MSC Nastran Topology Optimization - Multidiscipline - Static Loading and Natural Frequency

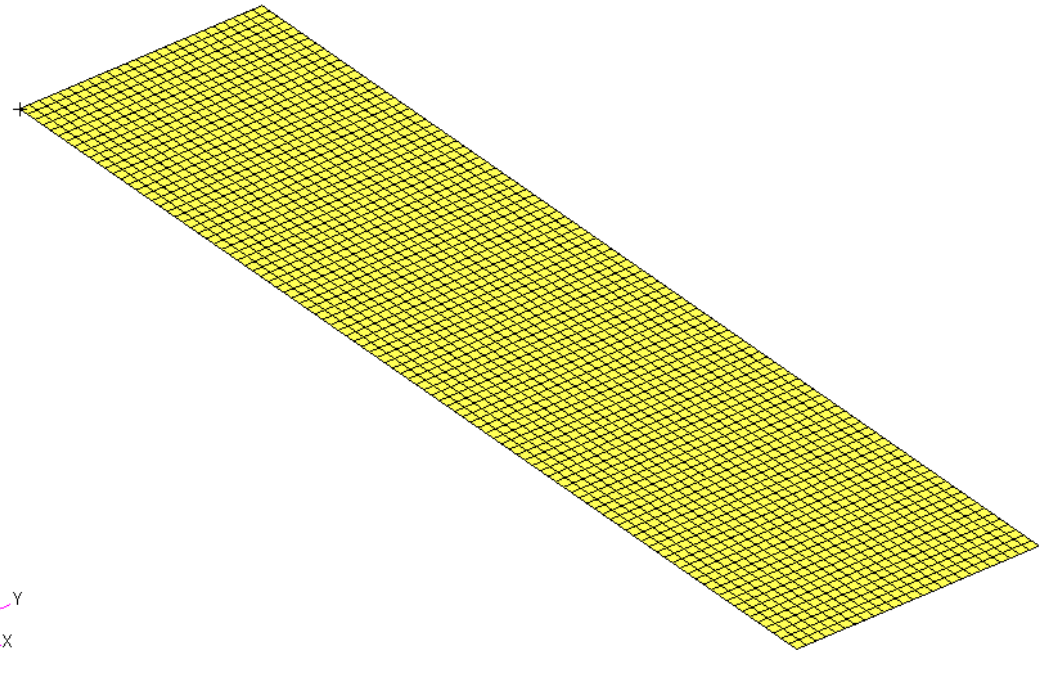
AN MSC NASTRAN SOL 200 TUTORIAL

Questions? Email: christian@ the-engineering-lab.com

Goal: Use Nastran SOL 200 Optimization

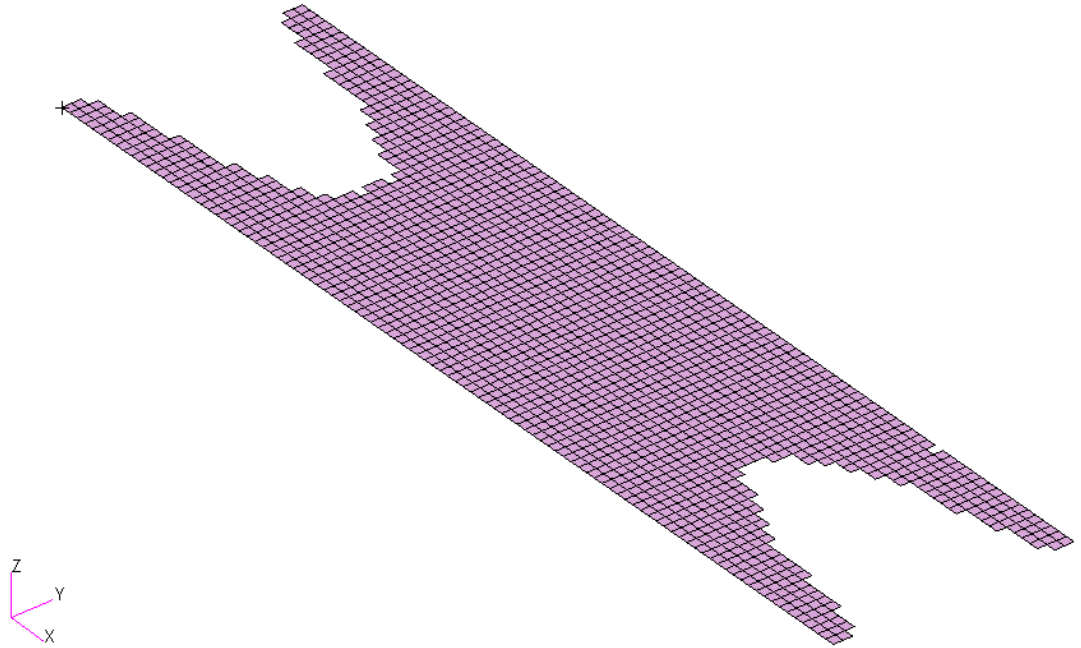
Before Optimization

- Mass: 9.73E-06

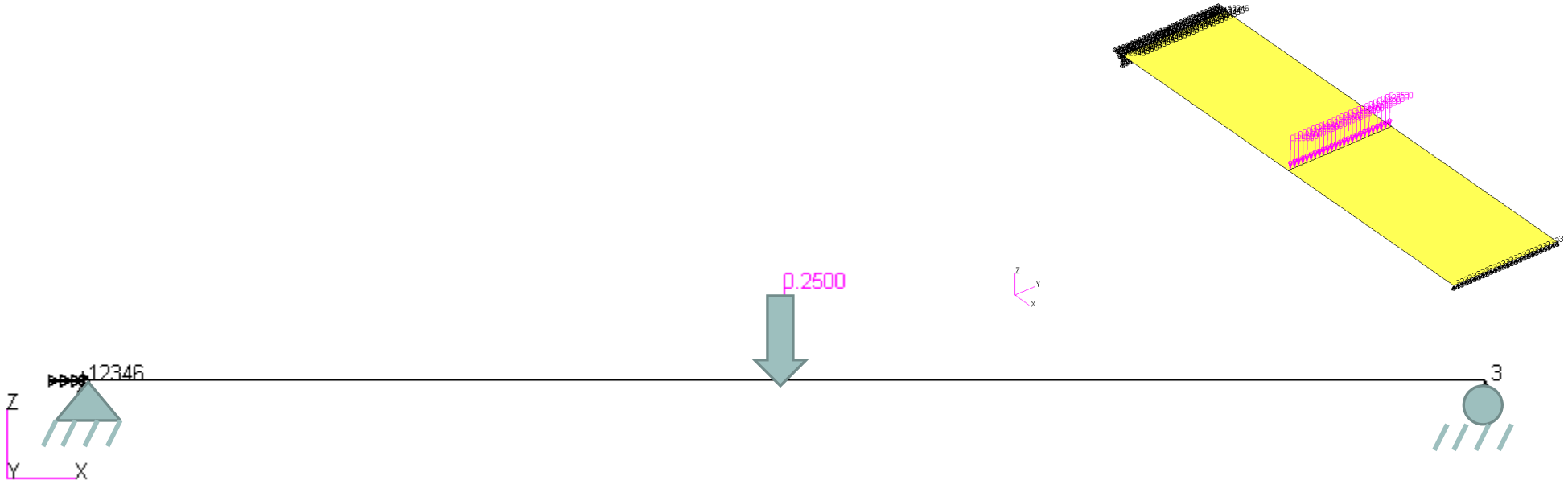


After Optimization

- Mass: 7.05E-06 (~25% mass reduction)
- Maximize stiffness
- Maximize first natural frequency



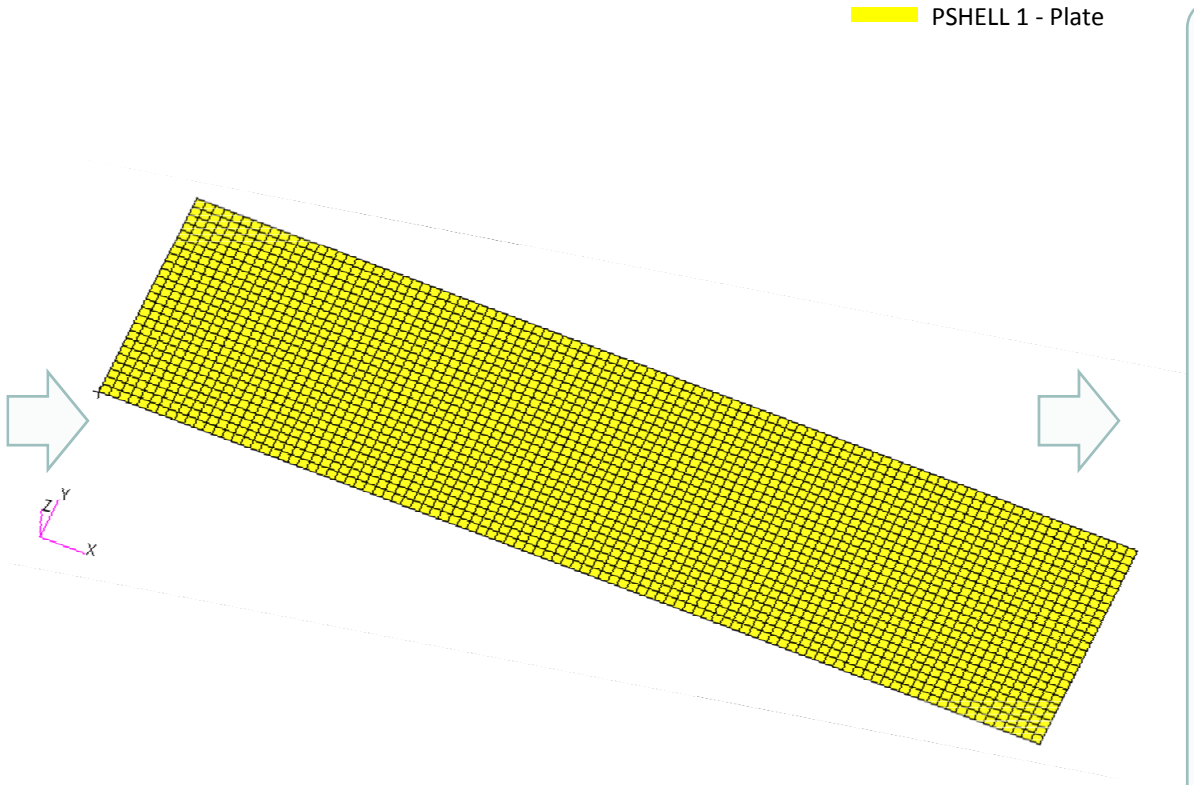
Details of the structural model



Optimization Problem Statement

Design Region/Variables

x1: PSHELL 1



Design Equation Objective

R0: Minimize the sum of normalized compliance and normalized natural frequency

$$R0 = \frac{a1}{36.7} + \frac{86.4}{a2}$$

a1: Compliance of SUBCASE 1
a2: Natural frequency of mode 1 of SUBCASE 2

Design Constraints

r1: Fractional mass

r1 < .75 (25% mass reduction)

r2: The z component of displacement at node 714

-5.0 < r2

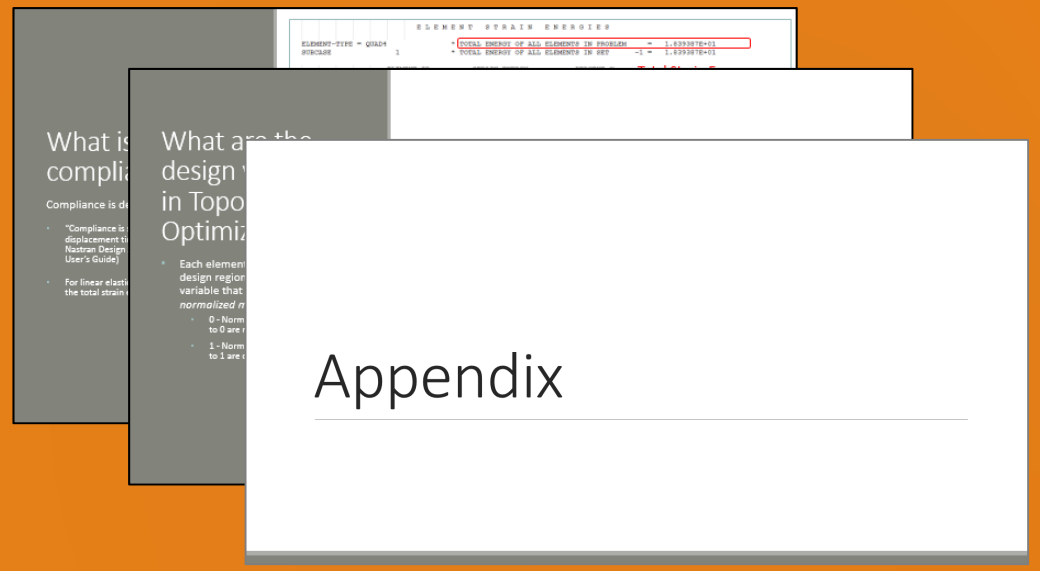
r3: The natural frequency of mode 1

20 < r3

More Information Available in the Appendix

The Appendix includes information regarding the following:

- Frequently Asked Questions
  - What are the design variables in Topology Optimization?
  - What is FRMASS or Fractional Mass?
  - What is compliance?
  - How can non-critical elements be removed from the design?
- Topology Optimization Workflows
- Viewer Web App for Topology Optimization Post Processing



Contact me

- Nastran SOL 200 training
- Nastran SOL 200 questions
- Structural or mechanical optimization questions
- Access to the SOL 200 Web App

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Tutorial

Tutorial Overview

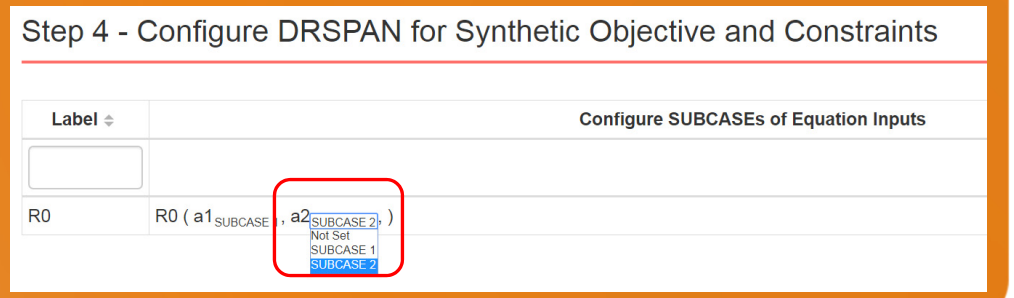
1. Start with a .bdf or .dat file
2. Use the SOL 200 Web App to:
   - Convert the .bdf file to SOL 200
     - Design Regions/Variables
     - Design Objective
     - Design Constraints
   - Perform optimization with Nastran SOL 200
3. Review optimization results
   - .f06
   - Topology Optimization and Structural Results

Special Topics Covered

Multidiscipline Optimization - This example is optimizing for static analysis and normal modes analysis.

