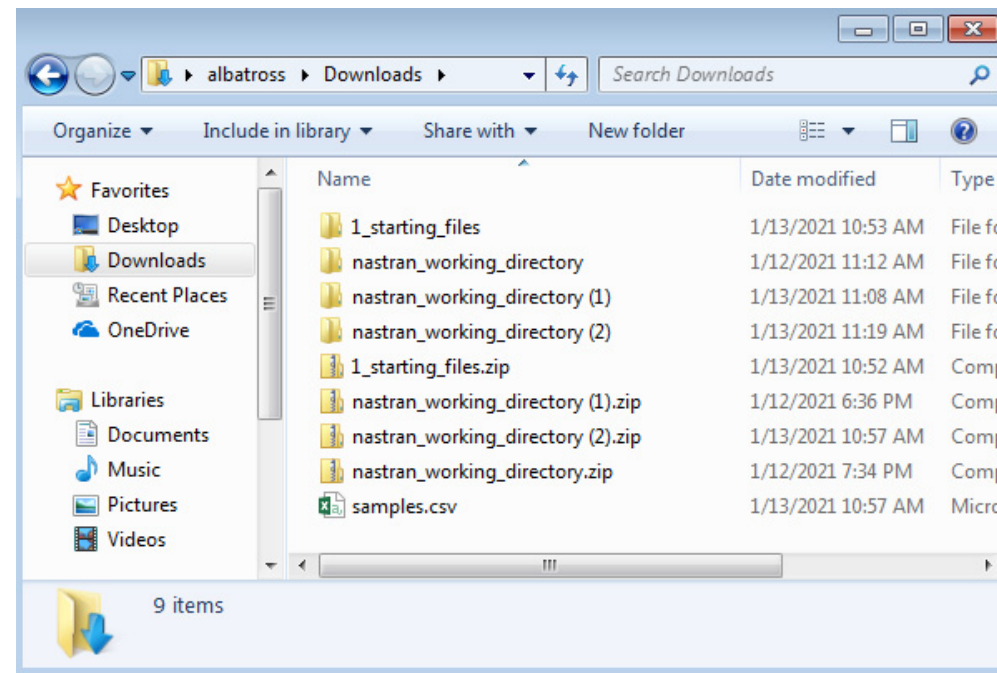
Parameters listed in decreasing order of relevance: x2, x1, x8, x11, x10, x3, x6, x4
```


Samples

It has been determined that 4 parameters x1, x2, x8 and x11 should be kept, and the other 7 parameters should be removed.

The next batch, Batch 2, has been configured previously for 4 parameters and 40 runs.

The following pages go over the regression process, making predictions and comparing the predictions to MSC Nastran outputs.



| Batch | File Name | Number of Runs | Number of Parameters | Purpose |
|-------|-----------------------------------|----------------|----------------------|---|
| 1 | nastran_working_directory.zip | 55 | 11 | This configuration includes 11 parameters. The goal is to use the data from the 55 run set to screen parameters and reduce the problem to 4 parameters. Automatic relevance determination (ARD) is used to identify the 4 most relevant parameters. |
| 2 | nastran_working_directory (1).zip | 40 | 4 | This configuration includes 4 parameters. The goal of this 40 run set is to produce training data to fit the surrogate model and make predictions. |
| 3 | nastran_working_directory (2).zip | 8 | 4 | This is an 8 run configuration. This set is used to compare the predicted responses with MSC Nastran responses. |

Performing Predictions

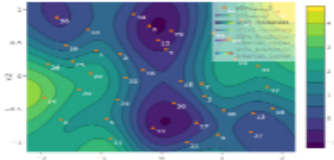
Prediction Analysis Web App

1. Return to the Machine Learning web app
2. Click Results
3. Click Prediction Analysis
4. The Prediction Analysis web app is now open
5. Ensure it says Connected

SOL 200 Web App - Machine Learning Parameters Samples Responses Download **Results** Connection Settings Home

1 2

Select a Results App

 3

Prediction Analysis

SOL 200 Web App - Prediction Analysis 4 Home

Gaussian Process (GP) App Connection Status

✓ Connected 5

Session ID: 8207

Output

```
GP App Update - Starting the Gaussian Process (GP) app on the server
- Session ID: 8207
- Address: http://localhost:8080/optimization
Desktop App Update - Connecting to the SOL 200 Web App...
GP App Update - Connection successful between the Node JS server and GP ap
```

Warnings and Errors

Warnings can be ignored

Training and Testing Data 1

x_training

CSV Export



CSV Import



Select a CSV File



CSV

imported

Delete all rows

y_training

CSV Export



CSV Import



Select a CSV File



sample

Delete all rows

y1

x_testing

CSV Export



CSV Import



Select a CSV File



sample

x1

Delete all rows

x2

y_testing

CSV Export



CSV Import



Select a CSV File



sample

Delete all rows

y1

Training Data

1. Navigate to the Training and Testing Data section
2. Delete any previous table data by clicking the four (4) buttons named Delete all rows

Training Data

1. Navigate to the section titled x_training
2. Click Select files
3. Navigate to the folder named nastran_working_directory (1) which contains data for 40 runs
4. Select the file app.config
5. Click Open
6. Click Import
7. The table is now loaded with the x inputs for all 40 runs

Training and Testing Data

x_training 1

CSV Export Export CSV Import Select files 2 app.config Import 6 CSV imported 7 Delete all rows

| sample | x1 | x2 | x8 | x11 |
|--------|----------|----------|----------|----------|
| 1 | 1. | 4.333333 | 3.051282 | 4.717949 |
| 2 | 1.128205 | 2.538462 | 3.435897 | 3.051282 |
| 3 | 1.25641 | 4.076923 | 5.102564 | 1.897436 |
| 4 | 1.384615 | 5.102564 | 2.794872 | 2.282051 |
| 5 | 1.512821 | 2.025641 | 3.692308 | 5.487179 |
| 6 | 1.641026 | 2.923077 | 5.615385 | 4.205128 |
| 7 | 1.769231 | 2.153846 | 1.384615 | 4.333333 |
| 8 | 1.897436 | 1.512821 | 5.230769 | 1.769231 |
| 9 | 2.025641 | 3.435897 | 1.128205 | 2.025641 |
| 10 | 2.153846 | 5.358974 | 4.974359 | 3.692308 |

« 1 2 3 4 5 6 » 10 25 50 100

Open

« Downloads » nastran_working_directory (1) 3 Search nastran_working_direct...

Organize New folder

Favorites Desktop Downloads Recent Places OneDrive Libraries Documents Music Pictures Videos

| Name | Date modified | Type | Size |
|-----------------------------|-------------------|----------------------|------|
| app | 1/12/2021 6:40 PM | File folder | |
| temp_files_900 | 1/12/2021 7:08 PM | File folder | |
| app.config | 1/12/2021 6:40 PM | CONFIG File | |
| app_monitored_responses.csv | 1/12/2021 7:05 PM | Microsoft Excel C... | |

File name: app.config 5 Custom Files (*.csv;*.config) Open Cancel

Training Data

1. Navigate to the section titled y_training
2. Click Select files
3. Navigate to the folder named nastran_working_directory (1) which contains data for 40 runs
4. Select the file app_monitored_responses.csv
5. Click Open
6. Click Import
7. The table is now loaded with the y outputs (monitored responses) for all 40 runs

y_training 1

CSV Export CSV Import 6

2 Export Select files app_monitored_responses.csv Import CSV imported

7 Delete all rows

| sample | y1 | y2 | y3 | y4 | y5 |
|--------|------------------|-----------------|------------------|------------------|-----------------|
| 0001 | 1623.91901167... | 8805.8452178... | 22821.193146... | 5541.2567430... | 10385.666479... |
| 0002 | 3359.8379505... | 16480.136627... | 27563.192091... | 8512.8851463... | 13898.654026... |
| 0003 | 1651.6868959... | 10161.883720... | 23104.282217... | 5376.7000454... | 6222.3223568... |
| 0004 | 1232.0005870... | 8255.9317966... | 24803.977455... | 5250.8626775... | 8347.9430198... |
| 0005 | 4946.2021206... | 19512.637712... | 35145.876227... | 9580.9854331... | 19529.638862... |
| 0006 | 2380.4355554... | 14895.288913... | 26506.159979... | 5969.11718835... | 8810.7736512... |
| 0007 | 5150.3717122... | 12922.949712... | 34311.3147552... | 9088.31169865... | 23296.951237... |
| 0008 | 2873.0197230... | 20380.366829... | 33906.789193... | 11502.2642270... | 38950.712096... |
| 0009 | 2555.8025261... | 9876.4214755... | 26702.360968... | 5760.68110761... | 21661.738549... |
| 0010 | 1032.2065319... | 9012.4160087... | 22089.927747... | 4261.0030036... | 5458.8500027... |

« 1 2 3 4 5 6 » 10 25 50 100

Open

« Downloads ▶ nastran_working_directory (1) ▶ 3 Search nastran_working_direct...

Organize New folder

Favorites Desktop Downloads Recent Places OneDrive

Libraries Documents Music Pictures Videos

| Name | Date modified | Type | Size |
|--|-------------------|----------------------|------|
| app | 1/12/2021 6:40 PM | File folder | |
| temp_files_900 | 1/12/2021 7:08 PM | File folder | |
| app.config | 1/12/2021 6:40 PM | CONFIG File | |
| app_monitored_responses.csv 4 | 1/12/2021 7:05 PM | Microsoft Excel C... | |

File name: app_monitored_responses.csv 5 Custom Files (*.csv;*.config) Open Cancel

Perform Regression

1. Click Perform Regression and the surrogate model will be fitted
2. The regression is complete when the following status message is visible:
 - Process complete

Regression

| Data | Link to Table | Status | Status Description |
|----------------------|----------------------|--------|--------------------|
| x_training | Link | ✓ | Ready |
| y_training | Link | ✓ | Ready |
| x_testing (Optional) | Link | ⓘ | Ready |
| y_testing (Optional) | Link | ⓘ | Ready |

 Perform Regression

✓ Process complete

[Click here](#) to view the Regression Results section

Output

```
| y3      | 6.34332 | 22.8637 | 0.285728 | 12.5891 |
| y4      | 0.329643 | 7.79946 | 7.49135 | 3.58932 |
| y5      | 0.00412772 | 298.861 | 0.9722 | 0.00234721 |
| y6      | 0.65093 | 20.7999 | 22.9172 | 3.70404 |
| y7      | 0.274844 | 35.1077 | 1.39711 | 3.72269 |
| y8      | 0.00739204 | 105.864 | 6.33735 | 2.76692 |
| y9      | 0.22452 | 47.8042 | 0.824128 | 4.19834 |
```

Parameters listed in decreasing order of relevance: x2, x8, x11, x1
GP App Update - Sending initial data to the web browser
GP App Update - Sending complete

Warnings and Errors

```
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/GPy/kern/src/st
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/GPy/kern/src/st
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/GPy/kern/src/st
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/GPy/kern/src/st
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/GPy/kern/src/st
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/paramz/transform
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/GPy/kern/src/rb
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/GPy/kern/src/st
/home/apricot/PycharmProjects/python-app/venv/lib/python3.6/site-packages/GPy/kern/src/st
```

Warnings can be ignored

Perform Prediction

1. Navigate to the section titled x_prediction
2. Click Select files
3. Navigate to the location of the file named samples.csv
4. Select the file samples.csv
5. Click Open
6. Click Import
7. The table is now loaded with the x inputs for 8 runs

Prediction

x_prediction ①

CSV Export

CSV Import



samples.csv

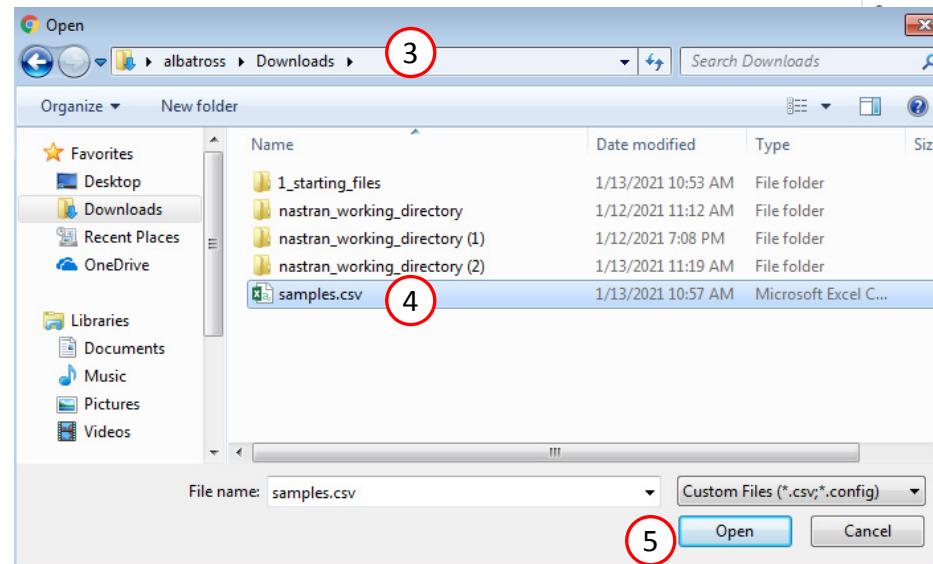


CSV
imported

Delete all rows

| sample | x1 | x2 | x8 | x11 |
|--------|----------|----------|----------|----------|
| 1 | 1. | 4.571429 | 3.142857 | 1.714286 |
| 2 | 1.714286 | 3.857143 | 4.571429 | 6. |
| 3 | 2.428571 | 1. | 1.714286 | 3.857143 |
| 4 | 3.142857 | 1.714286 | 6. | 2.428571 |
| 5 | 3.857143 | 5.285714 | 1. | 4.571429 |
| 6 | 4.571429 | 6. | 5.285714 | 3.142857 |
| 7 | 5.285714 | 3.142857 | 2.428571 | 1. |
| 8 | 6. | 2.428571 | 3.857143 | 5.285714 |

10 25 50 100




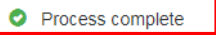
Perform Prediction

1. Navigate to the section titled Perform Prediction
2. Click Perform Prediction
3. The prediction is complete when the following status message is visible:
 - Process complete

- Note that the predictions are performed seemingly instantly

Perform Prediction ¹

 ²

 ³

[Click here](#) to view the Prediction Results section

Output