Equation Objective with SUBCASE spanning responses - The Equation Objective defined in this example is dependent on responses from multiple SUBCASEs. The a1 response comes from SUBCASE 1 and a2 comes from SUBCASE 2. The use of DRSPAN enables the specification of which SUBCASEs produces the necessary values.

$$R0 = \frac{a1}{36.7} + \frac{86.4}{a2}$$

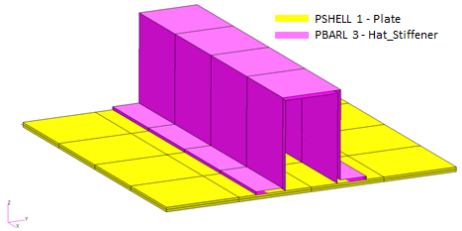


SOL 200 Web App Capabilities

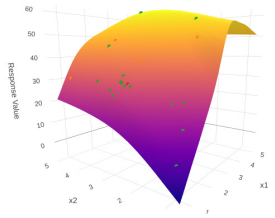
Benefits

- 200+ error validations (real time)
- Web browser accessible
- Automated creation of entries (real time)
- Automatic post-processing
- 76 tutorials

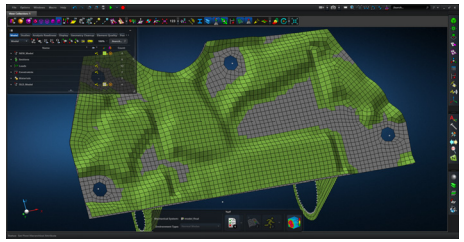
Capabilities



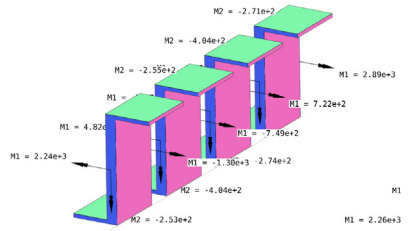
Web Apps for SOL 200
Pre/post for MSC Nastran SOL 200. Support for size, topology, topometry, topography and multi-model.



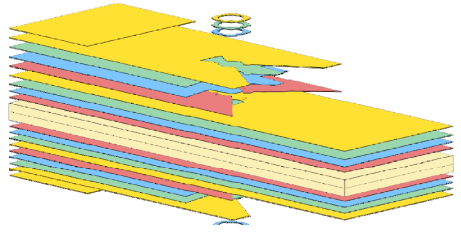
Machine Learning Web App
Bayesian Optimization for nonlinear response optimization (SOL 400)



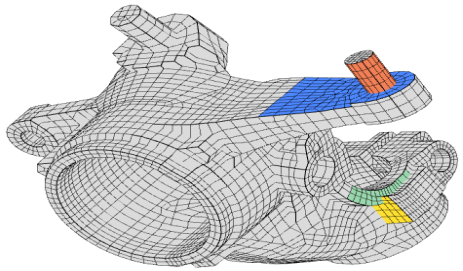
MSC Apex Post Processing Support
View the newly optimized model after an optimization



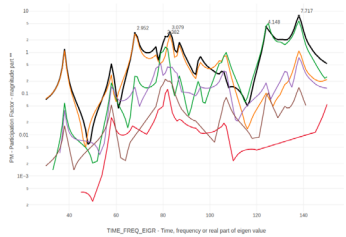
Beams Viewer Web App
Post process 1D element forces, including shear forces, moments, torque and axial forces



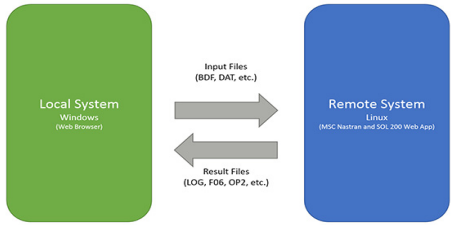
Ply Shape Optimization Web App
Spread plies optimally and generate new PCOMPG entries



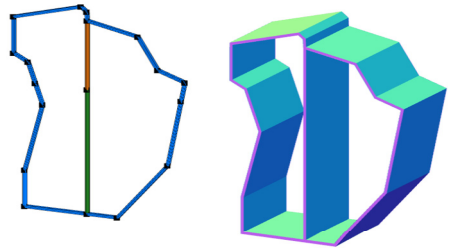
Shape Optimization Web App
Use a web application to configure and perform shape optimization.



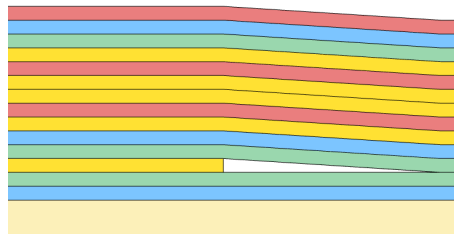
HDF5 Explorer Web App
Create XY plots using data from the H5 file



Remote Execution Web App
Run MSC Nastran jobs on remote Linux or Windows systems available on the local network



PBMSECT Web App
Generate PBMSECT and PBRSECT entries graphically

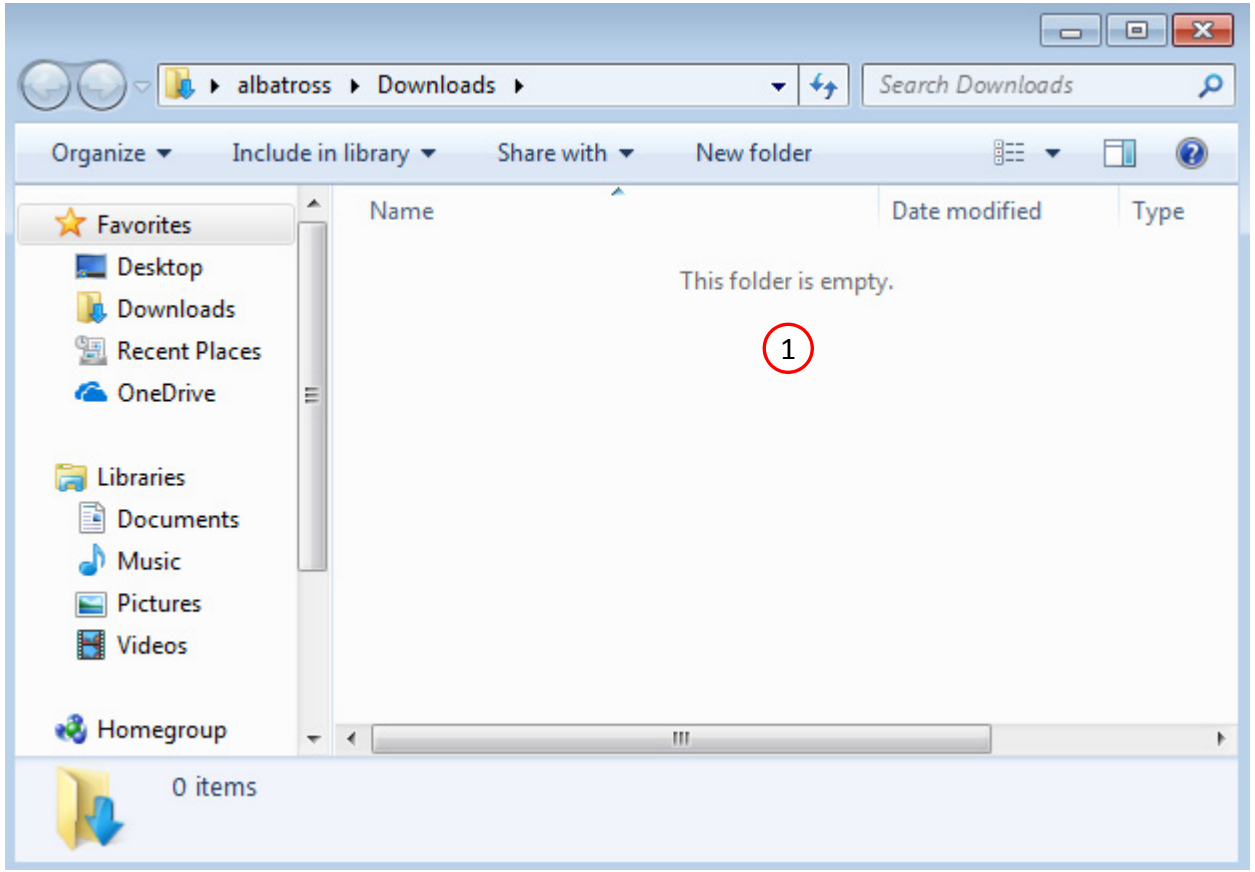


Stacking Sequence Web App
Optimize the stacking sequence of composite laminate plies

Before Starting

1. Ensure the Downloads directory is empty in order to prevent confusion with other files

- Throughout this workshop, you will be working with multiple file types and directories such as:
  - .bdf/.dat
  - nastran_working_directory
  - .f06, .log, .pch, .h5, etc.
- To minimize confusion with files and folders, it is encouraged to start with a clean directory.



Go to the User's Guide

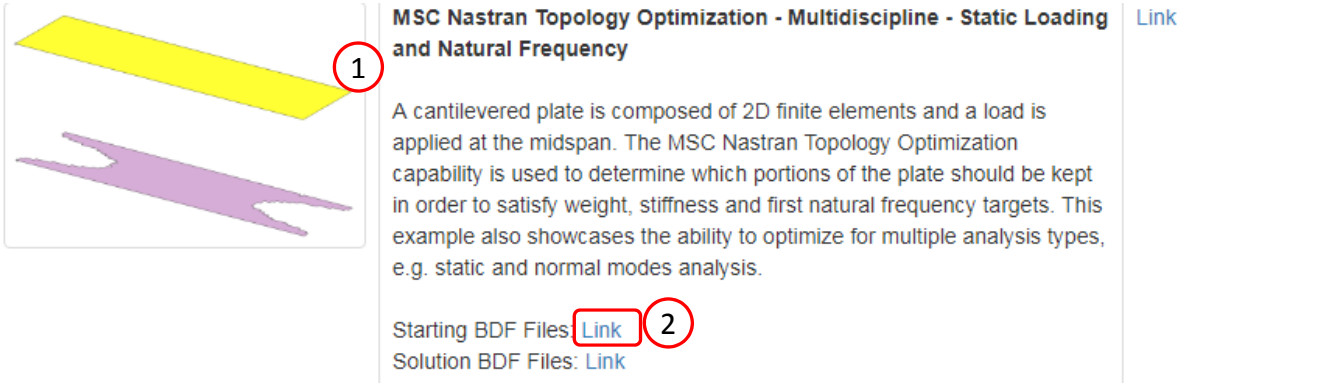
1. Click on the indicated link

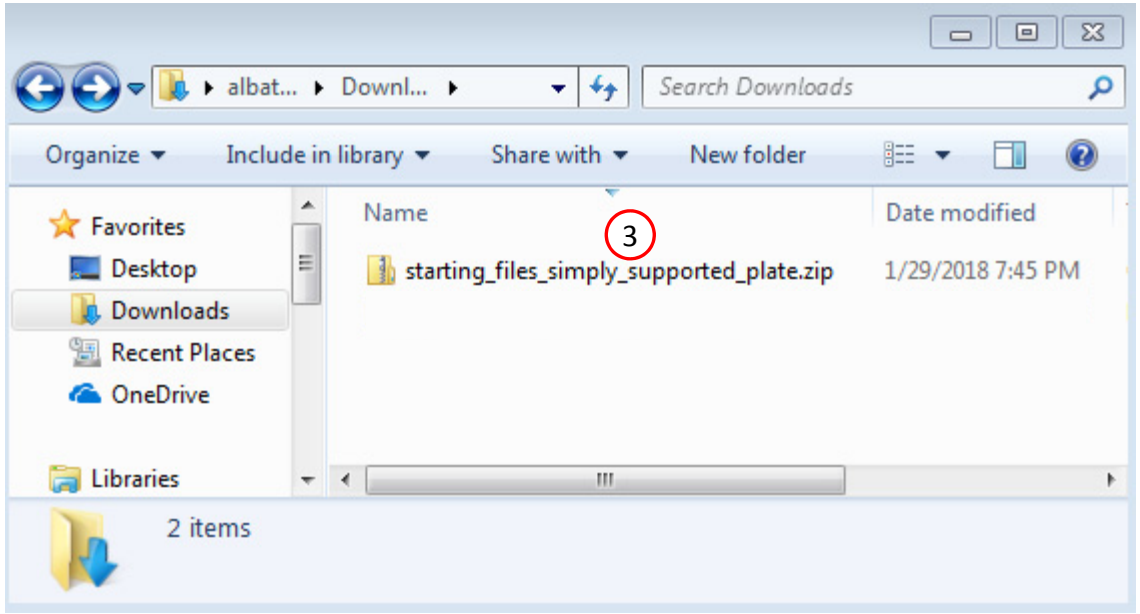
- The necessary BDF files for this tutorial are available in the Tutorials section of the User's Guide.

Obtain Starting Files

1. Find the indicated example
2. Click Link
3. The starting file has been downloaded

- When starting the procedure, all the necessary BDF files must be collected together.

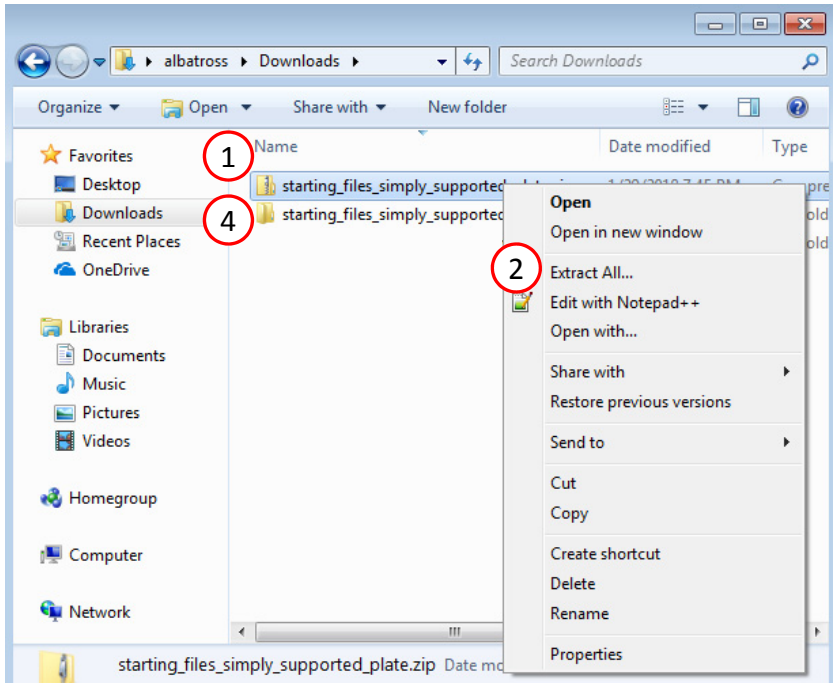


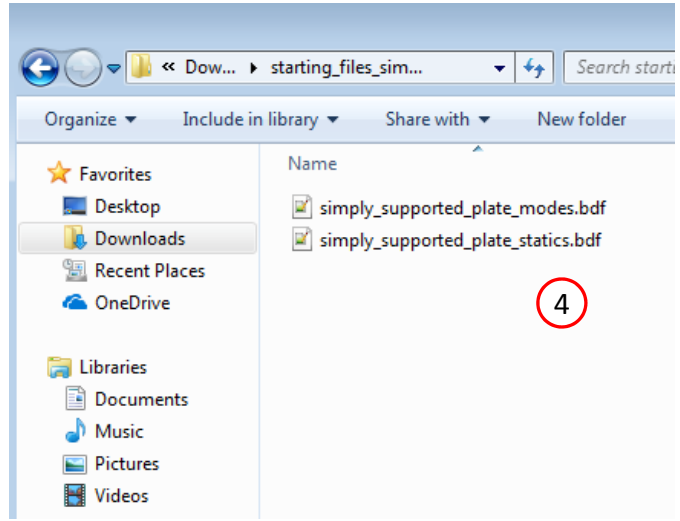


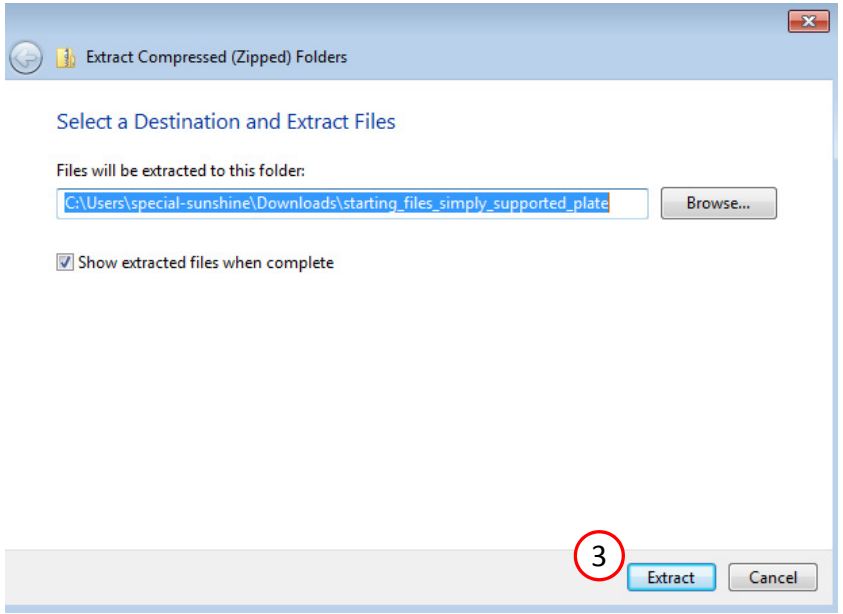
Obtain Starting Files

1. Right click on the zip file
2. Select Extract All…
3. Click Extract
4. The starting files are now available in a folder

- This example is using a previously created design model. The design model is a model that has been converted to SOL 200 and contains bulk data entries describing the optimization problem statement, e.g. variables, objective and constraints.







Merge the BDF files

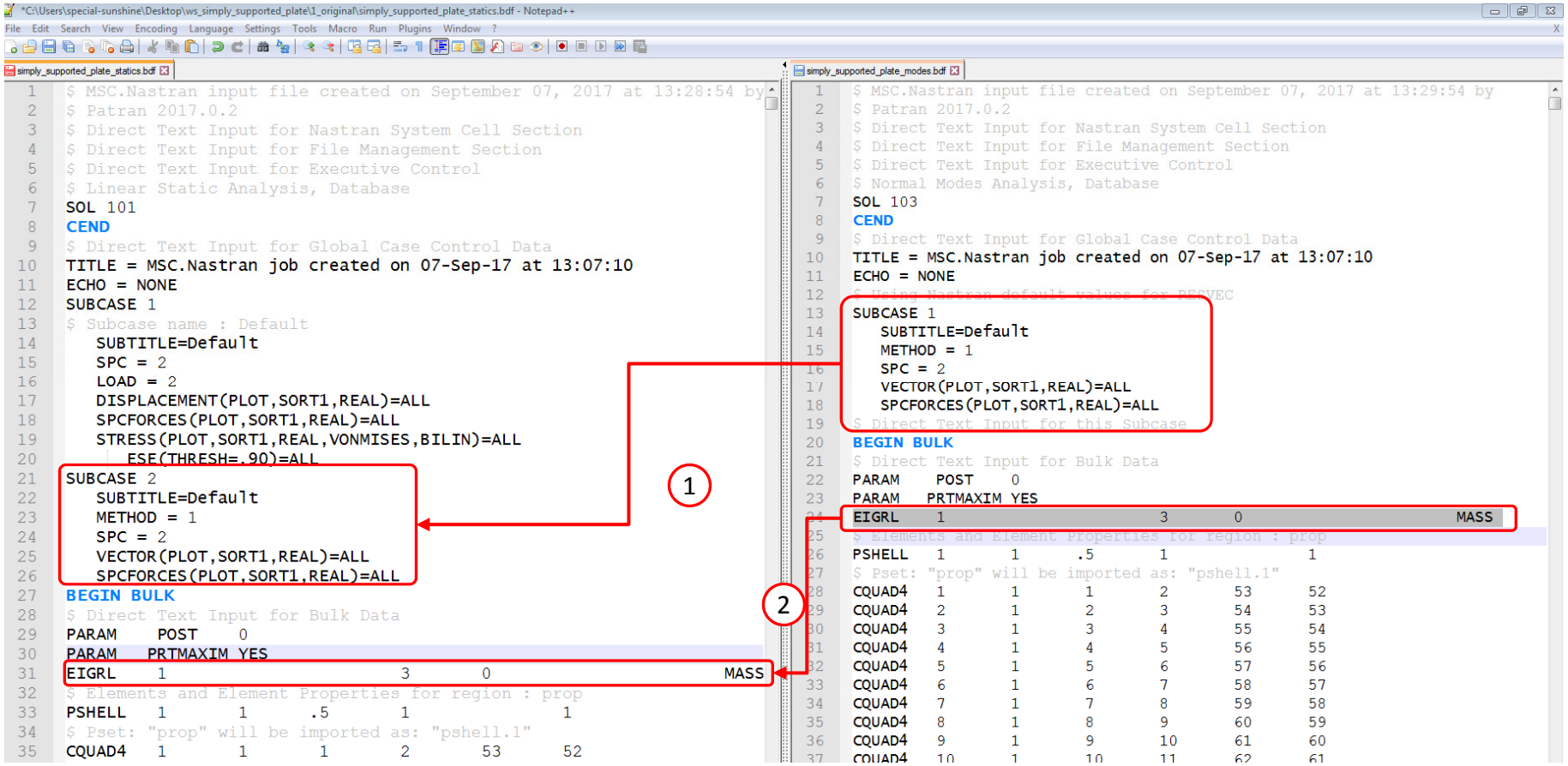
There are two separate BDF files. Both files contain the simply supported plate. One BDF file is configured to perform a Linear Static analysis. The second BDF file is configured to perform a Normal Modes Analysis. To perform an optimization for both static and normal modes analysis, the files must be combined.

1. Open *simply_supported_plate_modes.bdf*. Take SUBCASE 1 and move it to *simply_supported_plate_statics.bdf*. Rename SUBCASE 1 to SUBCASE 2 to avoid duplicate SUBCASEs.

2. Take the line with EIGRL at the beginning and move it to *simply_supported_plate_statics.bdf*

3. Save *simply_supported_plate_statics.bdf* as *simply_supported_plate_combined.bdf (Not shown)*

- In this tutorial a Multidisciplinary Optimization is performed. This is done by:
  1. Merging the BDF files
  2. Adding different ANALYSIS commands to each SUBCASE.



Open the Correct Page

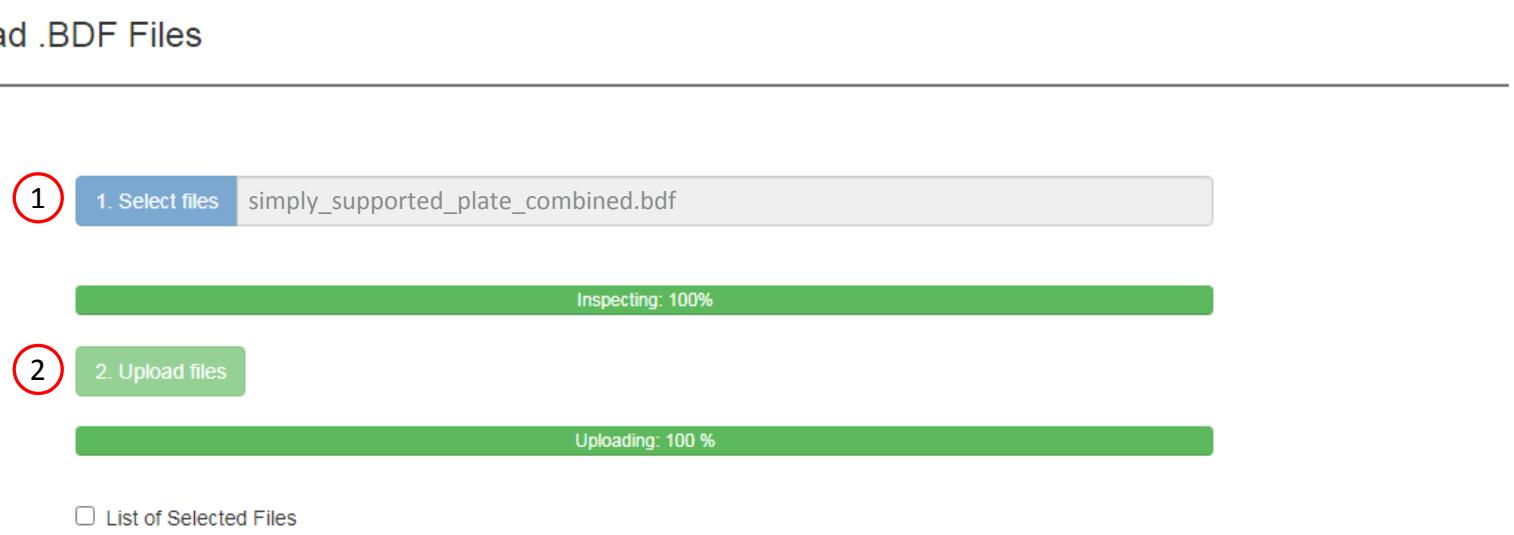
1. Click on the indicated link

- MSC Nastran can perform many optimization types. The SOL 200 Web App includes dedicated web apps for the following:
  - Optimization for SOL 200 (Size, Topology, Topometry, Topography, Local Optimization, Sensitivity Analysis and Global Optimization)
  - Multi Model Optimization
  - Machine Learning
- The web app also features the HDF5 Explorer, a web application to extract results from the H5 file type.

Upload BDF Files

1. Click 1. Select Files and select simply_supported_plate_combined.bdf
2. Click Upload Files

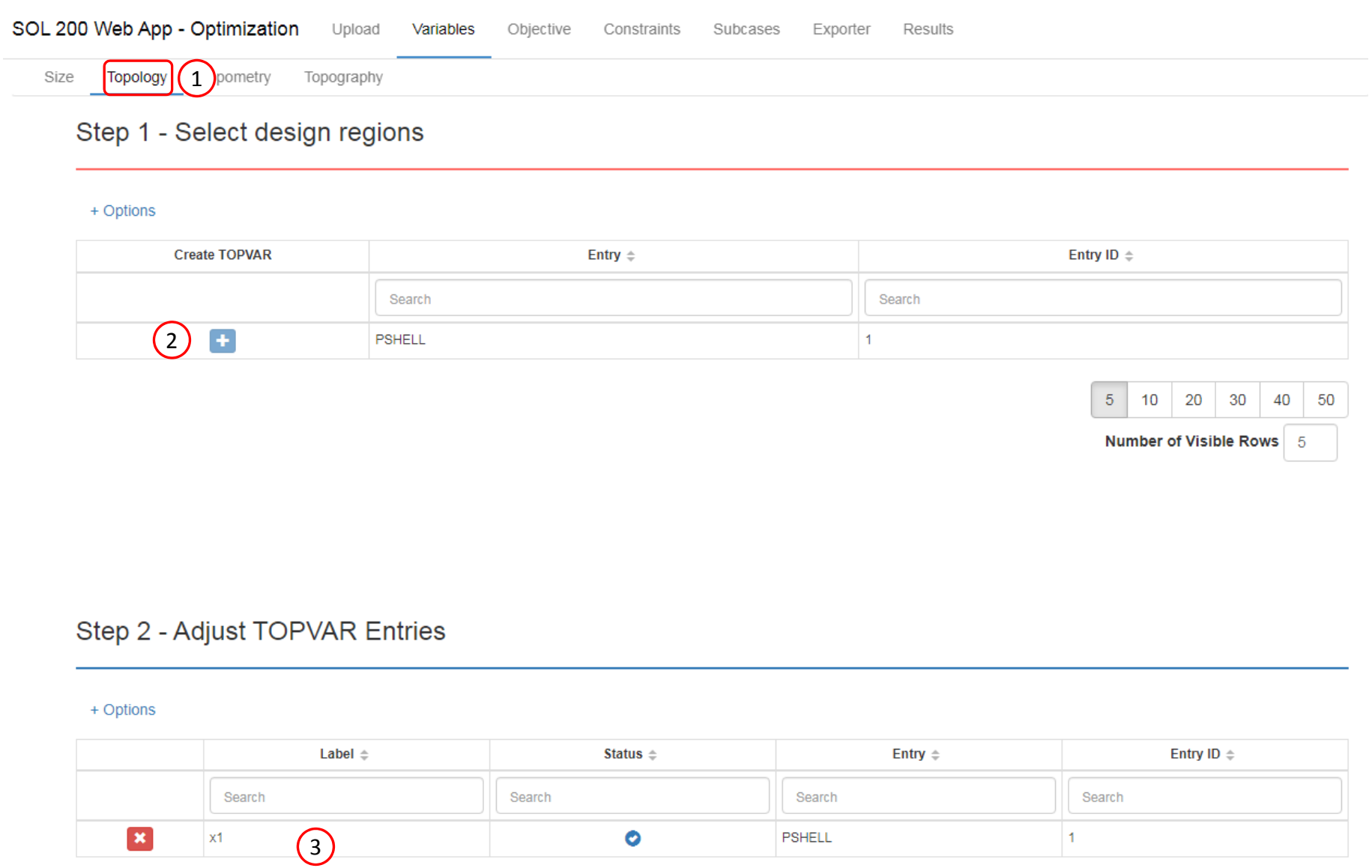
- The process starts by uploading all the necessary BDF files. The BDF files can be files of your own or files found in the Tutorials section of the User's Guide.