```
GP App Update - The web browser has requested a prediction
GP App Update - Determining prediction
GP App Update - Normalizing Design - Scaling and shifting the input space to [0,1]
GP App Update - Sending prediction data to the web browser
GP App Update - Sending complete
```

Warnings and Errors

Warnings can be ignored

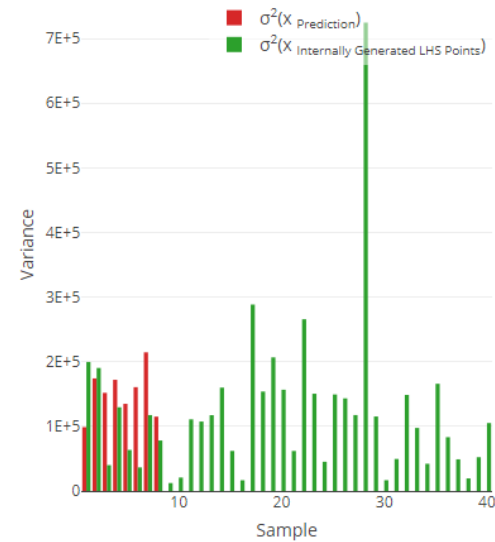
Variance

1. Navigate to the section titled Variance

Variance 1

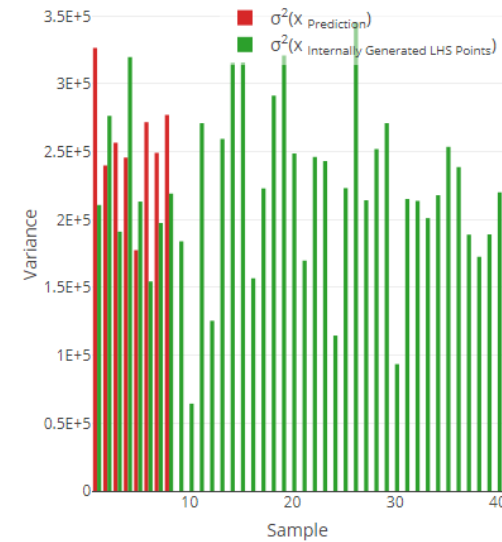
Matern52

NRMSE:



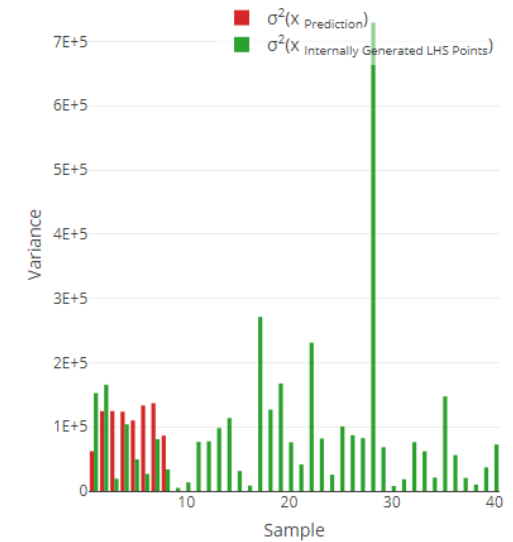
Exponential

NRMSE:



RBF

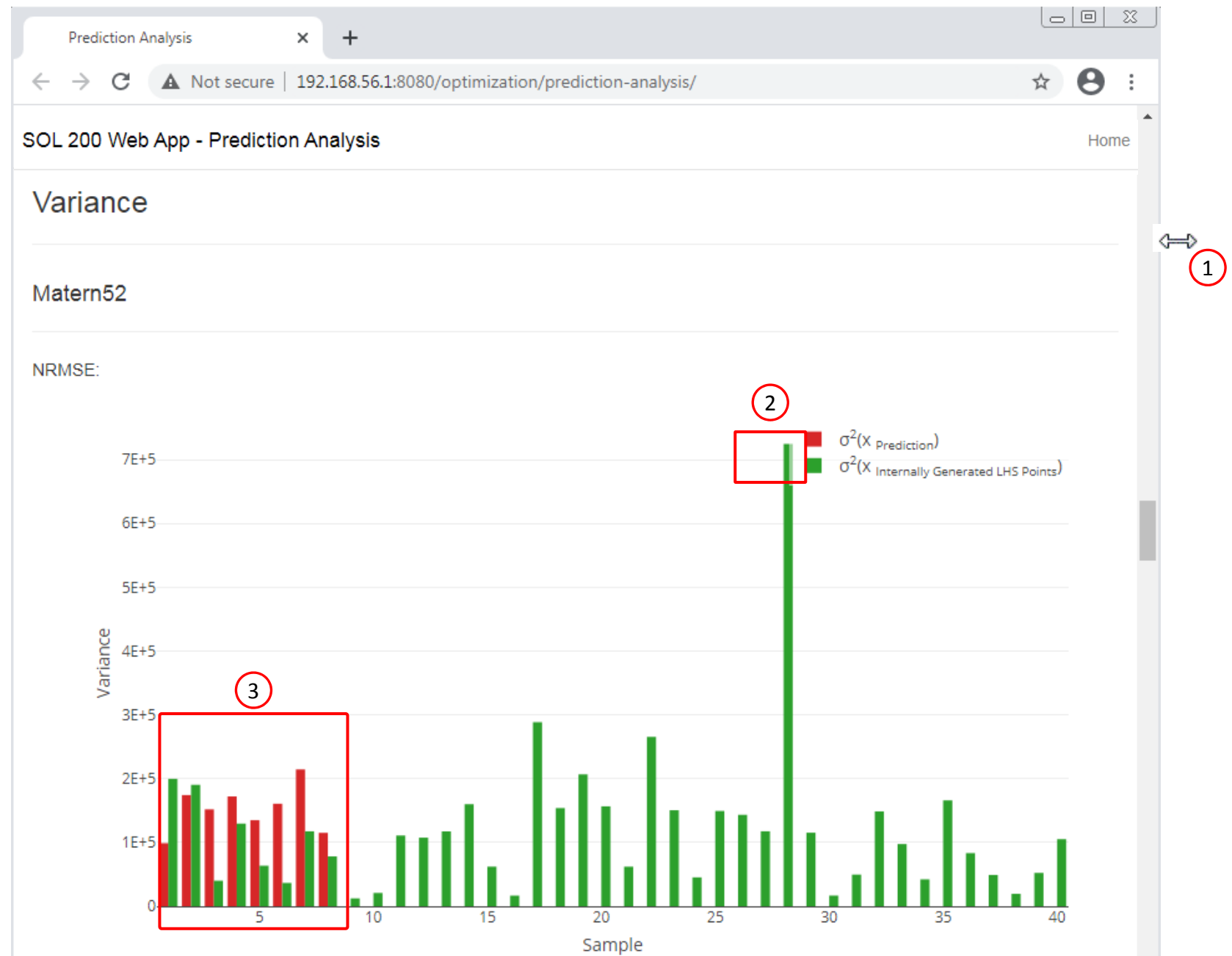
NRMSE:



Variance

1. Resize the window to fit half the screen, this causes the plot to be increased in size
2. A high bar indicates a high prediction uncertainty, or a high variance, and is indication that we do not have enough information to conclude the prediction is credible at that prediction point.
3. Predictions have been made at 8 samples and are indicated by 8 red bars
 - When making predictions, the prediction uncertainty should ideally be low, like in this example

- In this tutorial, variance (σ^2) is used to gauge the prediction uncertainty. Sometimes, you will see this prediction uncertainty expressed as the standard deviation (σ).



Pressure vs. Frequency

For frequency responses and after a prediction is performed, Response vs. Frequency plots are automatically generated.

1. Navigate to the section titled XYPLOT
2. Set Select a response to r8
3. Set Select a sample to 2
4. Set Include 95% Prediction Intervals to Yes
5. Set the Vertical Axis Format to Linear
6. The predicted plots are now displayed. Since 3 kernel functions were used during regression, there are 3 predicted plots.

XYPLOT

Select a response

r8

Select a sample

1
2
3
4
5

Include 95% Prediction Intervals?

Yes

Matern52

Exponential

RBF

Vertical Axis Format

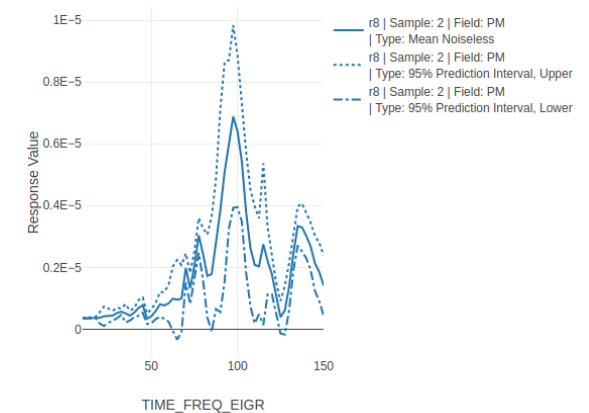
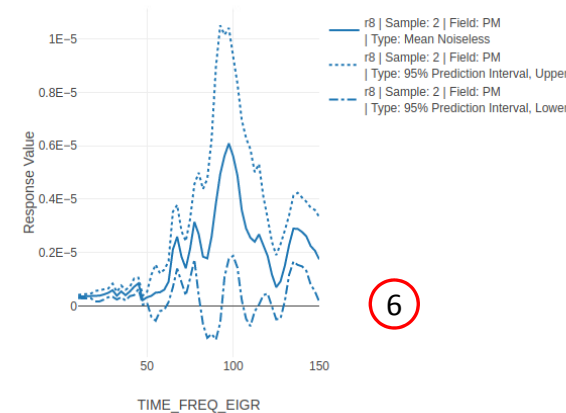
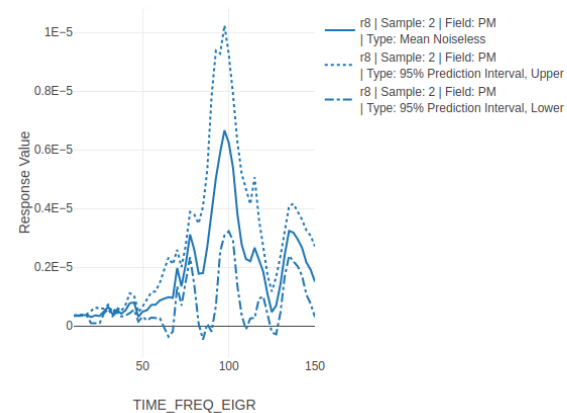
Linear

Vertical Axis Format

Linear

Vertical Axis Format

Linear



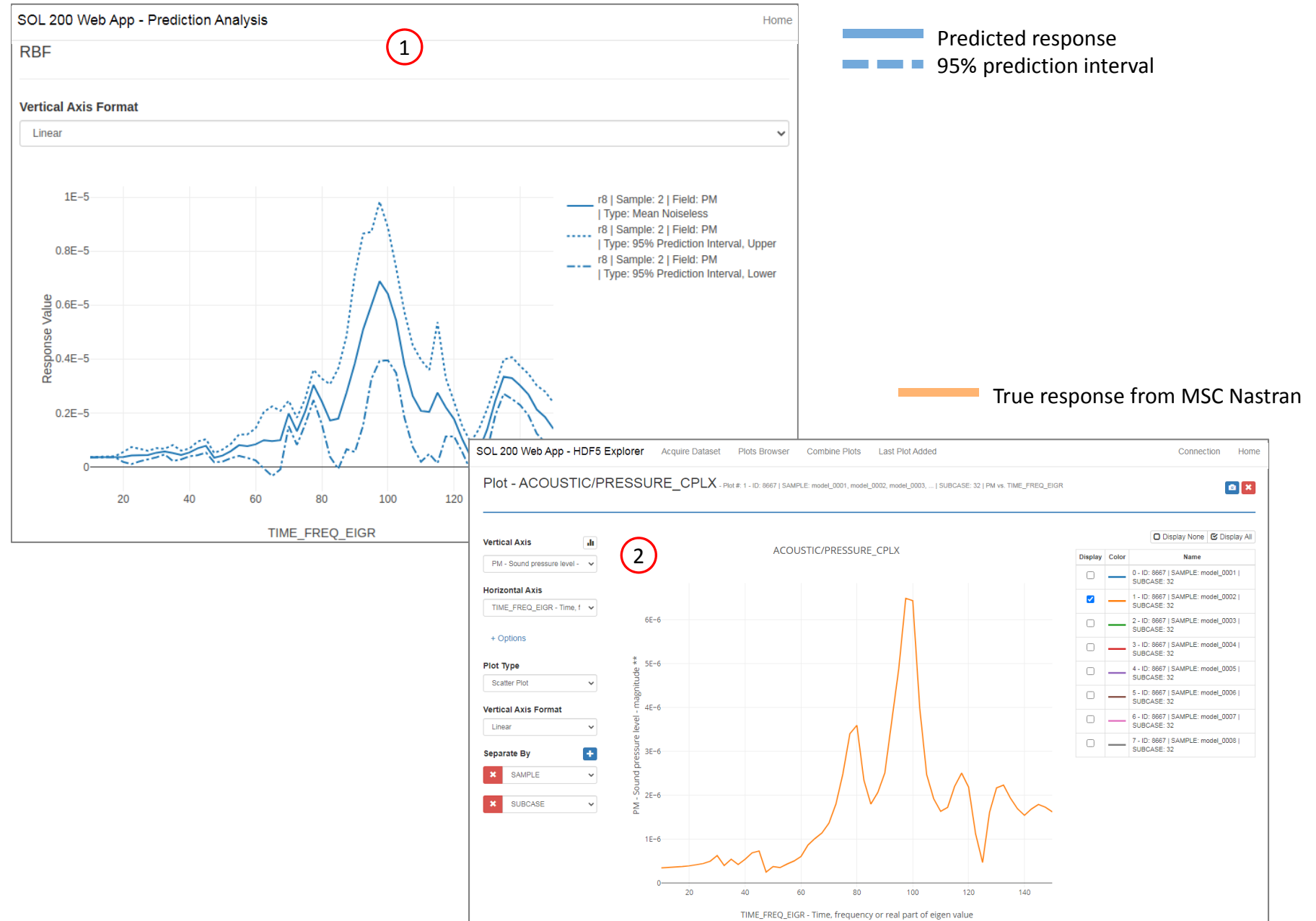
Comparison of Prediction with MSC Nastran

Recall that batch 2 was used to produce the training data and fit the surrogate model. Batch 3 contained 8 sample points.

1. The surrogate model was used to predict the output responses at the 8 sample points. The predicted response vs. frequency plot is displayed.
2. MSC Nastran was used to evaluate all 8 sample points and the HDF5 Explorer was used to display the true response vs. frequency plots.

A comparison can be made between the prediction and MSC Nastran output.

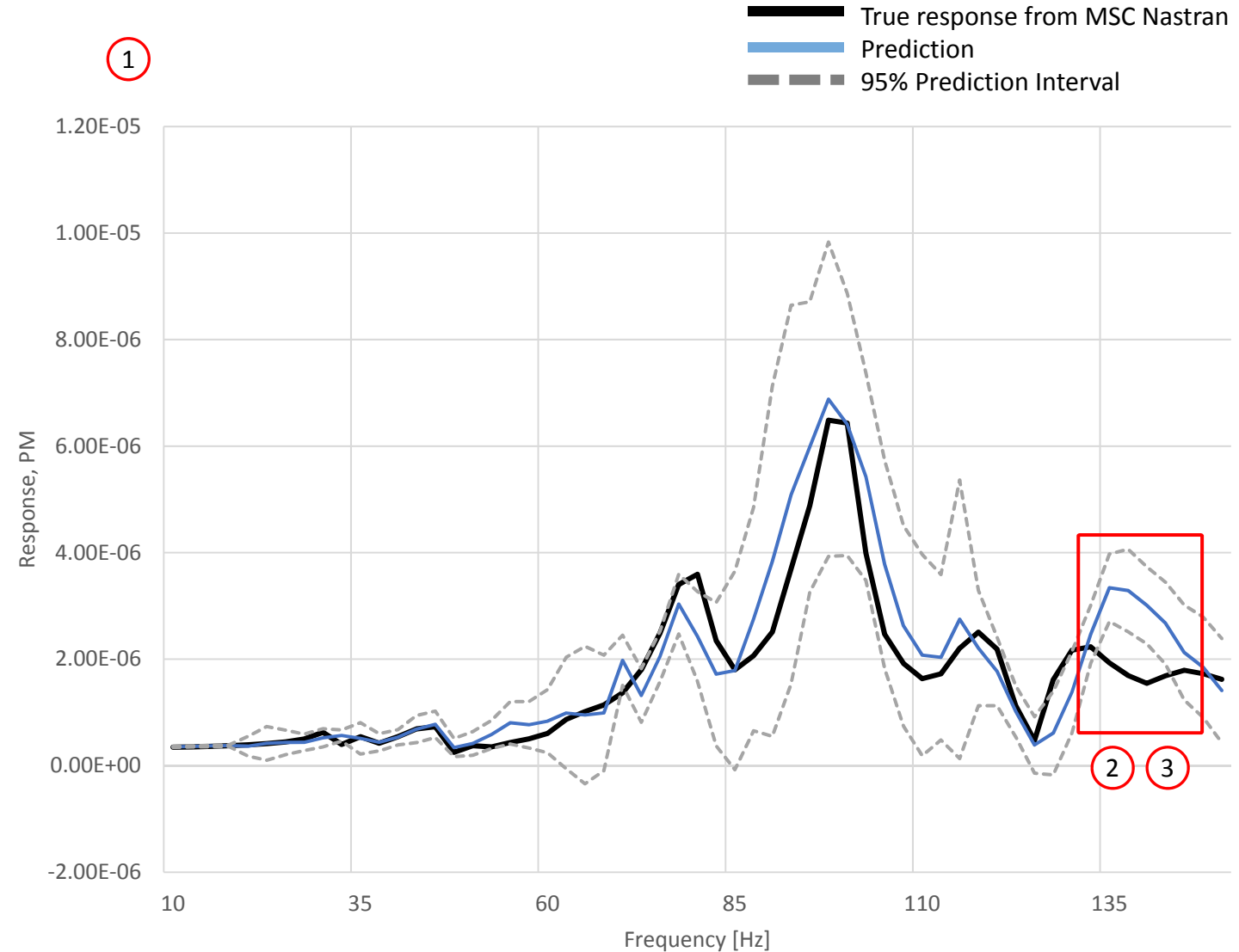
- In this tutorial, variance (σ^2) is used to gauge the prediction uncertainty. Sometimes, you will see this prediction uncertainty expressed as the standard deviation (σ).



Comparison of Prediction with MSC Nastran

1. Optional - Excel was used to overlap the MSC Nastran output over the predicted response
2. Note that the 95% prediction interval does not guarantee the true value is within this interval.
3. With a limited number of samples, the surrogate model poorly predicts the true response between 80-100Hz

- In some cases, using more samples improves the surrogate model. You are encouraged to repeat this exercise but with additional samples. For example, this prediction used 40 samples. Perhaps repeat this prediction with 50, 60 or 70 samples.

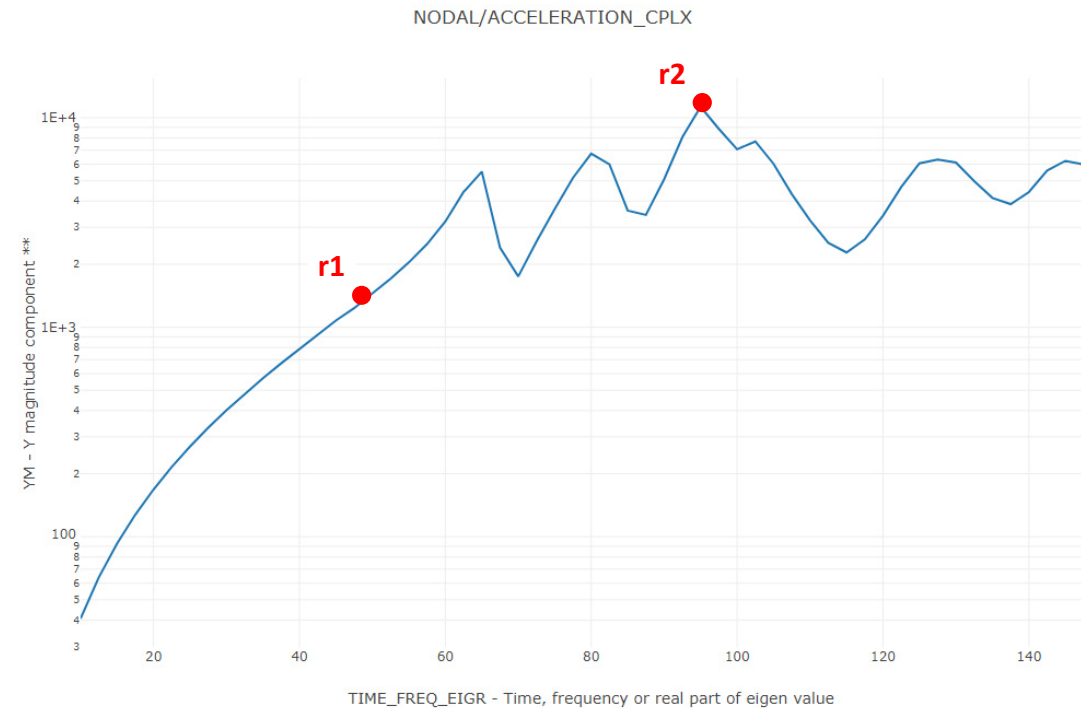


Creating Response vs. Frequency Plots with the HDF5 Explorer

Responses

Recall the following

- r1 is the response at 50Hz
- r2 is the maximum responses across all frequencies



ID: 1001 | SUBCASE: 12 | YM vs. TIME_FREQ_EIGR

Start Desktop App

1. Open this folder:
nastran_working_directory (2)
2. Inside of the new folder, double click on
Start Desktop App
3. Click Open, Run or Allow Access on any
subsequent windows

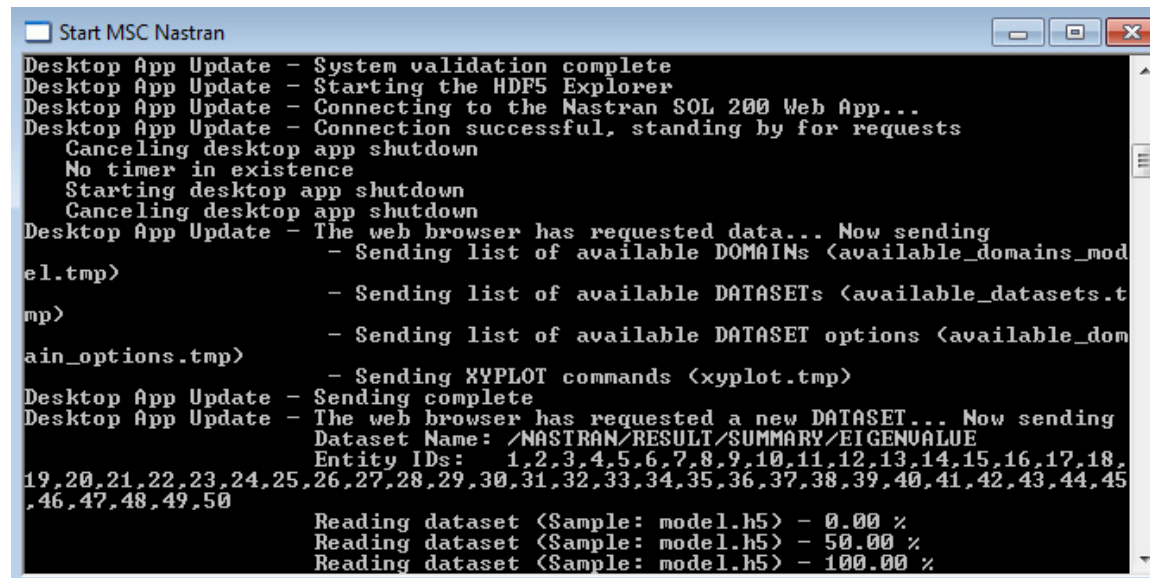
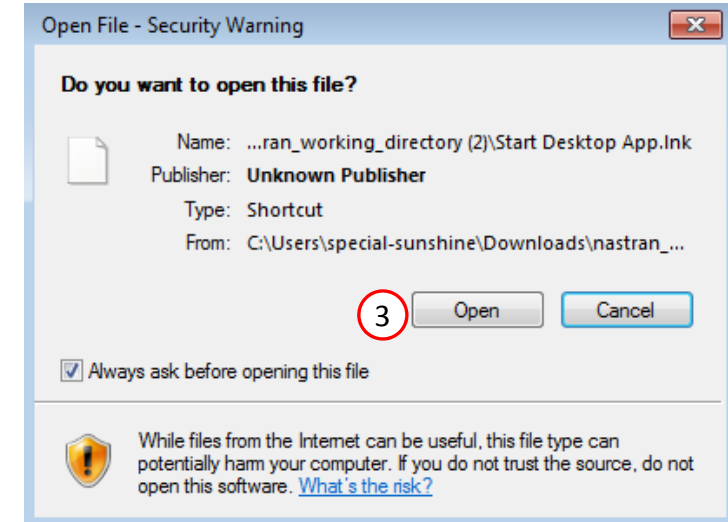
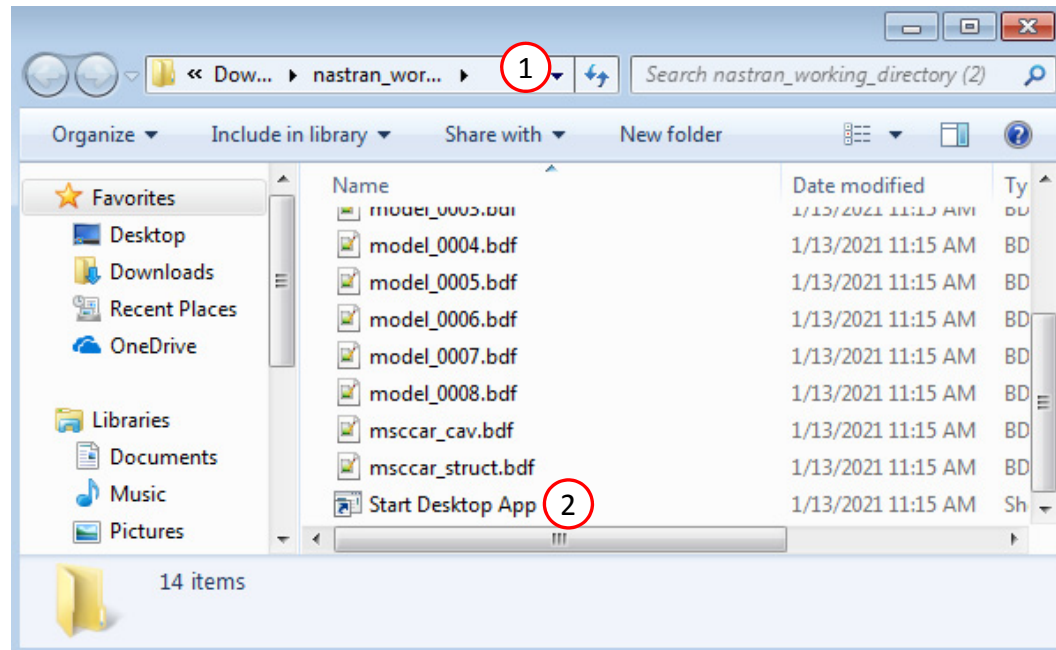
Using Linux?

Follow these instructions:

- 1) Open Terminal
- 2) Navigate to the nastran_working_directory
`cd ./nastran_working_directory`
- 3) Use this command to start the process
`./Start_MSC_Nastran.sh`

In some instances, execute permission must be granted to the directory. Use this command. This command assumes you are one folder level up.

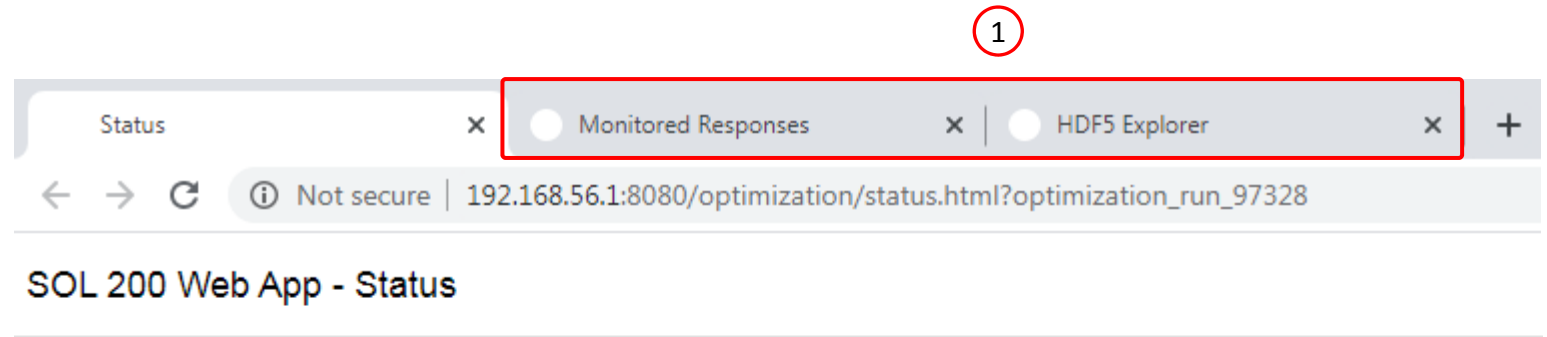
```
sudo chmod -R u+x ./nastran_working_directory
```



Results

Multiple web apps are automatically opened to display the results.

1. Use the tabs to switch between each web app
2. A description of each web app is given in the table.



2

| Name of Web App | Purpose | Description |
|---------------------|---|--|
| Monitored Responses | <ul style="list-style-type: none">• The response value from each sample can be compared. | <ul style="list-style-type: none">• After each MSC Nastran analysis, the response values are extracted from the H5 file and contained in a file named app_monitored_responses.csv. The Monitored Responses web app is used to create a bar chart of the values contained in this CSV file. |
| HDF5 Explorer | <ul style="list-style-type: none">• This web app is used to probe each H5 file and generate XY plots. | |

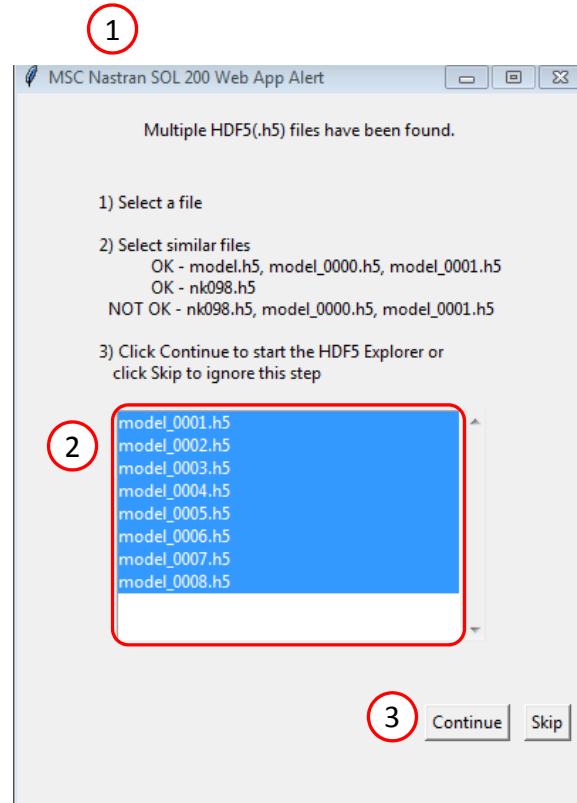
Review Results

The following steps describe how to start the HDF5 Explorer and display the plots for responses r1 and r2.

1. A new window is opened
2. Select all H5 files in the list
3. Click Continue
4. Click Plots Browser
5. Click the indicated plot:
 - Plot #: 5 - ID: 1001 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 12 | YM vs. TIME_FREQ_EIGR

The HDF5 Explorer is broken into sections.

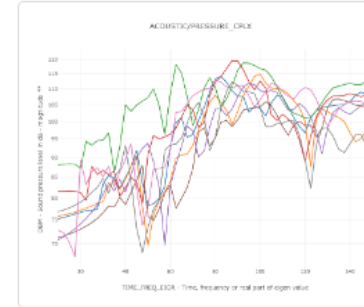
- Acquire Dataset – Specific datasets from the H5 file can be extracted in this section.
- Plots Browser – Use this section to navigate every plot created.
- Combine Plots – This section allows you to combine multiple plots. For example, you can create Load vs. Displacement plots in this section.
- Last Plot Added – This display the last plot that was created.



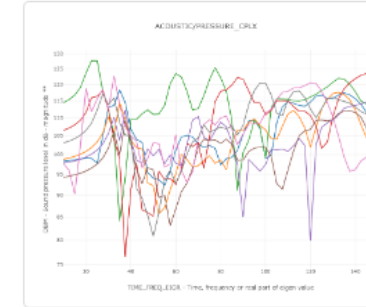
4

Plots Browser

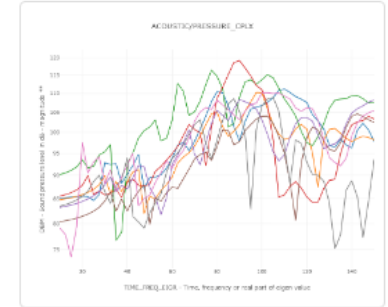
ACOUSTIC/PRESSURE_CPLX



Plot #: 1 - ID: 8667 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 12 | DBM vs. TIME_FREQ_EIGR

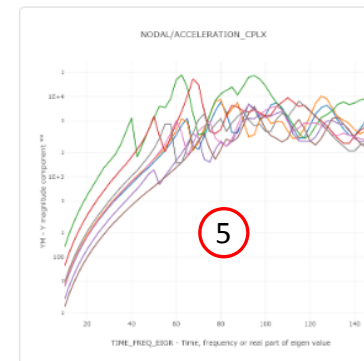


Plot #: 2 - ID: 8667 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 13 | DBM vs. TIME_FREQ_EIGR

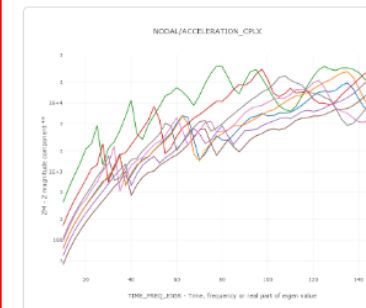


Plot #: 3 - ID: 8667 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 32 | DBM vs. TIME_FREQ_EIGR

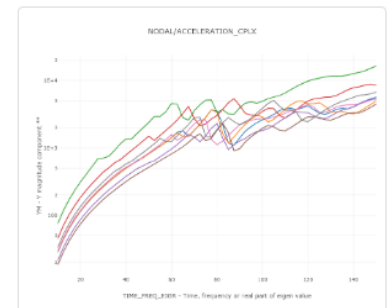
NODAL/ACCELERATION_CPLX



Plot #: 5 - ID: 1001 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 12 | YM vs. TIME_FREQ_EIGR



Plot #: 6 - ID: 1001 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 13 | ZM vs. TIME_FREQ_EIGR



Plot #: 7 - ID: 1003 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 32 | YM vs. TIME_FREQ_EIGR

Review Results

This plot will be referenced later

The plots in the HDF5 explorer have additional functionalities that are hidden by default. Click on any of the following to show the extra functions.

- A. + Options
- B. + View Filters and Plotted Values

Users are encouraged to experiment with the additional functions.

Plot - NODAL/ACCELERATION_CPLX - Plot #: 5 - ID: 1001 | SAMPLE: model_0001, model_0002, model_0003, ... | SUBCASE: 12 | YM vs. TIME_FREQ_EIGR



Vertical Axis



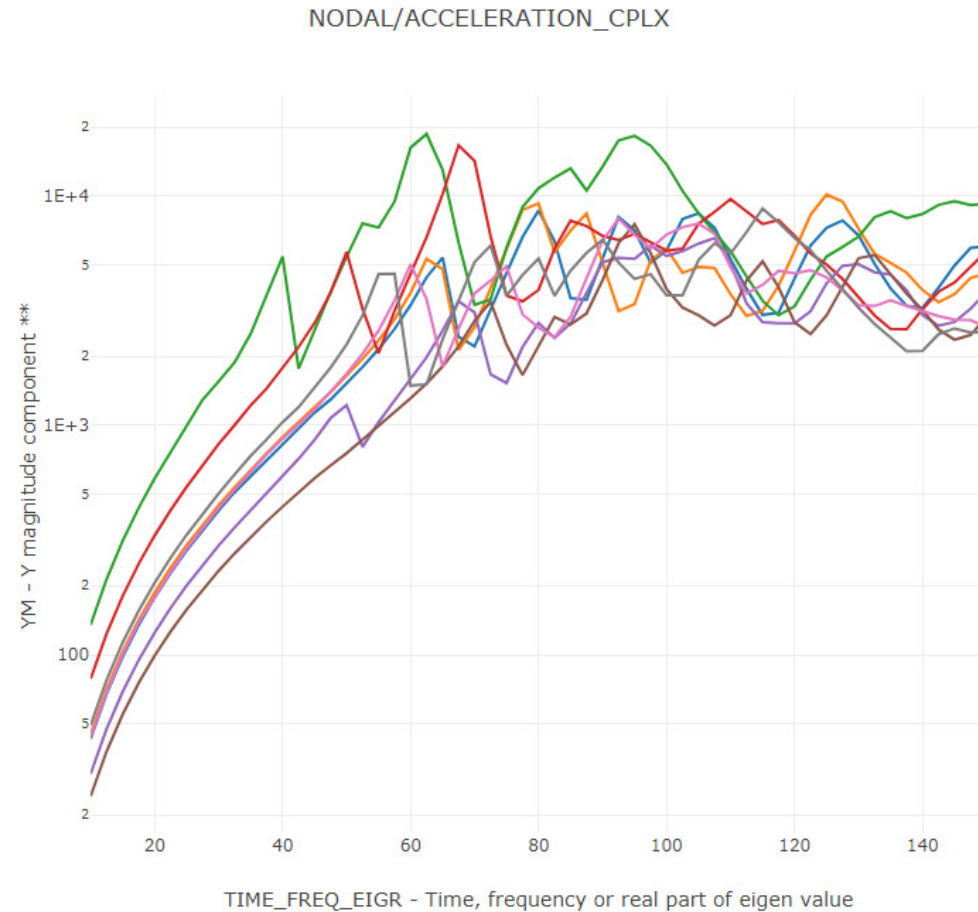
YM - Y magnitude compon

Horizontal Axis

TIME_FREQ_EIGR - Time

+ Options

A



☐ Display None ☒ Display All

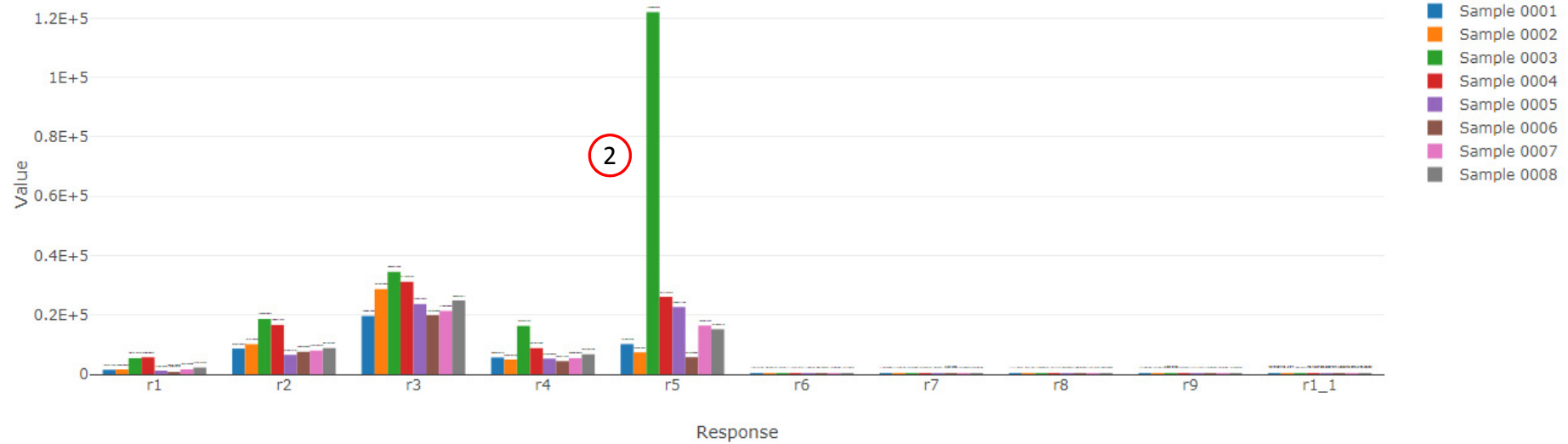
| Display | Color | Name |
|-------------------------------------|--------|---|
| <input checked="" type="checkbox"/> | Blue | 0 - ID: 1001 SAMPLE: model_0001 SUBCASE: 12 |
| <input checked="" type="checkbox"/> | Orange | 1 - ID: 1001 SAMPLE: model_0002 SUBCASE: 12 |
| <input checked="" type="checkbox"/> | Green | 2 - ID: 1001 SAMPLE: model_0003 SUBCASE: 12 |
| <input checked="" type="checkbox"/> | Red | 3 - ID: 1001 SAMPLE: model_0004 SUBCASE: 12 |
| <input checked="" type="checkbox"/> | Purple | 4 - ID: 1001 SAMPLE: model_0005 SUBCASE: 12 |
| <input checked="" type="checkbox"/> | Brown | 5 - ID: 1001 SAMPLE: model_0006 SUBCASE: 12 |
| <input checked="" type="checkbox"/> | Pink | 6 - ID: 1001 SAMPLE: model_0007 SUBCASE: 12 |
| <input checked="" type="checkbox"/> | Grey | 7 - ID: 1001 SAMPLE: model_0008 SUBCASE: 12 |

B

+ View Filters and Plotted Values

Review Results

1. The Monitored Responses web app is opened
2. The value of each response and for each sample is displayed in a bar chart
3. A table lists the values for each response and sample.



B

Monitored Responses

Display MAX and MIN Download CSV Reset Filters

| Label | Dataset Name | Field | Field Description |
|------------------------------------|---|-----------------|--|
| r1 r1_1 r1_2 r1_3 r1_4 | ACOUSTIC/PRESSURE_CPLX NODAL/ACCELERATION_CPLX | DBM YM ZM | Sound pressure level in dB - mag Y magnitude component ** Z magnitude component ** |
| r1 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |
| r2 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |
| r3 | NODAL/ACCELERATION_CPLX | ZM | Z magnitude component ** |
| r4 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |

Monitored Responses from Each Sample

3

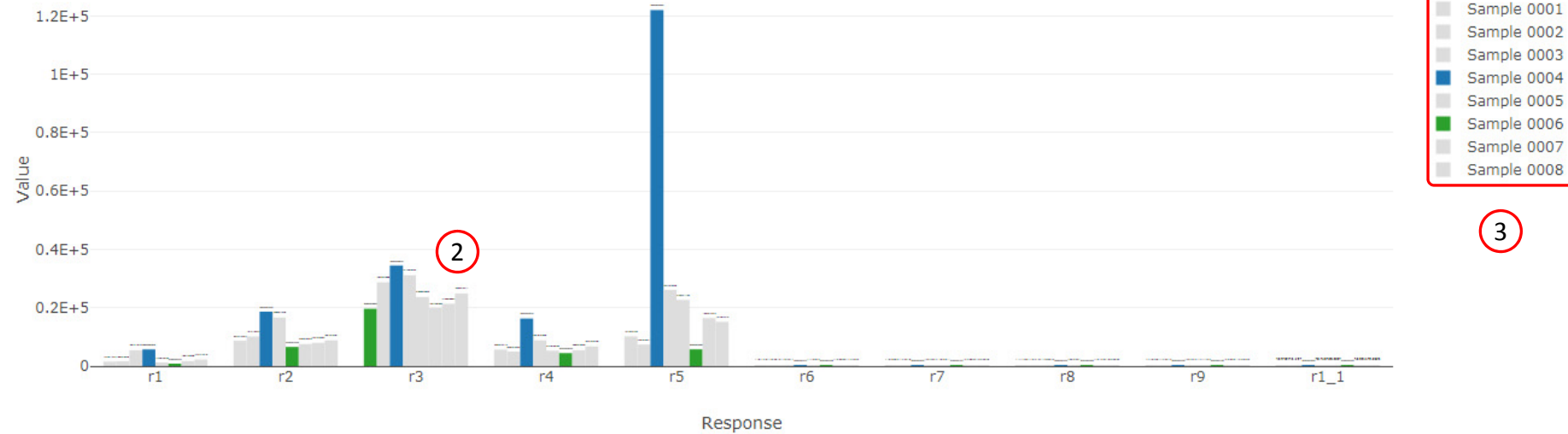
| 0001 | 0002 | 0003 | 0004 |
|--------------------|--------------------|--------------------|--------------------|
| 1526.125681263411 | 1646.542449357661 | 5431.856987635404 | 5706.046062108631 |
| 8657.530528587466 | 10151.6078119792 | 18656.548989469935 | 16649.137630152713 |
| 19648.168717343582 | 28702.664023028425 | 34493.15381275541 | 31158.639324650096 |
| 5643.971287579098 | 4963.355450686416 | 16309.51034127708 | 8814.994819594214 |