Create Design Region

1. Click Topology
2. Click on the plus (+) icons to set PSHELL 1 as a Design Region
3. The Design Region is displayed in the next table. Any element associated with PSHELL 1 will be allowed to change during the optimization.

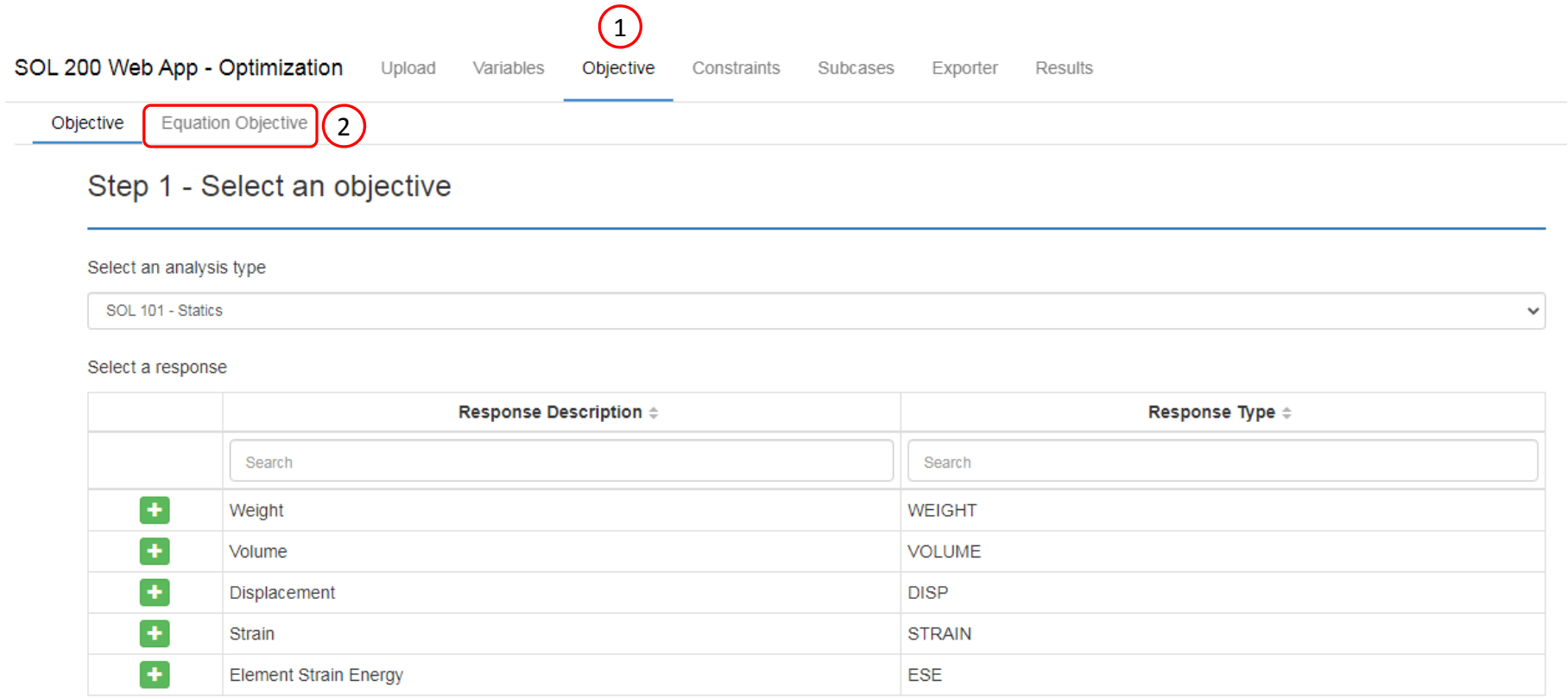
- In traditional Size optimization, individual design variables are created. It is slightly different for Topology optimization. When a design region is set, each element in the design region has a design variable created for it. Each design variable corresponds to the Normalized Material Density of that element, see the appendix for additional details.
- If PSHELL 1 has 500 elements associated and is configured as a design region, then there will be 500 design variables created.
- Each step has hidden functionality for advanced users. The visibility is controlled by clicking + Options.
- If the property entry, e.g. PSHELL, was given a name in Patran, e.g. Car Door, the name can be shown by marking the checkbox titled Entry Name.



Create Design Objective

1. Click on Objective
2. Click on Equation Objective

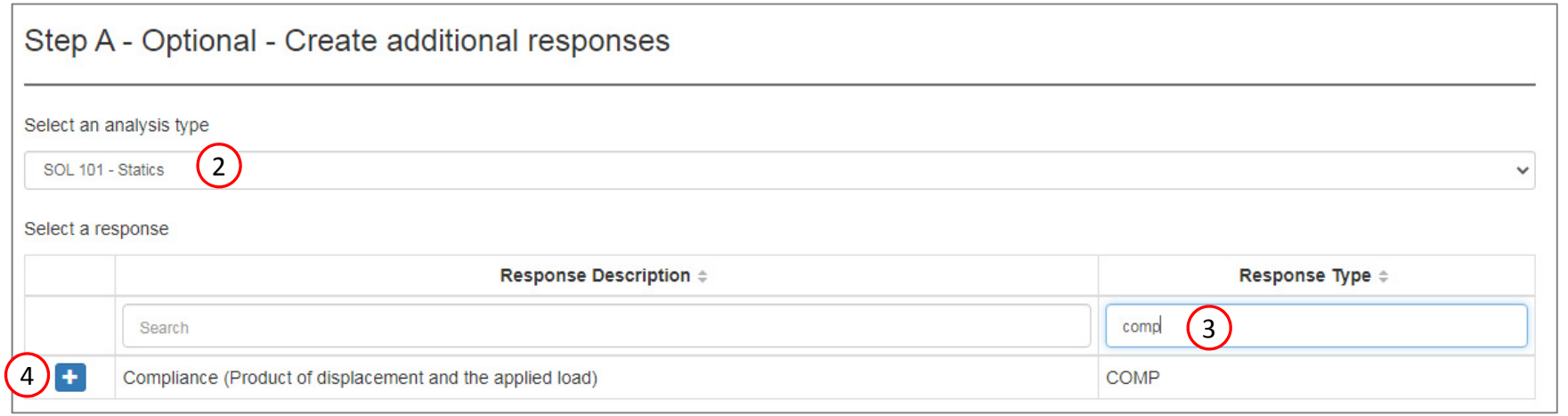
- There are 2 methods of setting an objective.
  - Method 1 – Select a objective from a given list of responses, e.g. Weight, Volume, etc.
  - Method 2 – Create an equation.
- This example uses Method 2 for the objective.

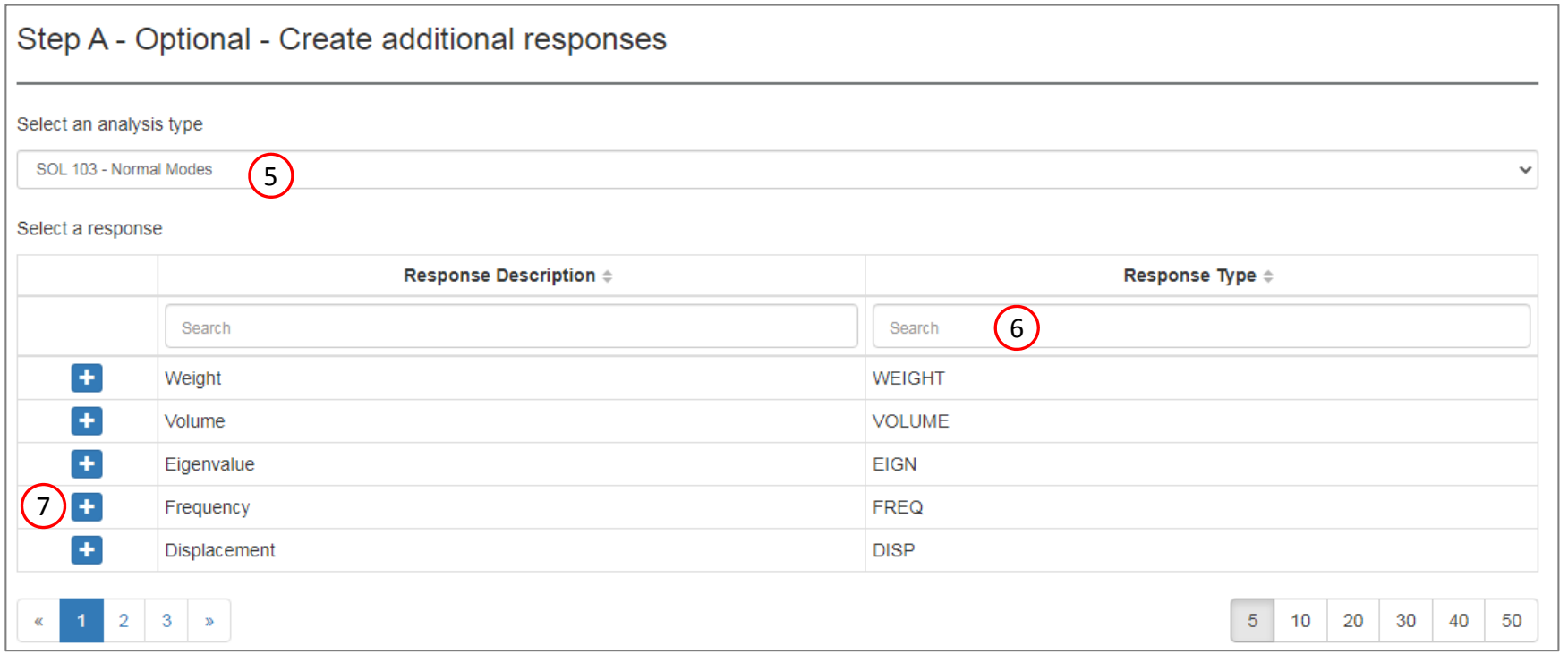


Create Design Objective

1. Scroll down to section Step A - Optional - Create additional responses
2. Ensure the analysis type is set to SOL 101 - Statics
3. Type in ‘comp’ to the search box
4. Click the plus (+) icon to set compliance as a response type
5. Set the analysis type as SOL 103 - Normal Modes
6. Clear the search box.
7. Click the plus (+) icon to set Frequency as a response type

- This example performs a multidisciplinary optimization for statics and modes. The objective will be a combination of compliance and natural frequency. The responses necessary for compliance and natural frequency are created on this page.

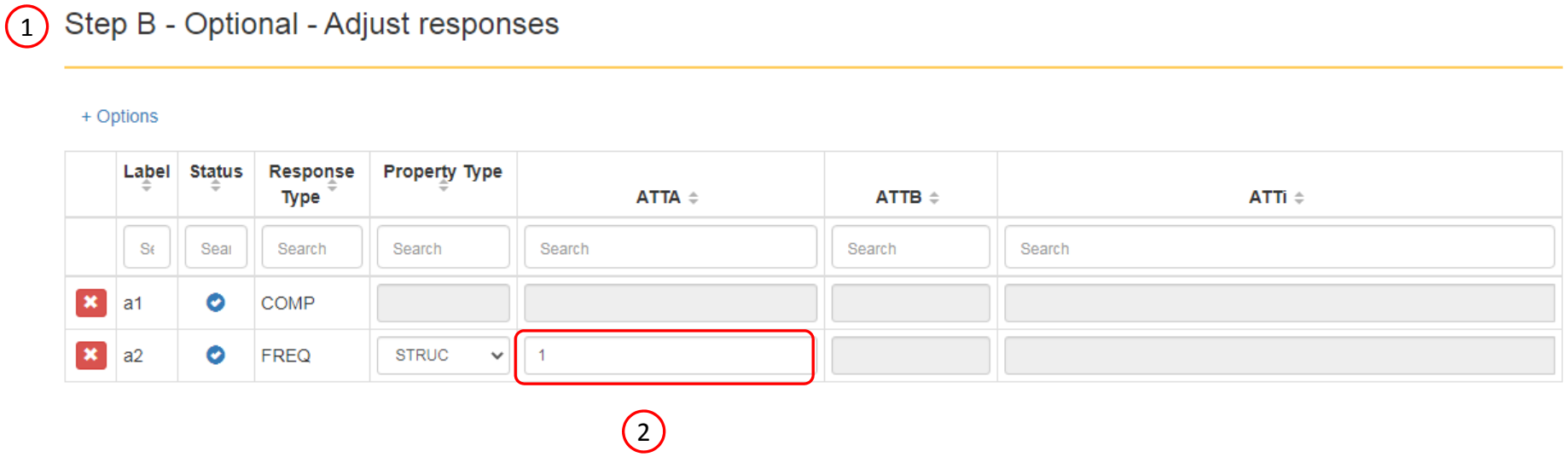




Create Design Objective

1. Scroll to section Step B - Optional - Adjust responses
2. For response a2, ensure ATTA is set to 1 which represents mode 1