- A. The table titled Monitored Response can be interacted with. Each column in the table contains filters. Once a filter is modified, the Bar Chart will instantly update.
- B. Additional functions include the ability to highlight the MAX and MIN bars, download a CSV file and reset the filters.

Review Results

1. Click Display MAX and MIN
2. The bars are now colored blue, green and gray
3. The legend is displayed on the top right corner

- When Display MAX and MIN is clicked, for each response the maximum bar is colored blue and the minimum is colored green.
- The coloring in the legend on the top right corner is only accurate for the first response displayed. In the figure shown, for response r1, sample 4 produces the maximum response and sample 6 produces the minimum response.



Monitored Responses

Display MAX and MIN Download CSV Reset Filters

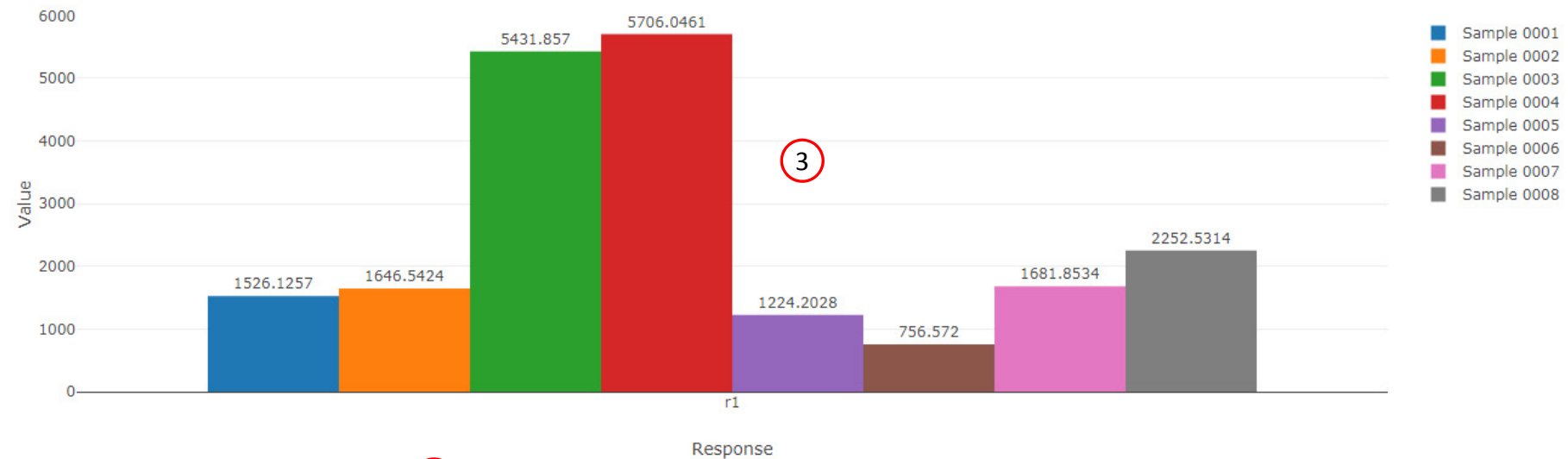
| Label | Dataset Name | Field | Field Description |
|------------------------------------|---|-----------------|--|
| r1 r1_1 r1_2 r1_3 r1_4 | ACOUSTIC/PRESSURE_CPLX NODAL/ACCELERATION_CPLX | DBM YM ZM | Sound pressure level in dB - mag Y magnitude component ** Z magnitude component ** |
| r1 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |
| r2 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |
| r3 | NODAL/ACCELERATION_CPLX | ZM | Z magnitude component ** |
| r4 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |
| r5 | NODAL/ACCELERATION_CPLX | ZM | Z magnitude component ** |
| r6 | ACOUSTIC/PRESSURE_CPLX | DBM | Sound pressure level in dB - mag |

Monitored Responses from Each Sample

| 0001 | 0002 | 0003 | 0004 | |
|--------------------|--------------------|--------------------|--------------------|---|
| 1526.125681263411 | 1646.542449357661 | 5431.856987635404 | 5706.046062108631 | 1 |
| 8657.530528587466 | 10151.6078119792 | 18656.548989469935 | 16649.137630152713 | 6 |
| 19648.168717343582 | 28702.664023028425 | 34493.15381275541 | 31158.639324650096 | 2 |
| 5643.971287579098 | 4963.355450686416 | 16309.51034127708 | 8814.994819594214 | 5 |
| 10180.927393382006 | 7386.50209251185 | 122054.75754985167 | 26125.939837904127 | 2 |
| 114.1514155253656 | 114.94181882212138 | 118.76114036753917 | 119.51549857017466 | 1 |

Review Results

1. Click Display MAX and MIN
2. In the filters, select the following:
 - Label: r1
3. Only the responses for response r7 are now shown



1

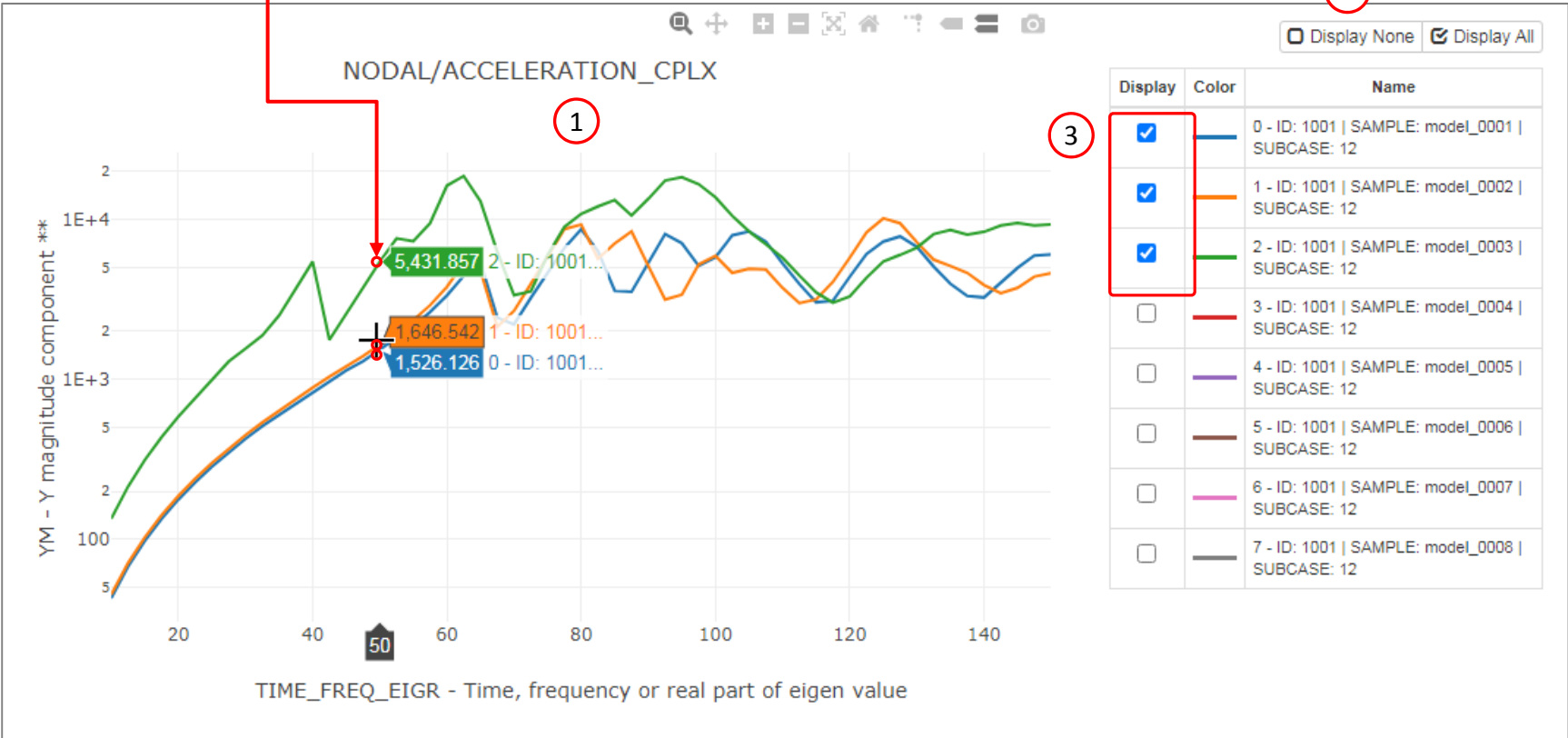
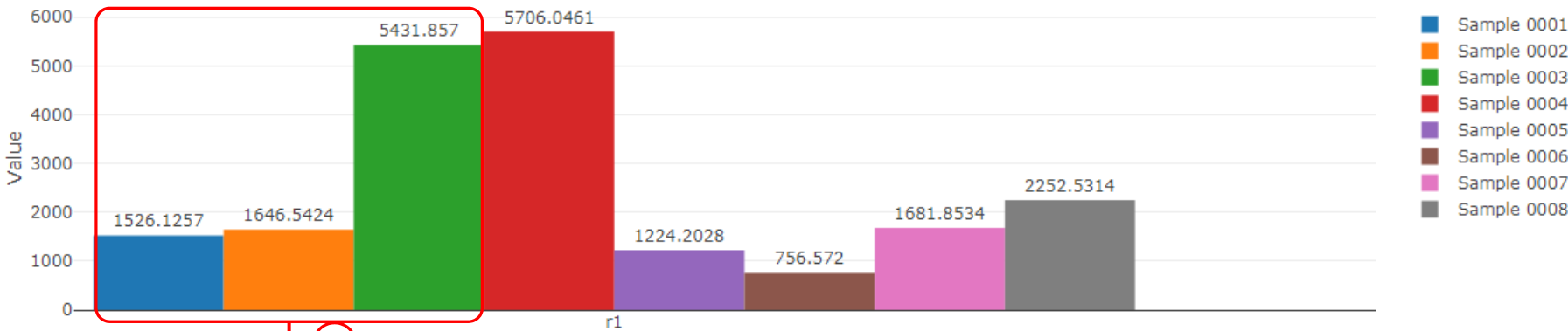
| Monitored Responses | | | |
|--|--|--|---|
| Display MAX and MIN Download CSV Reset Filters | | | |
| Label | Dataset Name | Field | Field Description |
| <div> <div>2</div> <div> <div>r1</div> <div>r1_1</div> <div>r1_2</div> <div>r1_3</div> <div>r1_4</div> </div> </div> | <div>ACOUSTIC/PRESSURE_CPLX</div> <div>NODAL/ACCELERATION_CPLX</div> | <div>DBM</div> <div>YM</div> <div>ZM</div> | <div>Sound pressure level in dB - magnitude</div> <div>Y magnitude component **</div> <div>Z magnitude component **</div> |

[illegible]

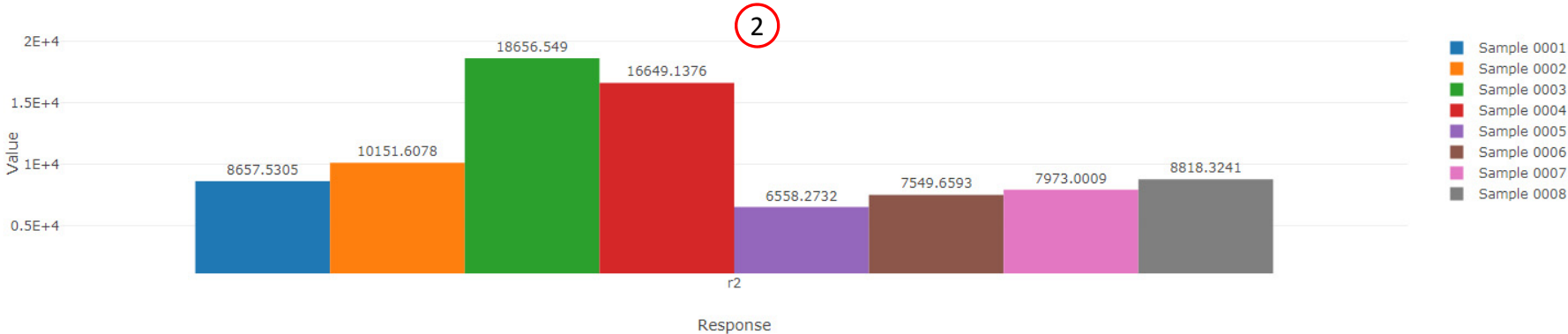
| Monitored Responses | | | |
|--|---|---|--|
| <div> Display MAX and MIN Download CSV Reset Filters </div> | | | |
| Label | Dataset Name | Field | Field Description |
| <div> <div>2</div> <div> <div>r1</div> <div>r1_1</div> <div>r1_2</div> <div>r1_3</div> <div>r1_4</div> </div> </div> | <div> <div>ACOUSTIC/PRESSURE_CPLX</div> <div>NODAL/ACCELERATION_CPLX</div> </div> | <div> <div>DBM</div> <div>YM</div> <div>ZM</div> </div> | <div> <div>Sound pressure level in dB - magnitude</div> <div>Y magnitude component **</div> <div>Z magnitude component **</div> </div> |

Review Results

1. Refer to the plot that was previously shown
2. Click Display None
3. Mark the checkboxes for the first 3 rows (Samples 0, 1 and 2)
4. The response values that were extracted and displayed in the bar chart match the values at 50Hz in the Acceleration vs. Frequency plot



- Refer to the Appendix for an explanation on the use of the following:
 - Monitor the maximum or minimum response, whichever has the greatest absolute value: Yes, No or blank



Review Results

- 1. In the filters, select only response r2
- 2. Only the responses for response r2 are now shown

Monitored Responses

Display MAX and MIN Download CSV Reset Filters

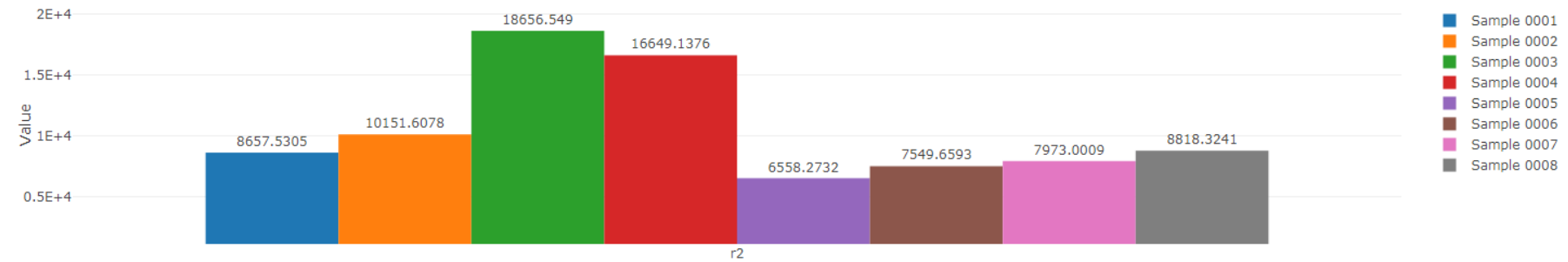
| Label | Dataset Name | Field | Field Description |
|----------------------------|---|-----------------|---|
| r1_56 r1_57 r2 r3 | ACOUSTIC/PRESSURE_CPLX NODAL/ACCELERATION_CPLX | DBM YM ZM | Sound pressure level in dB - magnitude ** Y magnitude component ** Z magnitude component ** |
| r2 | NODAL/ACCELERATION_CPLX | YM | Y magnitude component ** |

Monitored Responses from Each Sample

| 0001 | 0002 | 0003 | 0004 | 0005 |
|-------------------|------------------|--------------------|--------------------|----------------|
| 8657.530528587466 | 10151.6078119792 | 18656.548989469935 | 16649.137630152713 | 6558.273211742 |

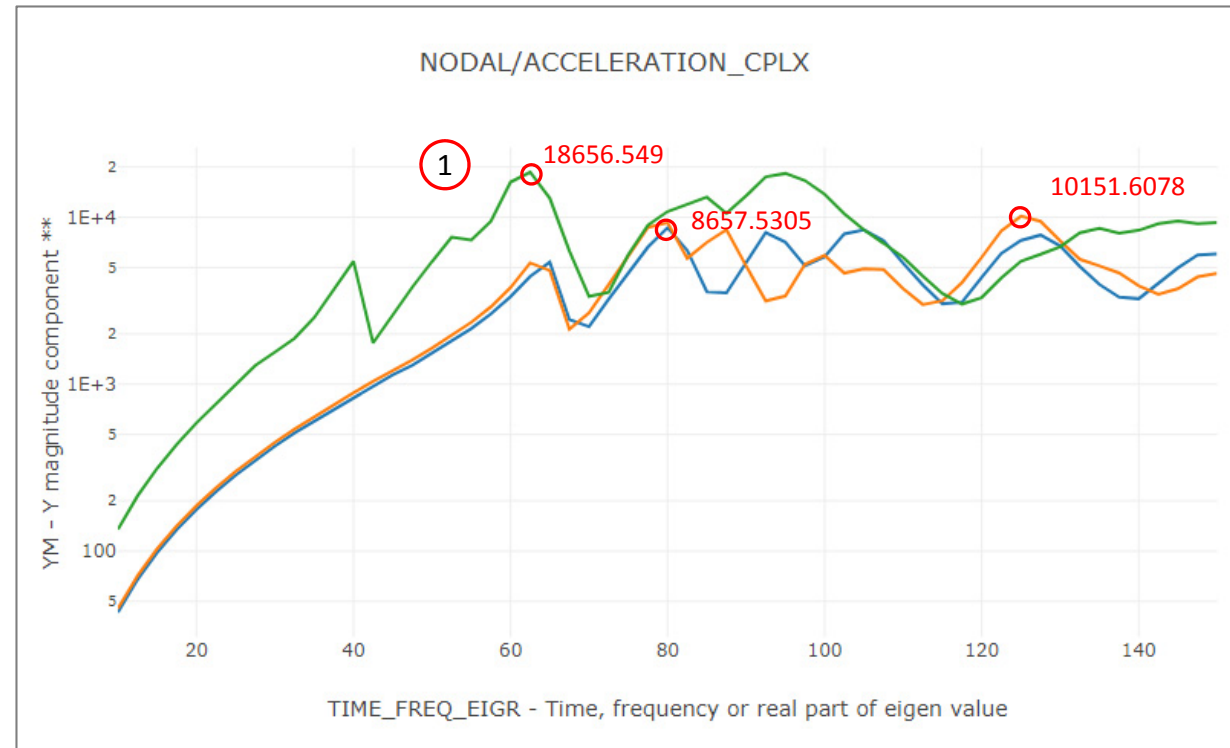
Monitored Responses

| Label | Dataset Name |
|----------------------------|---|
| r1_56 r1_57 r2 r3 | ACOUSTIC/PRESSURE_CPLX NODAL/ACCELERATION_CPLX |
| r2 | NODAL/ACCELERATION_CPLX |



Review Results

- The response values that were extracted and displayed in the bar chart match the peak values in the Acceleration vs. Frequency plot



- Refer to the Appendix for an explanation on the use of the following:
 - Monitor the maximum or minimum response, whichever has the greatest absolute value: Yes, No or blank

End of Tutorial

Appendix

Appendix Contents

- Response Configuration
 - Monitor the maximum or minimum response, whichever has the greatest absolute value: Yes, No or blank
- How to import and edit previous files
- What is Gaussian Process Regression?

Response Configuration

During this tutorial, this option was used:

- Monitor the maximum or minimum response, whichever has the greatest absolute value : Yes

Suppose response r99 is configured for 10 seconds and corresponds to point A on the plot. When Yes is used for the option, the response furthest from the horizontal axis is monitored. In this example, points B and C are furthest from the horizontal axis. Since point B is furthest from the horizontal axis, a value of -15000.0 is monitored.

View Responses to Monitor

Monitored Responses

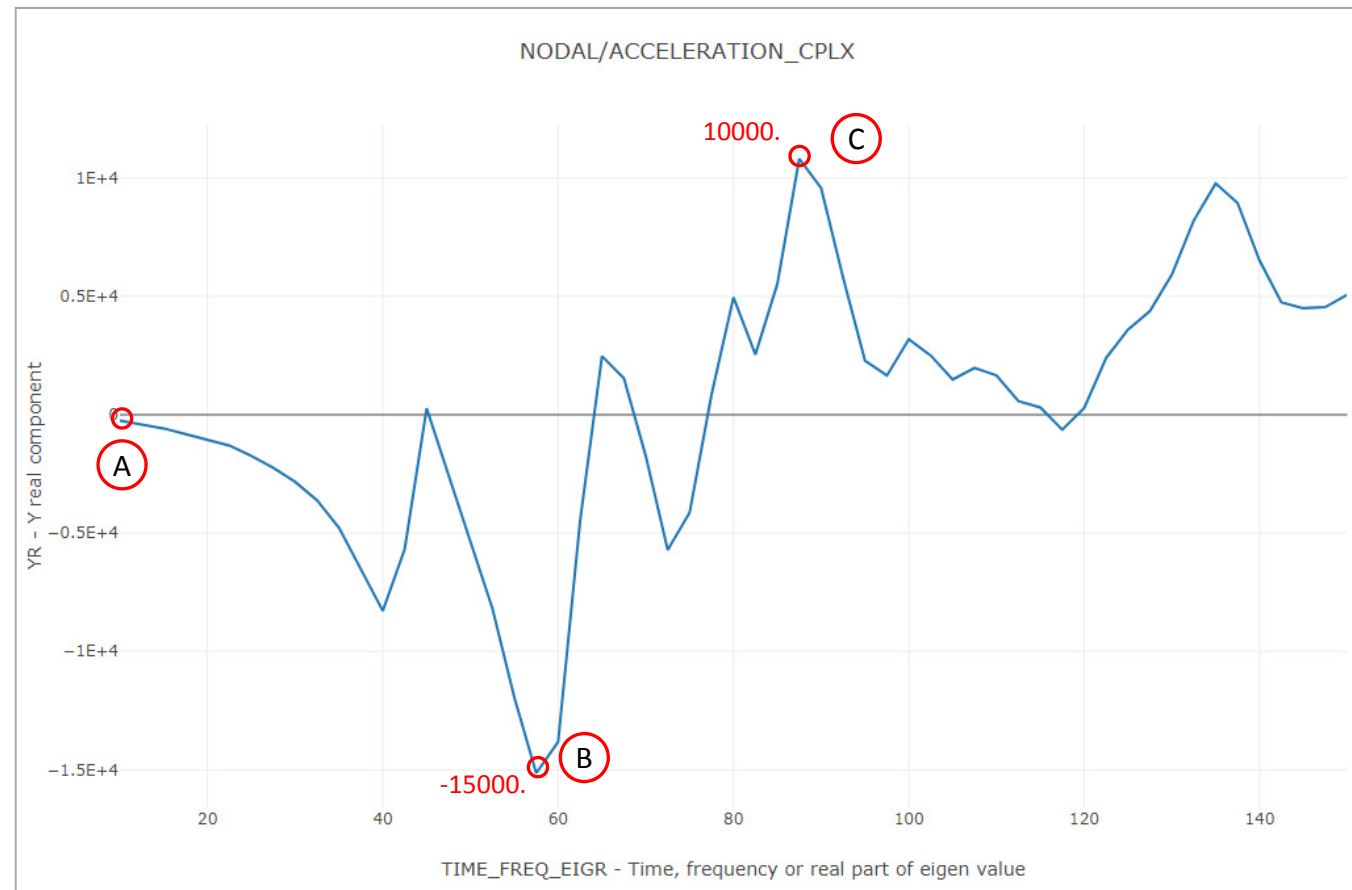
| Delete | Label | Status | Objective | Lower Bound | Upper Bound | Monitor the response of the FINAL design cycle (SOL 200 only) | Monitor the maximum or minimum response, whichever has the greatest absolute value |
|--------|-------|--------|----------------------|-------------|-------------|---|--|
| | r99 | | <input type="text"/> | Lower | Upper | <input type="text"/> | Yes - Monitor the maximum respon |

Monitor the maximum or minimum response, whichever has the greatest absolute value

Yes - Monitor the maximum respon

Hide/Show Columns Reset Filters Download CSV

| Current Value | ID | SUBCASE | STEP | ANALYSIS |
|-------------------|------|---------|------|----------|
| 1443.476297324485 | 1001 | 12 | 0 | 5 |



How to import and edit previous files

How to import and edit previous files

The parameters, samples and responses are contained in the following files

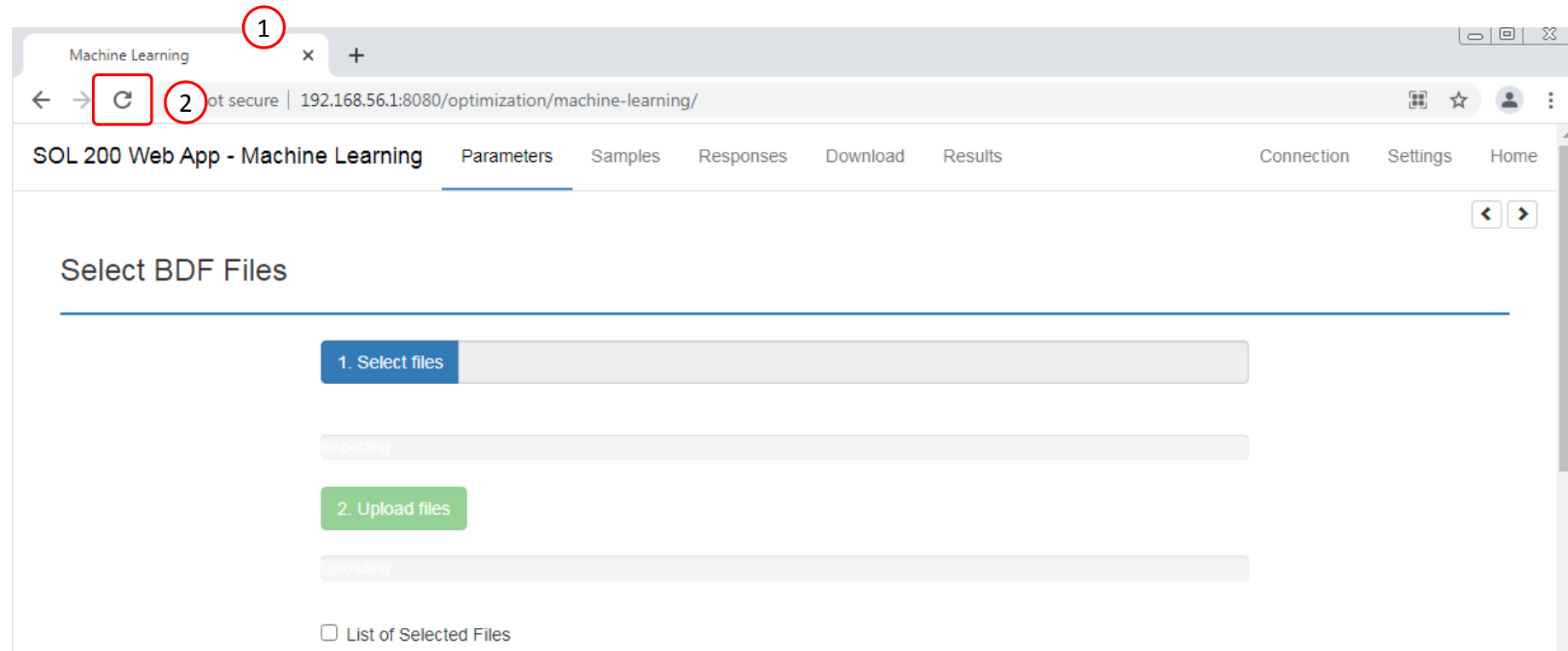
- app.config
- BDF files

These files may be imported back to the Machine Learning web app, and any parameters, samples and responses can be reconfigured

Import

1. Return to the window or tab that has the Machine Learning web app opened
2. Refresh the web page to start a new session

- Refreshing the page is only required when the *Select files* button is disabled.





Select BDF Files

1

1. Select files

3 files selected

Inspecting: 100%

5

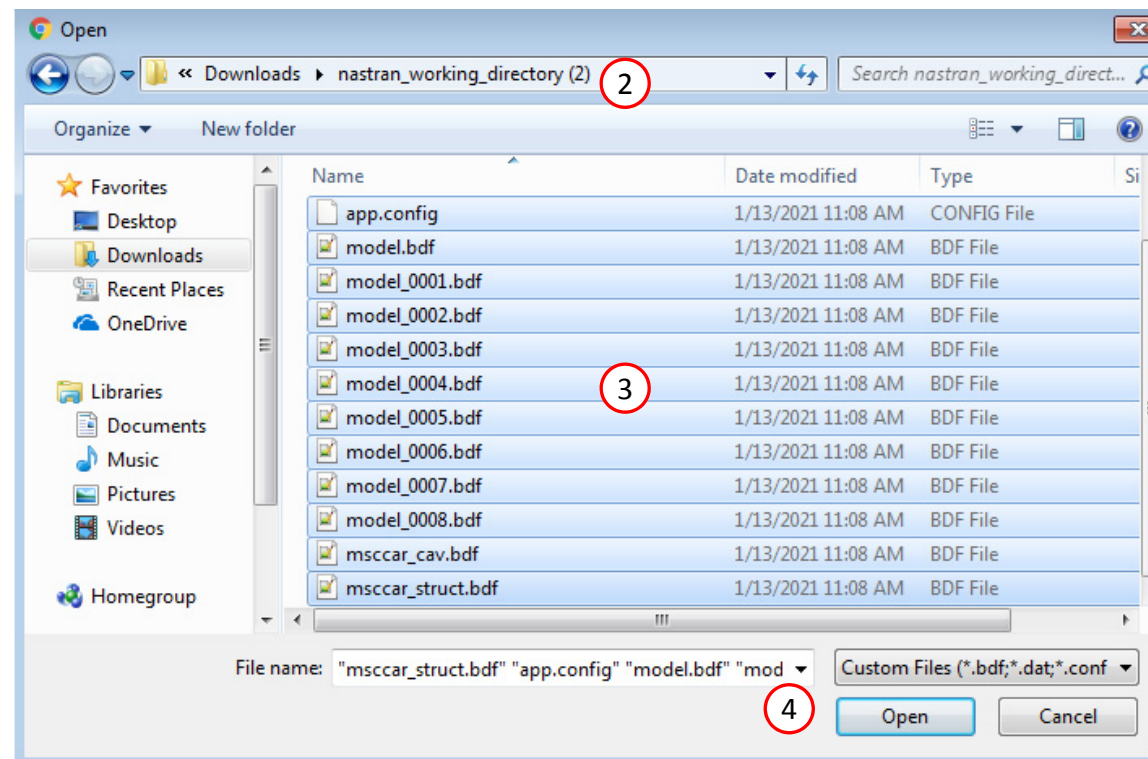
2. Upload files

Uploading

Import

1. Click Select Files
2. Navigate to the folder named nastran_working_directory (2)
3. Select all the BDF files AND the app.config file.
4. Click Open
5. Click Upload files

- All imports require the app.config file to be selected.



Import

For the Response section, the H5 file will need to be re-uploaded.

1. Click Responses
2. Select the H5 file
3. Click Upload
4. Data from the H5 is loaded and ready to use

SOL 200 Web App - Machine Learning Parameters Samples **Responses** Download Results Connection Settings Home

Upload .h5 File 1

2 1. Select files model.h5

3 2. Upload files

Select Responses to Monitor Session ID: 7429 HDF5

Select Dataset Acquired Dataset Reset Filters

View Responses to Monitor

Monitored Responses Hide/Show Columns Reset Filters Download CSV

| Delete | Label | Status | Objective | Lower Bound | Upper Bound | Monitor the response of the FINAL design cycle (SOL 200 only) | Monitor the response greater |
|--------|----------------------------|--------|-----------|-------------|-------------|---|------------------------------|
| | r1 r2 r3 r4 r5 | | | | | | NO YES |
| ✖ | r1 | ✓ | ▼ | Lower | Upper | ▼ | No - Monitor |
| ✖ | r2 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |
| ✖ | r3 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |
| ✖ | r4 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |
| ✖ | r5 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |

SOL 200 Web App - Machine Learning Parameters Samples **Responses** Download Results Connection Settings Home

Select Responses to Monitor Session ID: 7429 HDF5

Select Dataset Acquired Dataset Reset Filters

ACQUSTIC/PRESSURE_CPLX
NODAL/ACCELERATION_CPLX
NODAL/DISPLACEMENT_CPLX
NODAL/GRID_WEIGHT
NODAL/VELOCITY_CPLX
SUMMARY/ECOSYSTEM

Specify Entities
8667
Point ID (ID)
Examples: 8667, etc.
☒ Auto Execute
Acquire Dataset
✓ Acquisition complete and successful

ACQUSTIC/PRESSURE_CPLX - 8667

| ID | PR | PRMSR | DBR | DBAR |
|----------|-----------------------------|---------------------------------|-----------------------------------|------------------------------------|
| Point ID | Sound pressure level - real | RMS Sound pressure level - real | Sound pressure level in dB - real | Sound pressure level in dBA - real |