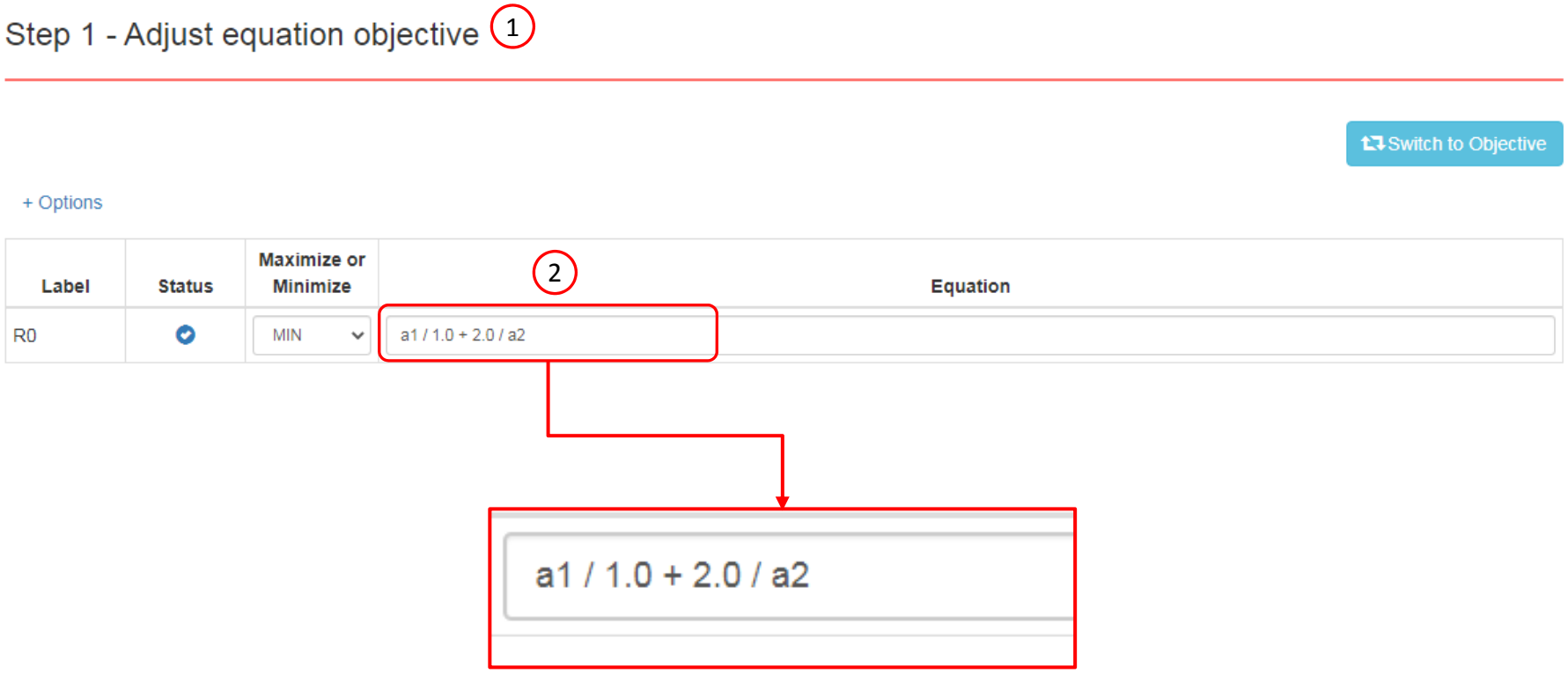
- a1 is read as the compliance. Compliance is twice the total strain energy. Refer to the Appendix for more information about compliance.
- a2 is the natural frequency for mode 1.



Create Design Objective

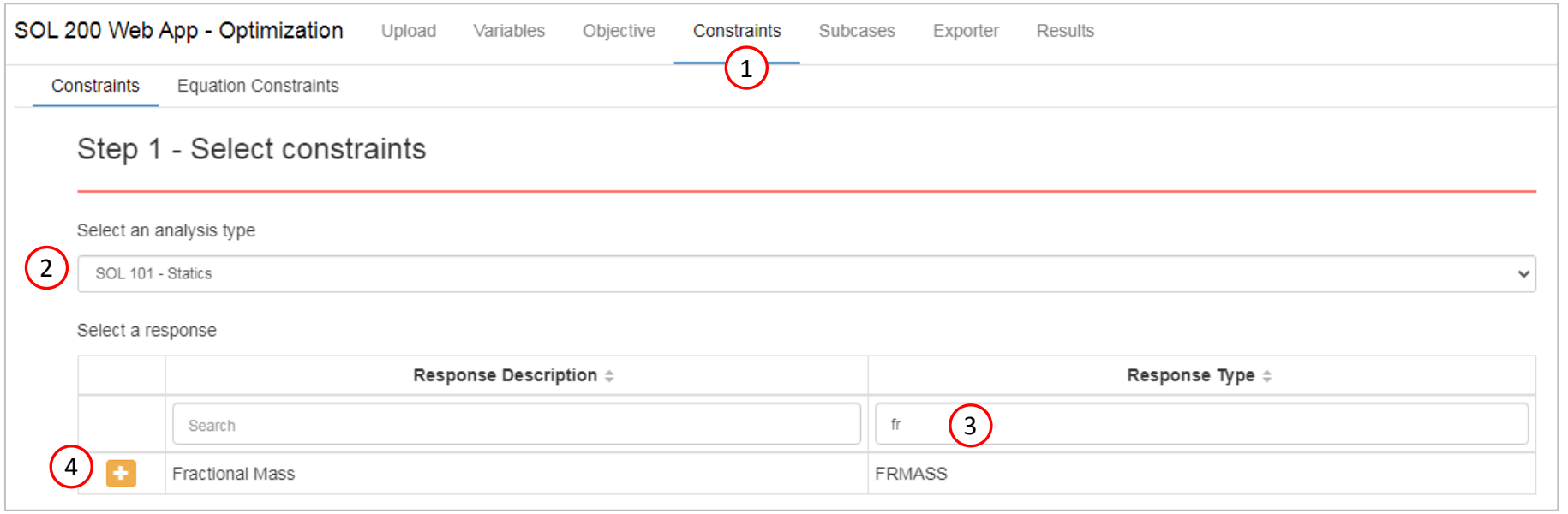
1. Scroll to section Step 1 - Adjust equation objective
2. Type this equation into the box
   - a1 / 1.0 + 2.0 / a2
3. The values 1.0 and 2.0 will be replaced later in this tutorial

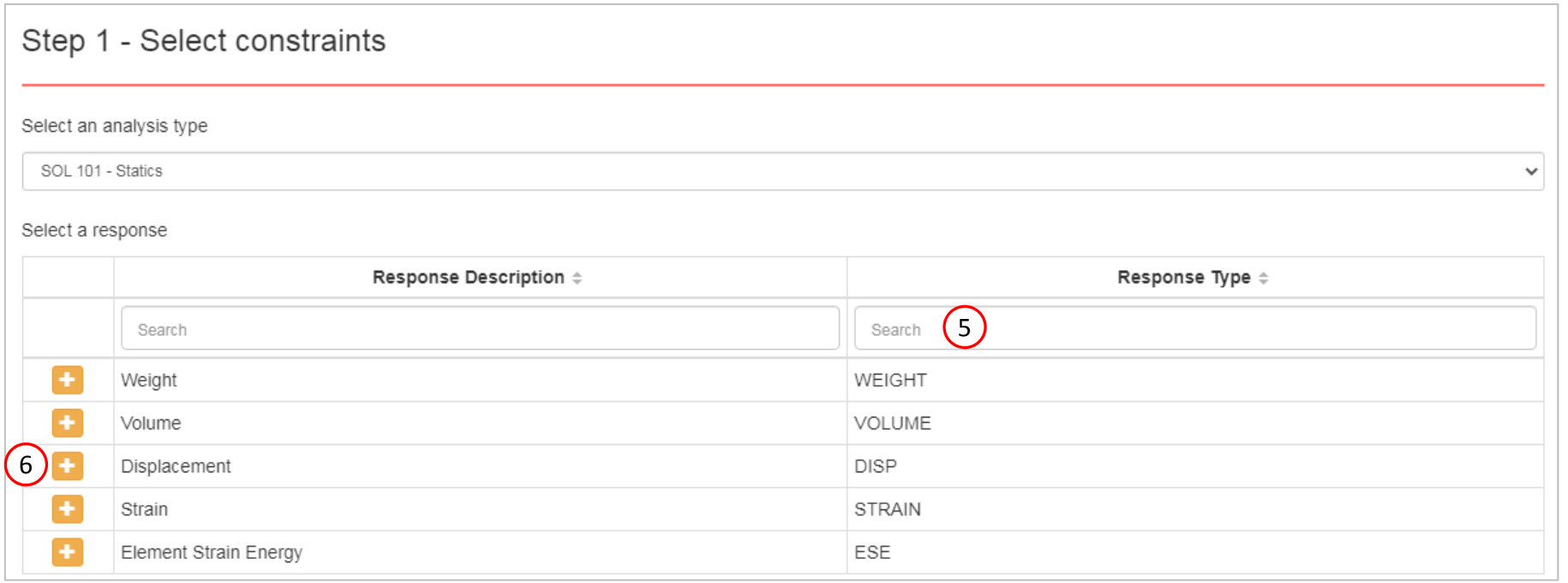
- The objective is a combination of a1 and a2. The objective must be conditioned properly such that if one response is larger than the other, e.g. a1=.01 and a2 = 2000000, a change in the smaller of the 2 is still detected by the optimizer. This is addressed by normalizing both a1 and a2. For now, it is not known which values are necessary to normalize a1 or a2, so values 1 and 2 are used for now.



Create Design Constraints

1. Click Constraints
2. Set the analysis type to SOL 101 - Statics
3. Type in ‘fr’ to the search box
4. Select the plus(+) icon for Fractional Mass
5. Clear the search box.
6. Select the plus(+) icon for Displacement

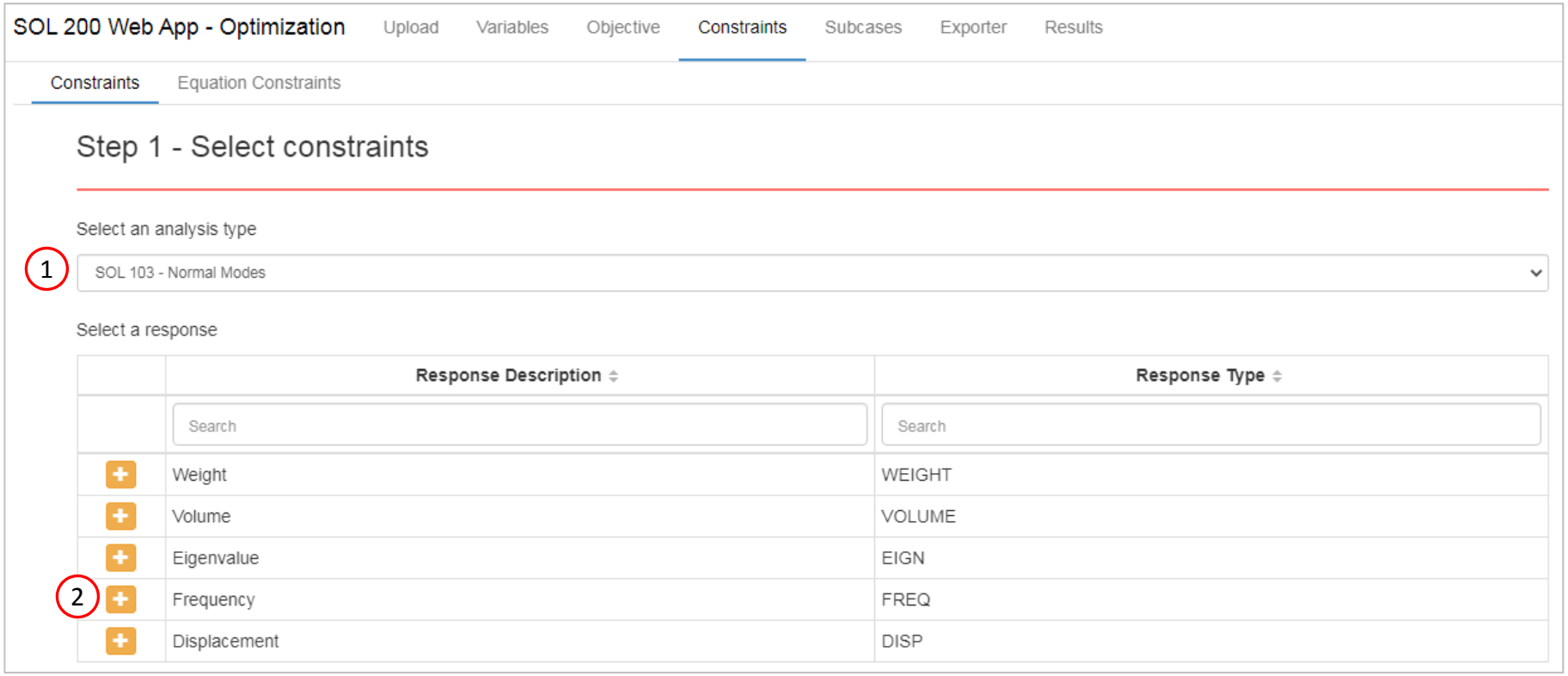




Create Design Constraints

1. Set the analysis type to SOL 103 - Modes
2. Select the plus(+) icon for Frequency

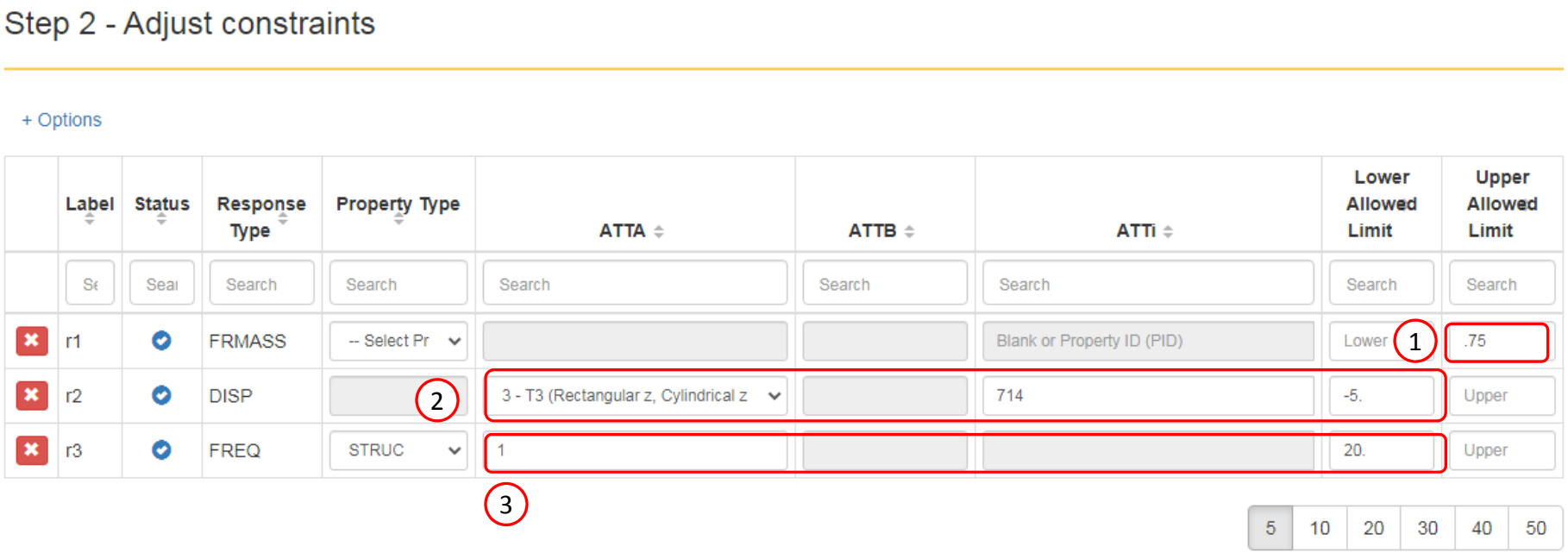
- Topology optimization works best when working with a small number of responses, e.g. Compliance, Fractional Mass, a single von Misses stress.
- In this tutorial a single displacement is constrained. The number of constraints should be kept to a minimum. For example, constraining multiple displacements at various nodes is not advised.