| 8667 | | 4 | | |
| 8667 | 1.07875096... | 7.62792125... | 74.51314112... | 4.24621661... |
| 8667 | 1.118924817... | 7.911993264... | 74.8173249... | 11.54942061... |
| 8667 | 1.17040290... | 8.27599833... | 75.1905549... | 16.7130260... |
| 8667 | 1.23496464... | 8.73251876... | 75.6346344... | 21.4036797... |
| 8667 | 1.31515638... | 9.29956000... | 76.1527769... | 25.8065989... |

View Responses to Monitor

Monitored Responses Hide/Show Columns Reset Filters Download CSV

| Delete | Label | Status | Objective | Lower Bound | Upper Bound | Monitor the response of the FINAL design cycle (SOL 200 only) | Monitor the response greater |
|--------|----------------------------------|--------|-----------|-------------|-------------|---|------------------------------|
| | r1 r2 r3 r4 r5 r6 | | | | | | NO YES |
| ✖ | r1 | ✓ | ▼ | Lower | Upper | ▼ | No - Monitor |
| ✖ | r2 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |
| ✖ | r3 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |
| ✖ | r4 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |
| ✖ | r5 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |
| ✖ | r6 | ✓ | ▼ | Lower | Upper | ▼ | Yes - Monitor |

Import

After import, any Parameter, Samples or Responses can be modified.



Select BDF Files

1. Select files

4 files selected

Inspecting: 100%

2. Upload files

Uploading: 100 %

☐ List of Selected Files

Select Parameters

| \$ _1 _ _2 _ _3 _ _4 _ _5 _ _6 _ _7 _ _8 _ _9 _ _10 _ | | | | | | | | | |
|---|--------|----------|------------------|-------|----------|-----|----------|--|--|
| EIGRL | 1 | | 225. | | | | | | |
| EIGRL | 2 | | 300. | | | | | | |
| FORCE | 212 | 1001 | | 500. | 0.0 | 1.0 | 0.0 | | |
| FORCE | 213 | 1001 | | 1000. | 0.0 | 0.0 | 1.0 | | |
| FORCE | 232 | 1003 | | 500. | 0.0 | 1.0 | 0.0 | | |
| FORCE | 233 | 1003 | | 1000. | 0.0 | 0.0 | 1.0 | | |
| FREQ1 | 5 | 10. | 2.5 | 56 | | | | | |
| MAT1 | 7 | 210000.0 | | 0.3 | 7.90E-06 | | | | |
| MAT1 | 8 | 62000.0 | | 0.24 | 2.30E-06 | | | | |
| MAT10 | 6 | | 1.23E-12340000.0 | | | | | | |
| PARAM | G | 0.06 | | | | | | | |
| PARAM | GFL | 0.12 | | | | | | | |
| PARAM | LFREQ | 0.1 | | | | | | | |
| PARAM | PREFDB | 2.E-11 | | | | | | | |
| PARAM | WTMASS | .001 | | | | | | | |
| PSHELL | 1 | 7 | %x1% | 7 | 1.0 | | 0.833333 | | |

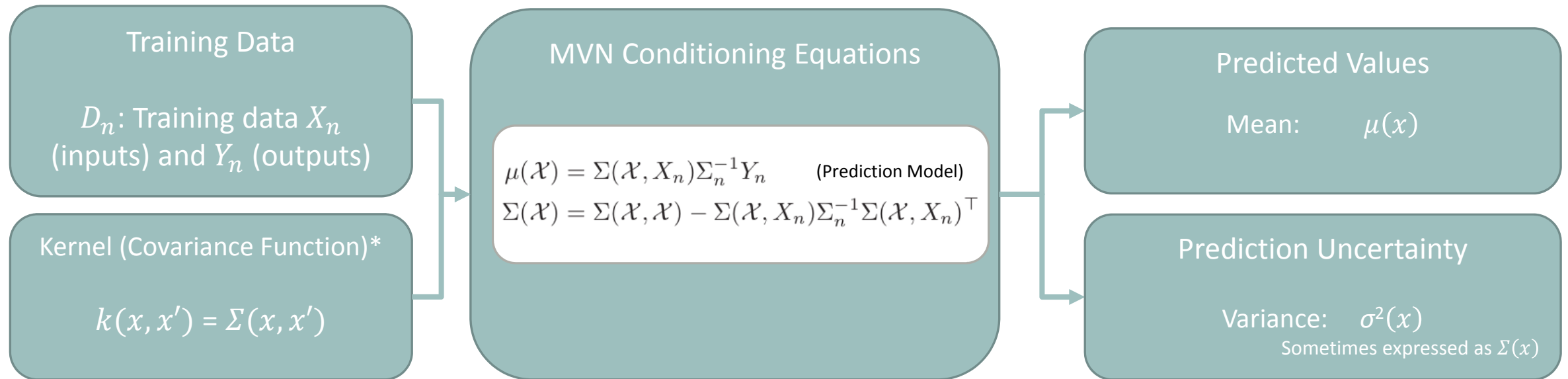


Configure Parameters

| Delete | Parameter | Status | Low | High | Comments |
|--------|-----------|--------|-----|------|-----------------|
| | x1 | | 1. | 6. | Field 4 of PSHE |
| | x2 | | 1. | 6. | Field 4 of PSHE |
| | x8 | | 1. | 6. | Field 4 of PSHE |
| | x11 | | 1. | 6. | Field 4 of PSHE |

What is Gaussian Process Regression?

Gaussian Process Regression Overview



* Hyperparameter optimization is part of the procedure but not covered in this presentation

** $\mu(x)$: This function corresponds to the mean function or kriging model. This function is the prediction model, also known as the surrogate model, meta model or emulator.

Multivariate Normal (MVN) Conditioning Equations

The following must be calculated: Covariance Matrix, Mean and Variance

Covariance Matrix

$$\Sigma = \begin{pmatrix} \Sigma(\chi, \chi) & \Sigma(\chi, X_n) \\ \Sigma(X_n, \chi) & \Sigma_n = \Sigma(X_n, X_n) \end{pmatrix}$$

X_n : Training locations
 χ : Testing (predictive) locations

Apply the covariance function $\Sigma(x, x')$ (kernel $k(x, x')$)

- $\Sigma(\chi, \chi)$: Covariance between testing (predictive) locations and themselves
- $\Sigma(\chi, X_n)$: Covariance between testing (predictive) and training locations
- $\Sigma(X_n, \chi)$: Covariance between training and testing (predictive) locations, which is the transpose of $\Sigma(\chi, X_n)$
- $\Sigma_n = \Sigma(X_n, X_n)$: Covariance between training locations and themselves

MVN Conditioning Equations (Mean and Variance)

Also referred to as “Gaussian process regression,” “kriging” or “kriging equations”

mean $\mu(\chi) = \Sigma(\chi, X_n) \Sigma_n^{-1} Y_n$ Prediction Model (Vary χ to make predictions)

and variance $\Sigma(\chi) = \Sigma(\chi, \chi) - \Sigma(\chi, X_n) \Sigma_n^{-1} \Sigma(X_n, \chi)^\top$ Prediction Uncertainty

Example 1

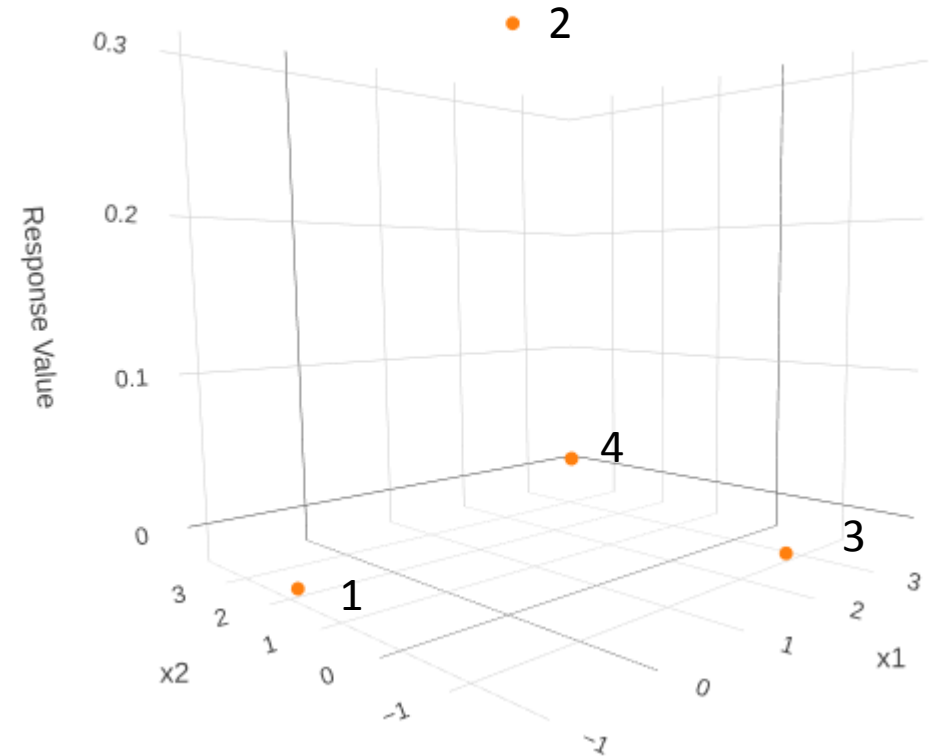
Example 1

Suppose a black box function was executed at 4 different samples (x1, x2 combinations)

With limited data (x and y), what does the response surface look like?

Training Data

| Sample | x1 | x2 | y |
|--------|-------|-------|-----------|
| 1 | -1.03 | 1.76 | -1.56E-02 |
| 2 | .49 | .49 | 3.04E-01 |
| 3 | 1.77 | -1.77 | 3.38E-03 |
| 4 | 3.62 | 3.76 | 5.43E-12 |



Training Data and Testing (Predictive) Locations

Suppose you have the following training data (X_n and Y_n) and testing locations (χ)

- X_n : The training design consists of 4 points
- χ : The test design (locations to make predictions) consists of 2 points

$$X = \begin{bmatrix} \chi \\ X_n \end{bmatrix} = \begin{bmatrix} .35 & .69 \\ .65 & .46 \\ -1.03 & 1.76 \\ .49 & .49 \\ 1.77 & -1.77 \\ 3.62 & 3.76 \end{bmatrix}$$