Create Design Constraints

1. Configure the following for r1
   - Upper Allowed Limit: .75
2. Configure the following for r2
   - ATTA: 3 (3 - T3 or Z component)
   - ATTi: 714 (node 714)
   - Lower Allowed Limit: -5.0
3. Configure the following for r3
   - ATTA: 1 (mode 1)
   - Lower Allowed Limit: 20.

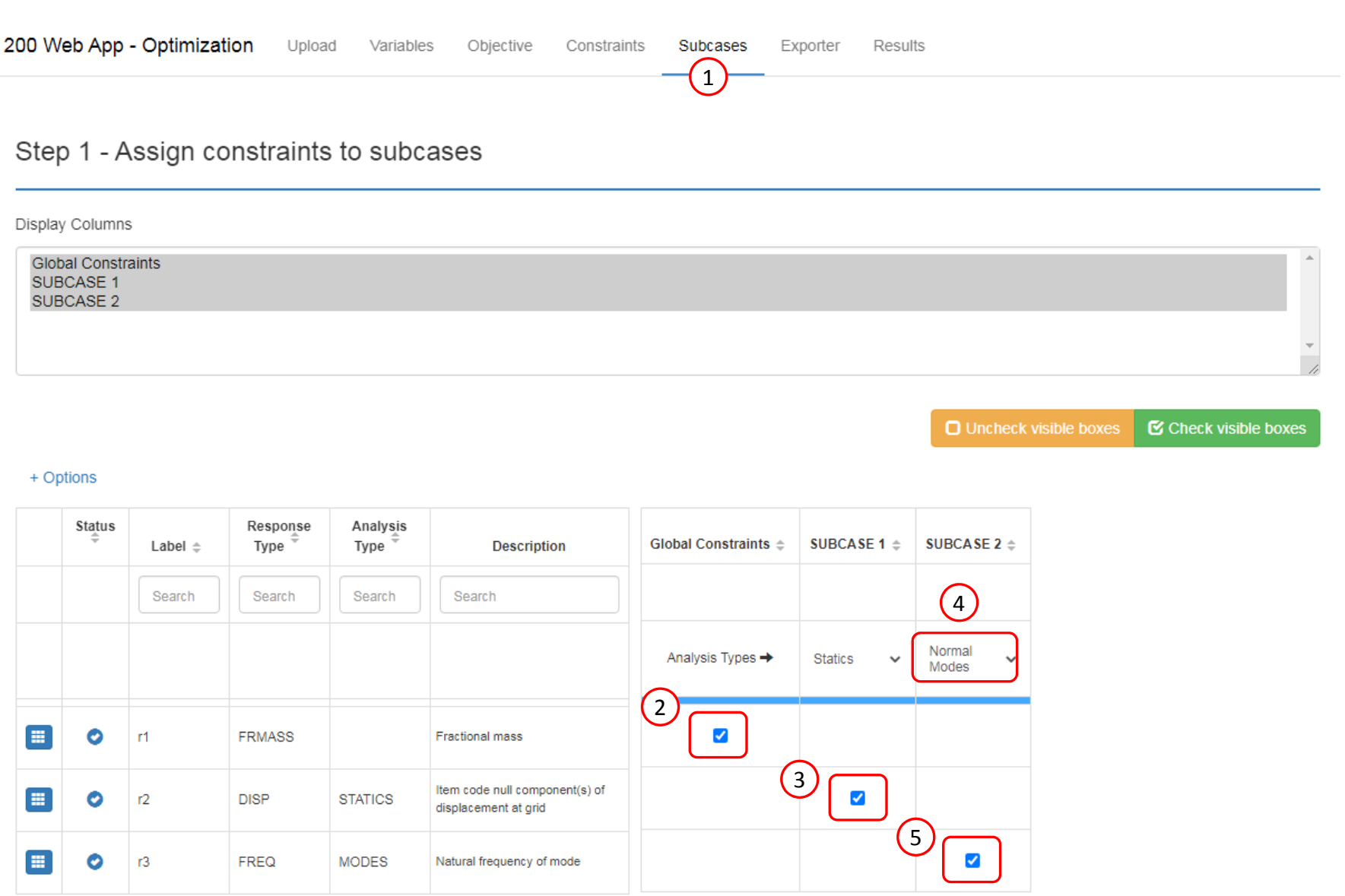
- Constraints r1 and r2 will be assigned to the statics subcase. Constraint r3 will be assigned to the modes subcase.



Assign Constraints to Load Cases (SUBCASES)

1. Click Subcases
2. Mark the checkbox
3. Mark the checkbox
4. Set the analysis type as Normal Modes for SUBCASE 2
5. Mark the checkbox

- r1 or FRMASS constraint has been assigned to Global Constraints
- r2 or DISP constraint has been assigned to SUBCASE 1, the statics subcase
- r3 or FREQ constraint has been assigned to SUBCASE 2, the modes subcase

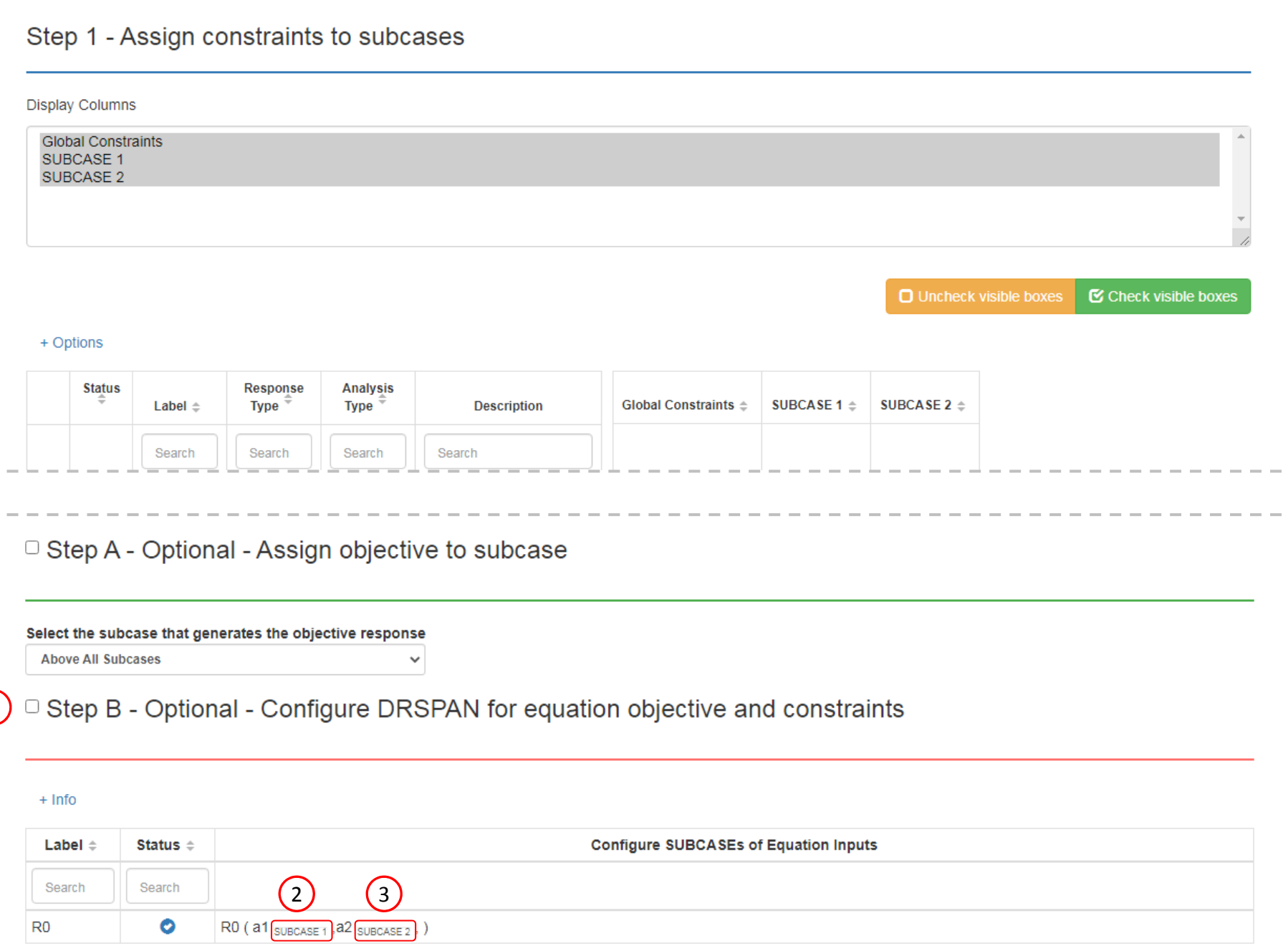


Configure DRSPAN

The Equation Objective is in terms of a1 and a2, where a1 is a statics response and a2 is a normal modes response. The DRSPAN functionality in Nastran is used to specify which SUBCASE generates a1 and a2.

1. Find this section: Step B - Optional - Configure DRSPAN for equation objective and constraints
2. Set a1 to SUBCASE 1
3. Set a2 to SUBCASE 2

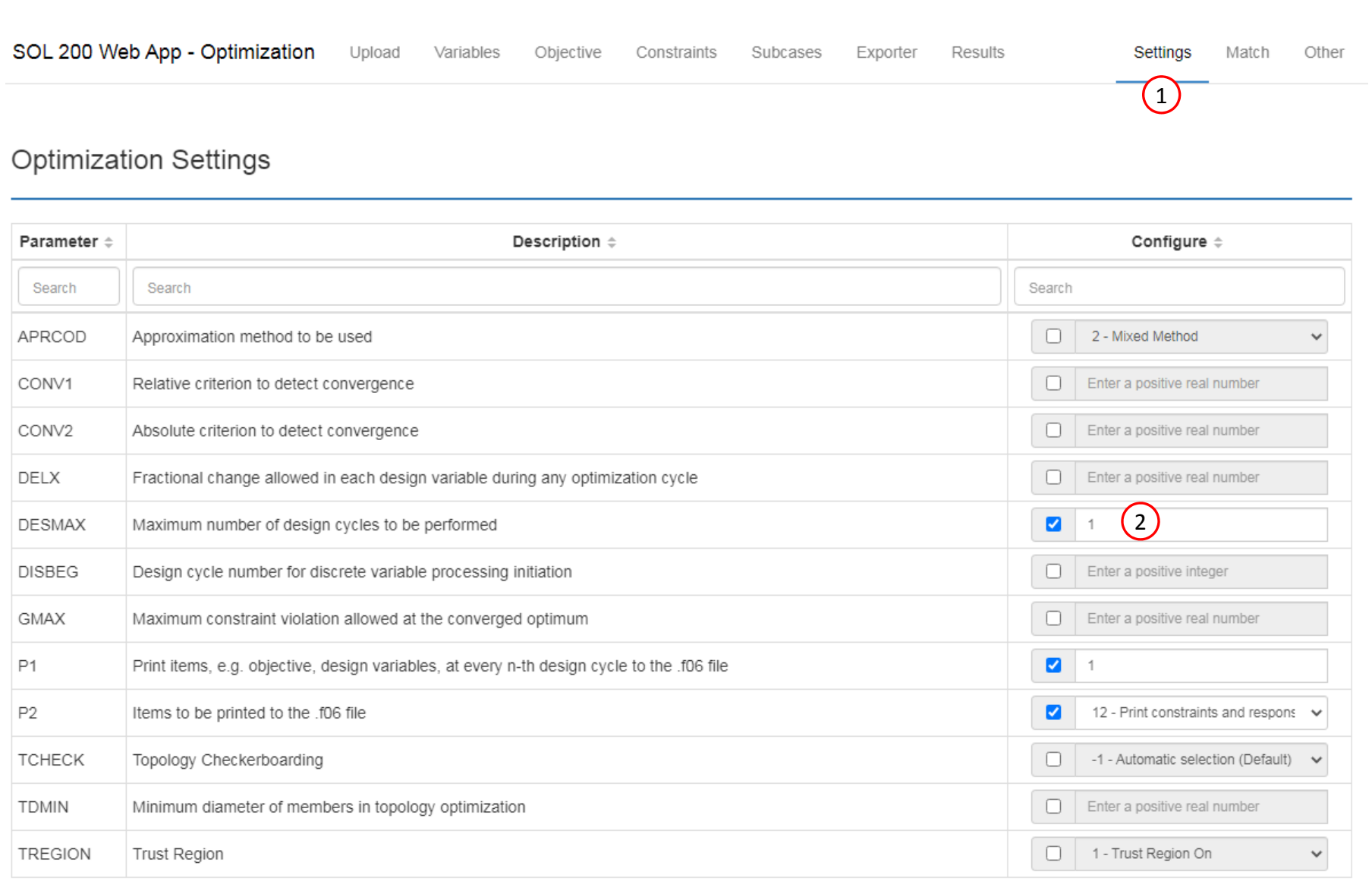
- Some responses, e.g. stress, strain, frequency, etc., are subcases dependent. The Equation Objective is composed of subcase dependent responses Compliance and Frequency. If there are numerous subcases, the optimizer must be told which subcases the responses originate from. This is done via the DRSPAN command and is configured on this page.