$$\begin{bmatrix} y^* \\ Y_n \end{bmatrix} = \begin{bmatrix} ? \\ ? \\ -1.56e-02 \\ 3.04e-01 \\ 3.38e-03 \\ 5.43e-12 \end{bmatrix}$$

The goal is make predictions (y^*) for points in χ

Note

- X_n : inputs of the training data
- Y_n : outputs of the training data
- χ or x : inputs of the testing data (predictive locations, i.e. points to make predictions)
- y^* : predicted outputs
- D_n : Training data X_n and Y_n

X : upper case of Greek letter chi (pronounced kai in English)
 χ : lower case of Greek letter chi

Calculation of the Covariance Matrix

1. Select a covariance (kernel) function

- Many covariance functions (kernels) exist: Radial Basis Function (RBF), Matern 5/2, 3/2, Exponential, ...
- For this example, a form of the RBF covariance function is used. This covariance function is described as the “inverse exponentiated squared Euclidean distance”

$$k(x, x') = \Sigma(x, x') = \exp\{-\|x - x'\|^2\} = e^{-\|x - x'\|^2}$$

2. Calculate D (Distance Matrix)

$$D = \|X - X\|^2 \quad \text{“Norm between } X \text{ and } X, \text{ squared”}$$

3. Calculate Σ (Covariance Matrix)

$$\Sigma = e^{-D}$$

Calculation of D

$D =$

| | | | | | |
|---|---|---|---|---|--|
| $\sqrt{(.35 - .35)^2 + (.69 - .69)^2}$ = 0 | $\sqrt{(.35 - .65)^2 + (.69 - .46)^2}$ = .1429 | $\sqrt{(.35 - -1.03)^2 + (.69 - 1.76)^2}$ = 3.0493 | $\sqrt{(.35 - .49)^2 + (.69 - .49)^2}$ = .0596 | $\sqrt{(.35 - 1.77)^2 + (.69 - -1.77)^2}$ = 8.068 | $\sqrt{(.35 - 3.62)^2 + (.69 - 3.76)^2}$ = 20.1178 |
| .1429 | $\sqrt{(.65 - .65)^2 + (.46 - .46)^2}$ = 0 | $\sqrt{(.65 - -1.03)^2 + (.46 - 1.76)^2}$ = 4.5124 | $\sqrt{(.65 - .49)^2 + (.46 - .49)^2}$ = .0265 | $\sqrt{(.65 - 1.77)^2 + (.46 - -1.77)^2}$ = 6.2273 | $\sqrt{(.65 - 3.62)^2 + (.46 - 3.76)^2}$ = 19.7109 |
| 3.0493 | 4.5124 | $\sqrt{(-1.03 - -1.03)^2 + (1.76 - 1.76)^2}$ = 0 | $\sqrt{(-1.03 - .49)^2 + (1.76 - .49)^2}$ = 3.9233 | $\sqrt{(-1.03 - 1.77)^2 + (1.76 - -1.77)^2}$ = 20.3009 | $\sqrt{(-1.03 - 3.62)^2 + (1.76 - 3.76)^2}$ = 25.6225 |
| .0596 | .0265 | 3.9233 | $\sqrt{(.49 - .49)^2 + (.49 - .49)^2}$ = 0 | $\sqrt{(.49 - 1.77)^2 + (.49 - -1.77)^2}$ = 6.746 | $\sqrt{(.49 - 3.62)^2 + (.49 - 3.76)^2}$ = 20.4898 |
| 8.068 | 6.2273 | 20.3009 | 6.746 | $\sqrt{(1.77 - 1.77)^2 + (-1.77 - -1.77)^2}$ = 0 | $\sqrt{(1.77 - 3.62)^2 + (-1.77 - 3.76)^2}$ = 34.0034 |
| 20.1178 | 19.7109 | 25.6225 | 20.4898 | 34.0034 | $\sqrt{(3.62 - 3.62)^2 + (3.76 - 3.76)^2}$ = 0 |

Calculation of Σ

$$\Sigma = \begin{bmatrix} e^0 = 1 & e^{-.1429} = .8668 & e^{-3.0493} = .0474 & e^{-.0596} = .9421 & e^{-8.068} = .0003 & e^{-20.1178} = 1.832e-9 \\ .8668 & e^0 = 1 & e^{-4.5124} = .0110 & e^{-.0265} = .9738 & e^{-6.2273} = .0020 & e^{-19.7109} = 2.8e-9 \\ .0474 & .0110 & e^0 = 1 & e^{-3.9233} = .0198 & e^{-20.3009} = 1.5e-9 & e^{-25.6225} = 7.5e-12 \\ .9421 & .9738 & .0198 & e^0 = 1 & e^{-6.746} = .0012 & e^{-20.4898} = 1.263e-9 \\ .0003 & .0020 & 1.5e-9 & .0012 & e^0 = 1 & e^{-34.0034} = 1.7e-15 \\ 1.832e-9 & 2.8e-9 & 7.5e-12 & 1.263e-9 & 1.7e-15 & e^0 = 1 \end{bmatrix}$$

Calculation of Σ

$\Sigma =$

$$\Sigma(\chi, \chi)$$

| | |
|-----------|----------------------|
| $e^0 = 1$ | $e^{-.3429} = .8668$ |
| .8668 | $e^0 = 1$ |

$$\Sigma(\chi, X_n)$$

| | | | |
|-----------------------|----------------------|-----------------------|---------------------------|
| $e^{-3.0493} = .0474$ | $e^{-.0596} = .9421$ | $e^{-8.068} = .0003$ | $e^{-20.1178} = 1.832e-9$ |
| $e^{-4.5124} = .0110$ | $e^{-.0265} = .9738$ | $e^{-6.7273} = .0020$ | $e^{-19.7109} = 2.8e-9$ |

$$\Sigma(X_n, \chi)$$

| | |
|----------|--------|
| .0474 | .0110 |
| .9421 | .9738 |
| .0003 | .0020 |
| 1.832e-9 | 2.8e-9 |

$$\Sigma_n = \Sigma(X_n, X_n)$$

| | | | |
|-----------|-----------------------|-------------------------|---------------------------|
| $e^0 = 1$ | $e^{-3.9233} = .0198$ | $e^{-20.3009} = 1.5e-9$ | $e^{-25.6225} = 7.5e-12$ |
| .0198 | $e^0 = 1$ | $e^{-6.746} = .0012$ | $e^{-20.4898} = 1.263e-9$ |
| 1.5e-9 | .0012 | $e^0 = 1$ | $e^{-34.0034} = 1.7e-15$ |
| 7.5e-12 | 1.263e-9 | 1.7e-15 | $e^0 = 1$ |

Since Σ is symmetric, note that $\Sigma(X_n, \chi) = \Sigma(\chi, X_n)^T$

Calculation of Predictive Quantities

The MVN conditioning equations are used to determine the predictive quantities mean and variance

mean $\mu(\mathcal{X}) = \Sigma(\mathcal{X}, X_n) \Sigma_n^{-1} Y_n$

$$\mu(\chi) = y * = \begin{pmatrix} 0.2849657 \\ 0.2954011 \end{pmatrix} \quad \text{Predicted values for locations in } \chi$$

and variance $\Sigma(\mathcal{X}) = \Sigma(\mathcal{X}, \mathcal{X}) - \Sigma(\mathcal{X}, X_n) \Sigma_n^{-1} \Sigma(\mathcal{X}, X_n)^\top$

$$\Sigma(\chi) = \begin{pmatrix} 0.11154162 & -0.05042265 \\ -0.05042265 & 0.05155061 \end{pmatrix} \quad \text{Prediction Uncertainty}$$

The diagonal terms are the variances at prediction points 1 and 2

$$\sigma^2(\chi) = \begin{pmatrix} 0.11154162 \\ 0.05155061 \end{pmatrix}$$

R

Code to replicate this example in R

```
library(plgp)

eps = sqrt(.Machine$double.eps)

# Training points
X = rbind(c(-1.03,1.76), c(.49,.49), c(1.77,-1.77), c(3.62,3.76))

# The goal is to fit this function:  $y(x) = x_1 * \exp(-x_1^2 - x_2^2)$ 
y = X[,1] * exp(-X[,1]^2 - X[,2]^2)

# Test points
XX = rbind(c(.35, .69), c(.65, .46))
XX

# Sigma 22 (Sigma) and its inverse (Si)
# #####
# Distance among the Training Data
D = distance(X)
Sigma = exp(-D)
Si = solve(Sigma)

# Sigma 11
# #####
# Distance among the Testing Data
DXX = distance(XX)
SXX = exp(-DXX)

# Sigma 12 and Sigma 21 (Transpose of Sigma 12)
# #####
# Distance between training and testing data
```

```
DX = distance(XX, X)
SX = exp(-DX)

# Calculate the predictive mean and predictive variance
# #####
# Predictive mean
mup = SX %*% Si %*% y
mup

# Predictive variance
Sigmap = SXX - SX %*% Si %*% t(SX)
Sigmap
```

Output

```
> # #####
> # Predictive mean
> mup = SX %*% Si %*% y
> mup
      [,1]
[1,] 0.2849657
[2,] 0.2954011
>
> # Predictive variance
> Sigmap = SXX - SX %*% Si %*% t(SX)
> Sigmap
      [,1] [,2]
[1,] 0.11154162 -0.05042265
[2,] -0.05042265 0.05155061
> |
```


R

Code to replicate this example in R with Plots

```
library(plgp)
library(lhs)

eps = sqrt(.Machine$double.eps)

# Training Data
# #####
# Training points
number_of_sample_points = 4
X = rbind(c(-1.03,1.76), c(.49,.49), c(1.77,-1.77), c(3.62,3.76))

# Observed values
# The goal is to fit this function:  $y(x) = x_1 * \exp(-x_1^2 - x_2^2)$ 
y = X[,1] * exp(-X[,1]^2 - X[,2]^2)

# Testing Data
# #####
# Test points
number_of_test_points_per_axis = 40
xx = seq(-2, 4, length=number_of_test_points_per_axis)
XX = expand.grid(xx, xx)

# Sigma 22 (Sigma) and its inverse (Si)
# #####
# Distance among the Training Data
D = distance(X)
Sigma = exp(-D) + diag(eps, nrow(X))
Si = solve(Sigma)

# Sigma 11
# #####
# Distance among the Testing Data
```

```
DXX = distance(XX)
SXX = exp(-DXX)

# Sigma 12 and Sigma 21 (Transpose of Sigma 12)
# #####
# Distance between training and testing data
DX = distance(XX, X)
SX = exp(-DX)

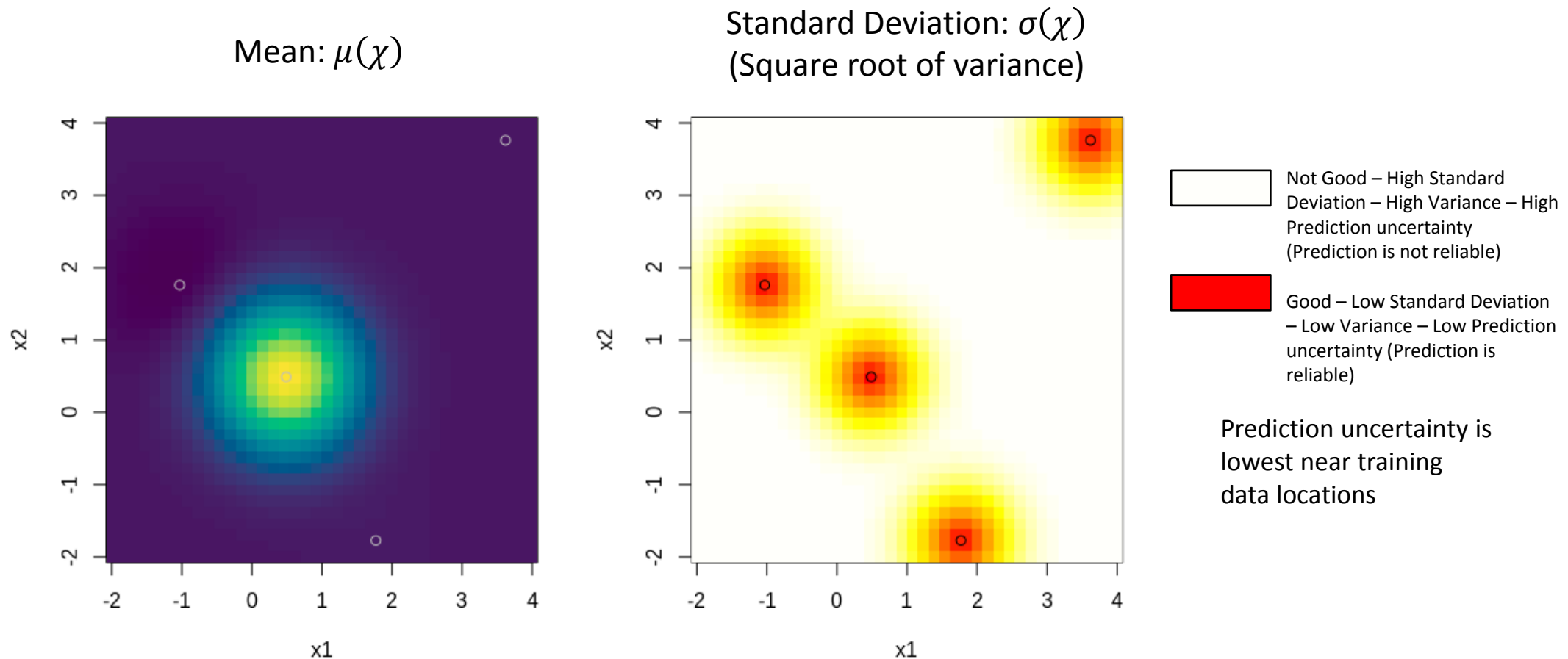
# Calculate the predictive mean and predictive variance
# #####
mup = SX %*% Si %*% y
Sigmap = SXX - SX %*% Si %*% t(SX)

# Predictive standard deviation
diag(Sigmap)
sdp = sqrt(diag(Sigmap))

# Figure 5.5
par(mfrow=c(1, 2))
cols_a = hcl.colors(128, palette = "viridis")
cols_b = heat.colors(128)
image(xx, xx, matrix(mup, ncol=length(xx)), xlab='x1', ylab='x2', col=cols_a)
points(X[,1], X[,2])
image(xx, xx, matrix(sdp, ncol=length(xx)), xlab='x1', ylab='x2', col=cols_b)
points(X[,1], X[,2])

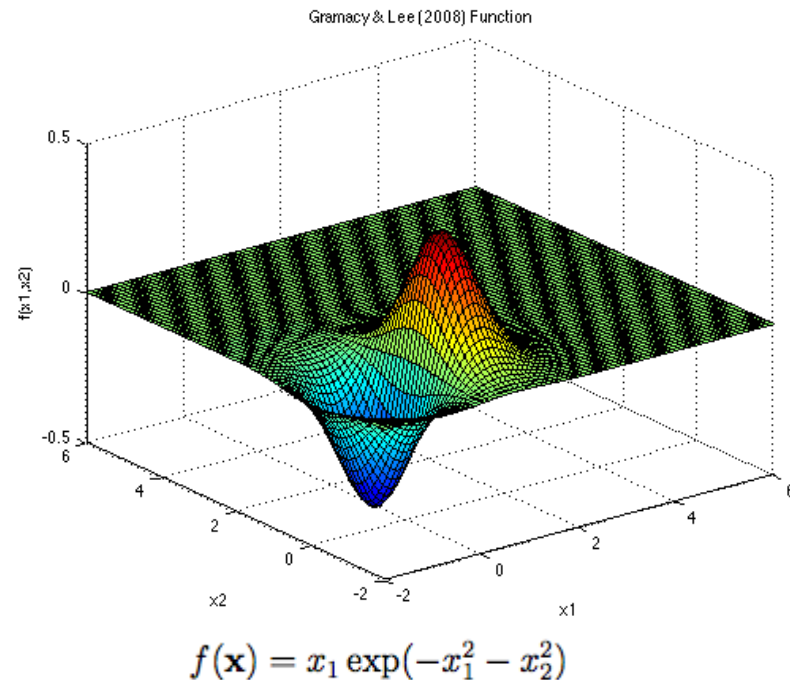
# Figure 5.6
persp(xx, xx, matrix(mup, ncol=number_of_test_points_per_axis), theta=-30, phi=30,
xlab='x1', ylab='x2', zlab='y', zlim = c(-.5,.5))
```

Predictive Quantities Mean and Standard Deviation



Comparison of True Function and Prediction Model

True Function



Source: <https://www.sfu.ca/~ssurjano/grlee08.html>

Prediction Model ($\mu(\chi)$)