Configure Optimization Settings

1. Click Settings
2. Set DESMAX to 1

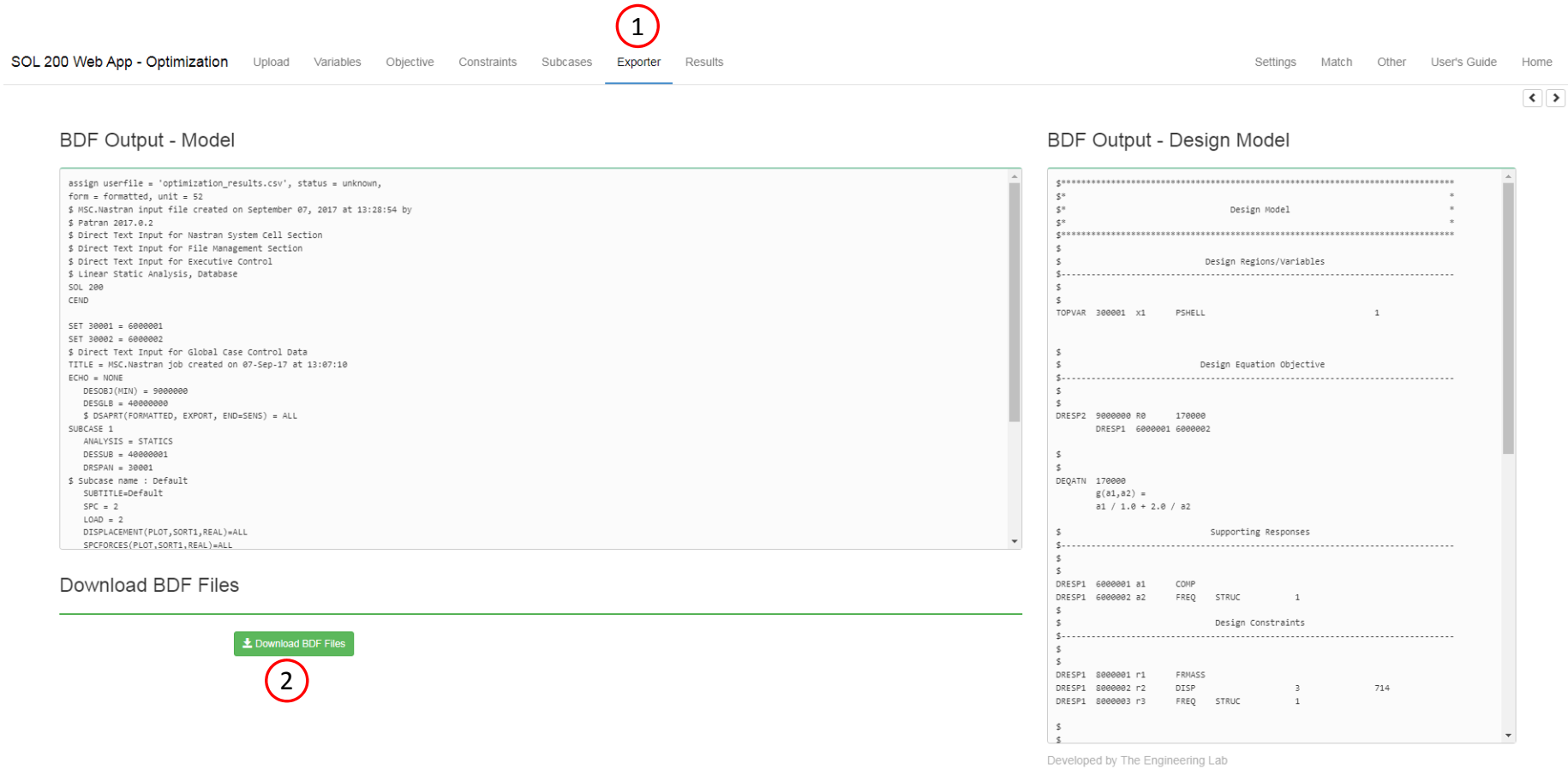
- Recall that the Equation Objective is composed of a1 and a2 and the goal is to find values that normalize both a1 and a2. This is done by obtaining the current or initial values of a1 and a2. In the event the values are not known, you can perform an optimization for only one design cycle. The initial values are then available as shown on the following pages.



Export New BDF Files

1. Click on Exporter
2. Click on Download BDF Files

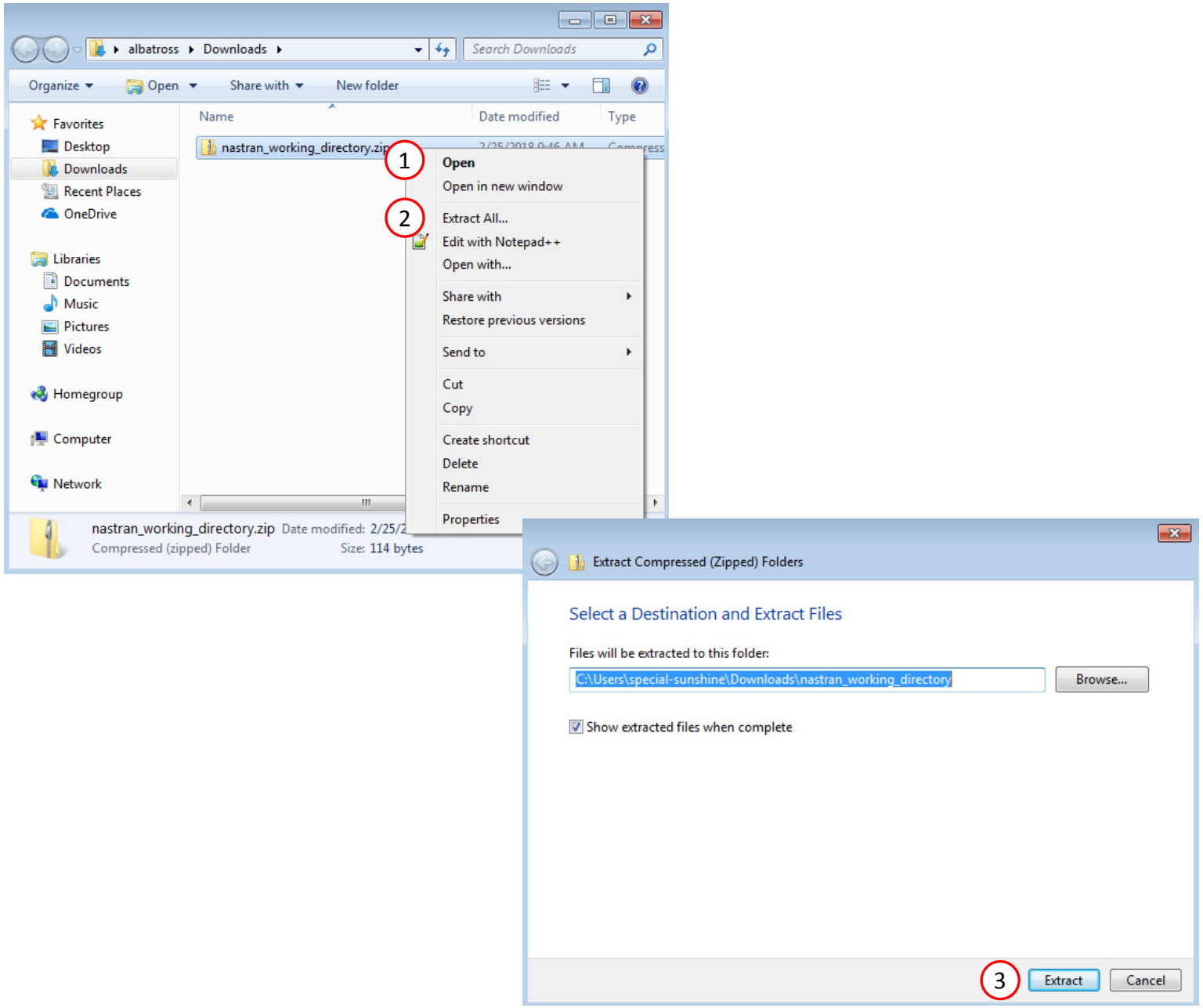
- When the download button is clicked a new file named “nastran_working_directory” is downloaded. If the file already exists in your local folder, the folder name is appended with a number, e.g. “nastran_working_directory (1).zip”



Perform the Optimization with Nastran SOL 200

1. A new .zip file has been downloaded
2. Right click on the file
3. Click Extract All
4. Click Extract on the following window

- Always extract the contents of the ZIP file to a new, empty folder.



Perform the Optimization with Nastran SOL 200

1. Inside of the new folder, double click on Start MSC Nastran
2. Click Open, Run or Allow Access on any subsequent windows
3. MSC Nastran will now start

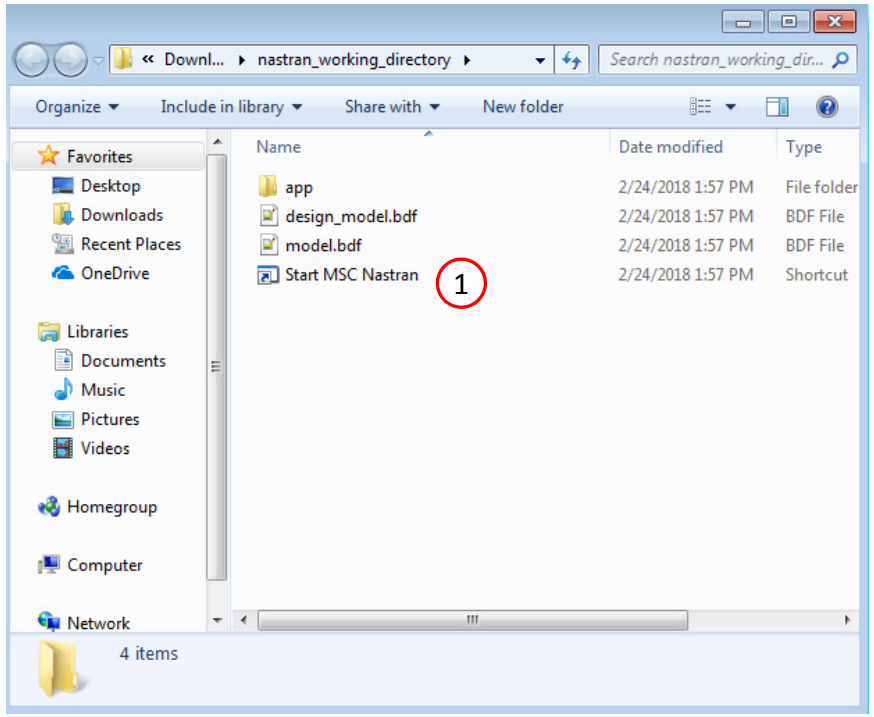
- After a successful optimization, the results will be automatically displayed as long as the following files are present: BDF, F06 and LOG.
- One can run the Nastran job on a remote machine as follows:
  1) Copy the BDF files and the INCLUDE files to a remote machine. 2) Run the MSC Nastran job on the remote machine. 3) After completion, copy the BDF, F06, LOG, H5 files to the local machine. 4) Click "Start MSC Nastran" to display the results.

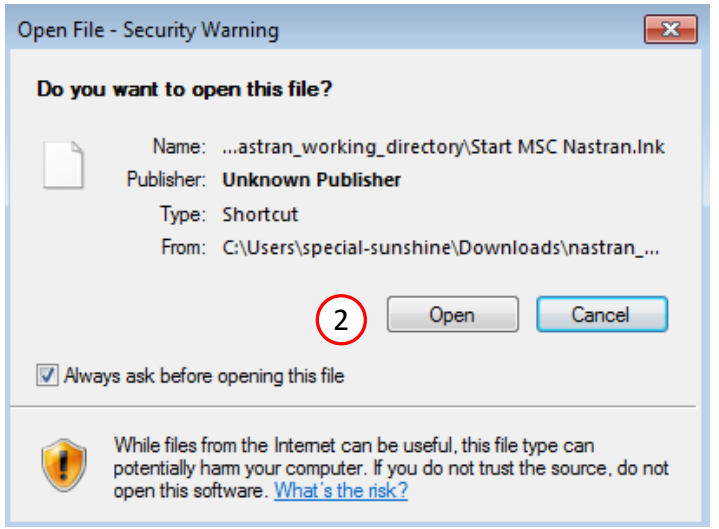
Using Linux?

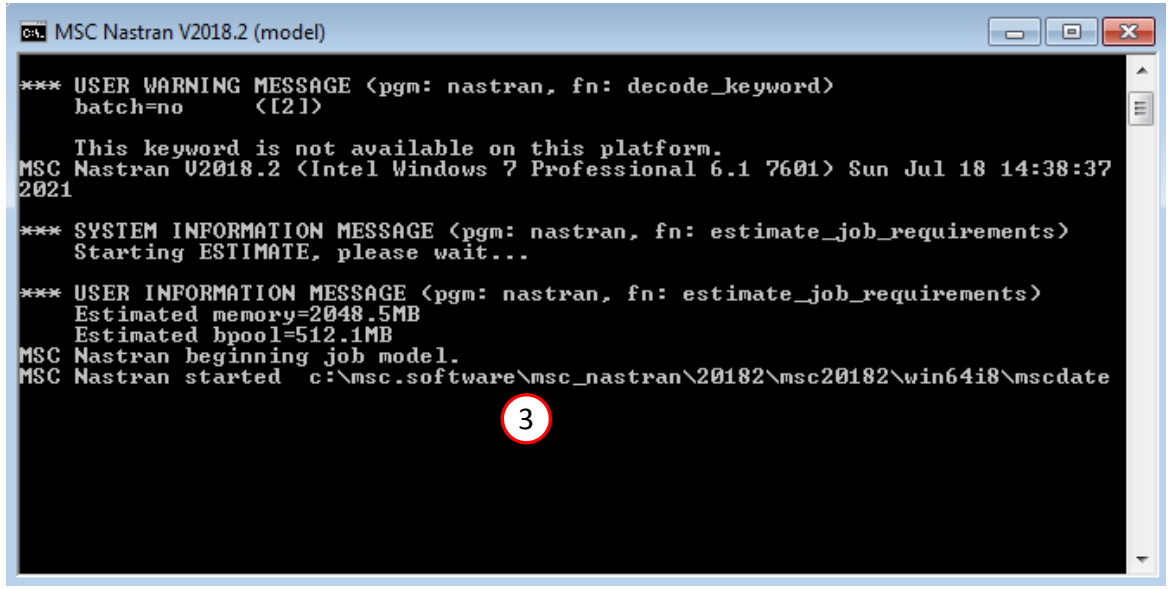
Follow these instructions:
1) Open Terminal
2) Navigate to the nastran_working_directory
cd ./nastran_working_directory
3) Use this command to start the process
./Start_MSC_Nastran.sh

In some instances, execute permission must be granted to the directory. Use this command. This command assumes you are one folder level up.

sudo chmod -R u+x ./nastran_working_directory







Status

1. While MSC Nastran is running, a status page will show the current state of MSC Nastran

- The status of the MSC Nastran job is reported on the Status page. Note that Windows 7 users will experience a delay in the status updates. All other users of Windows 10 and Red Hat Linux will see immediate status updates.

SOL 200 Web App - Status

Python MSC Nastran

Status

Name	Status of Job	Design Cycle	RUN TERMINATED DUE TO
model.bdf	Running	None	

Review Optimization Results

1. After MSC Nastran is successfully complete, the results will be automatically uploaded.
2. The final value of objective and normalized constraints can be reviewed.

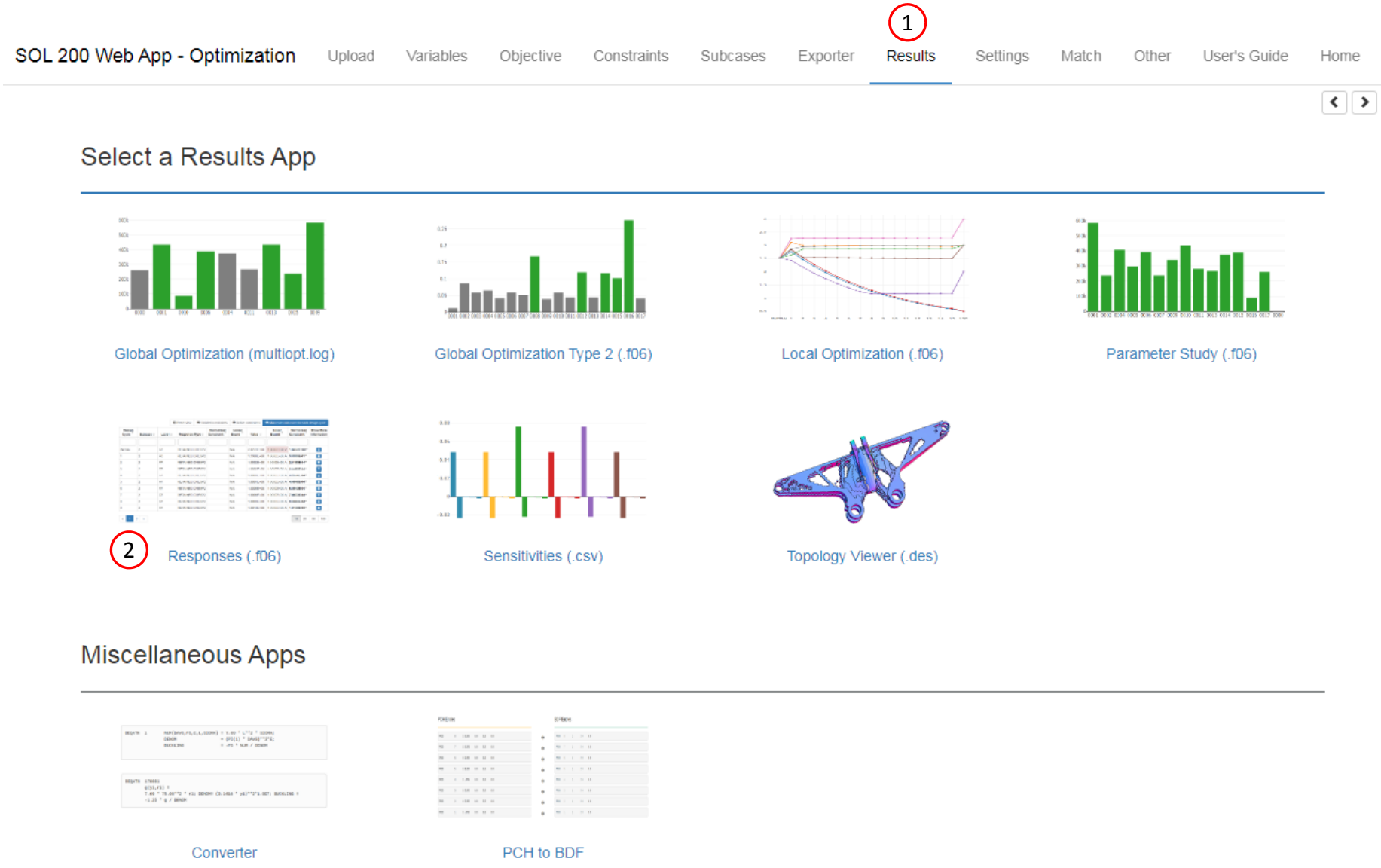
- After an optimization, the results will be automatically displayed as long as the following files are present: BDF, F06 and LOG.

Obtain quantities from .f06

The previous optimization was done only for one design cycle. The intent was to obtain two quantities a1 and a2, the compliance and 1st natural frequency, respectively.

1. Go to the Results section
2. Click on the Responses link

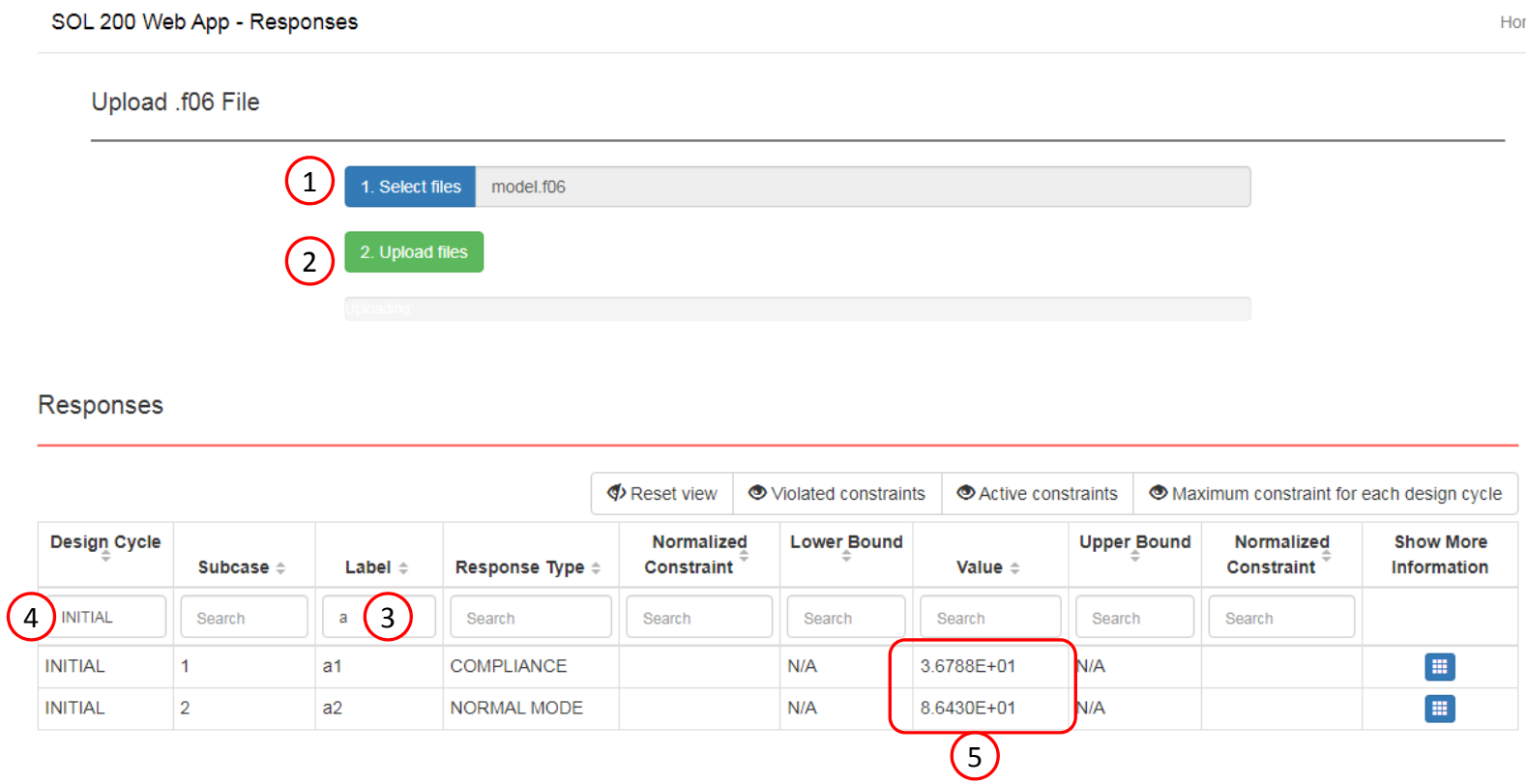
- Recall that the initial values for a1 and a2 must be obtained. These initial values are contained in the F06 file. The Responses app is opened and will be used to extract the initial values for a1 and a2.



Obtain quantities from .f06

1. Select the file named model.f06
2. Click Upload files
3. In the search box's Label column, type ‘a’
4. In the search box's Design Cycle column, type ‘INITIAL’
5. The values for a1 and a2 are now visible and will be used in the next slide

- The search boxes are used to display the values for a1 and a2. The Equation Objective is currently set to R0 = a1 / 1.0 + 2.0 / a2. The initial values will be used to replace 1.0 and 2.0.



Responses in Design Model

1. The previous table extracted values from the section titled *Responses in Design Model*
2. The value of a1 is visible
3. The value of a2 is visible

- As a side note, the values reported in the Responses app are values found in the F06 file, section RESPONSES IN DESIGN MODEL.

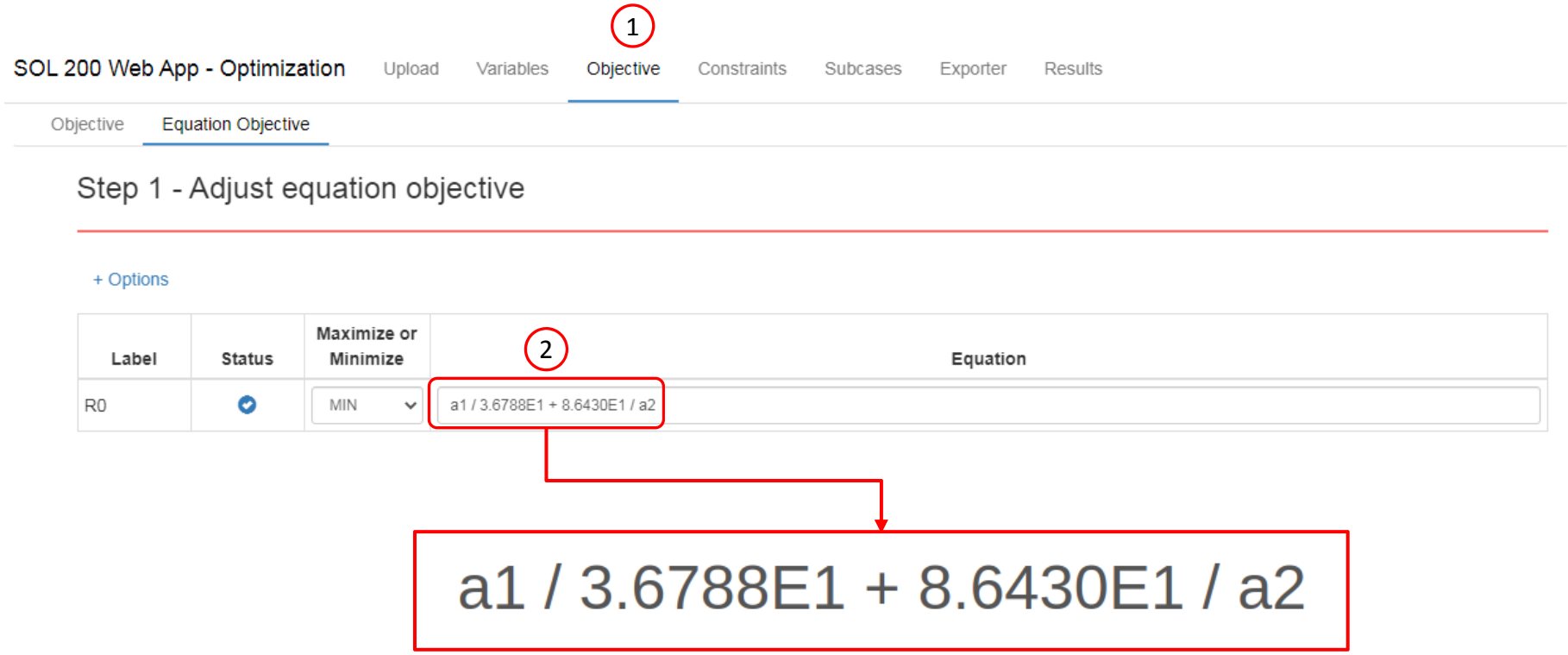
```
                                  ***********************************************
                                  *                                             *
                                  *        I N I T I A L   A N A L Y S I S      *
                                  *                                             *
                                  ***********************************************


                            *******   ANALYSIS RESULTS BASED ON THE INITIAL DESIGN   *******
MSC.NASTRAN JOB CREATED ON 07-SEP-17 AT 13:07:10                    SEPTEMBER   7, 2017  MSC Nastran  4/ 5/1
                                                                                                           SUBCA

                    (1)  ----------------------------------------------------------------
                         |     R E S P O N S E S    IN    D E S I G N    M O D E L       |
                         ----------------------------------------------------------------

                                  (N/A - BOUND NOT ACTIVE OR AVAILABLE)
                                (*** VIOLATED RESPONSES MARKED WITH V ***)
                                (*** ACTIVE RESPONSES MARKED WITH A ***)

                      I N I T I A L   A N A L Y S I S   S U B C A S E =      1

                                  -----   DISPLACEMENT RESPONSES   -----

-------------------------------------------------------------------------------------------------------------
    INTERNAL     DRESP1     RESPONSE     GRID     COMPONENT        LOWER                          UPPER
       ID          ID        LABEL        ID         NO.           BOUND            VALUE         BOUND
-------------------------------------------------------------------------------------------------------------
           1     8000002    R2            714           3     -5.0000E+00 V    -5.8426E+00        N/A

                                  -----    COMPLIANCE RESPONSES -----

-------------------------------------------------------------------------------------------------------------
   INTERNAL    DRESP1    RESPONSE                                        LOWER                    UPPER
      ID         ID       LABEL                                          BOUND        VALUE       BOUND
-------------------------------------------------------------------------------------------------------------
       2    6000001        A1                                             N/A  (2)  3.6788E+01     N/A

                               -----    FRACTIONAL MASS RESPONSES -----

-------------------------------------------------------------------------------------------------------------
   INTERNAL    DRESP1    RESPONSE   TOPVAR/TOMVAR                        LOWER                    UPPER
      ID         ID       LABEL         ID                               BOUND        VALUE       BOUND
-------------------------------------------------------------------------------------------------------------
          3    8000001   R1             0                                 N/A       7.5000E-01   7.5000E-01 A

                      I N I T I A L   A N A L Y S I S   S U B C A S E =      2

                                 -----   NORMAL MODE RESPONSES      -----

-------------------------------------------------------------------------------------------------------------
       INTERNAL      DRESP1      RESPONSE      MODE          LOWER                            UPPER
          ID           ID         LABEL         NO.          BOUND           VALUE            BOUND
-------------------------------------------------------------------------------------------------------------
            4       6000002      A2               1            N/A  (3)   8.6430E+01          N/A
```

Update Design Objective

The previous values, 3.6788E+01 and 8.6430E+01, from the .f06 file will be used to update the Design Objective.

1. Go back to the web app and click on Objective
2. Update the equation so it reads:
   - a1 / 3.6788E1 + 8.6430E1 / a2

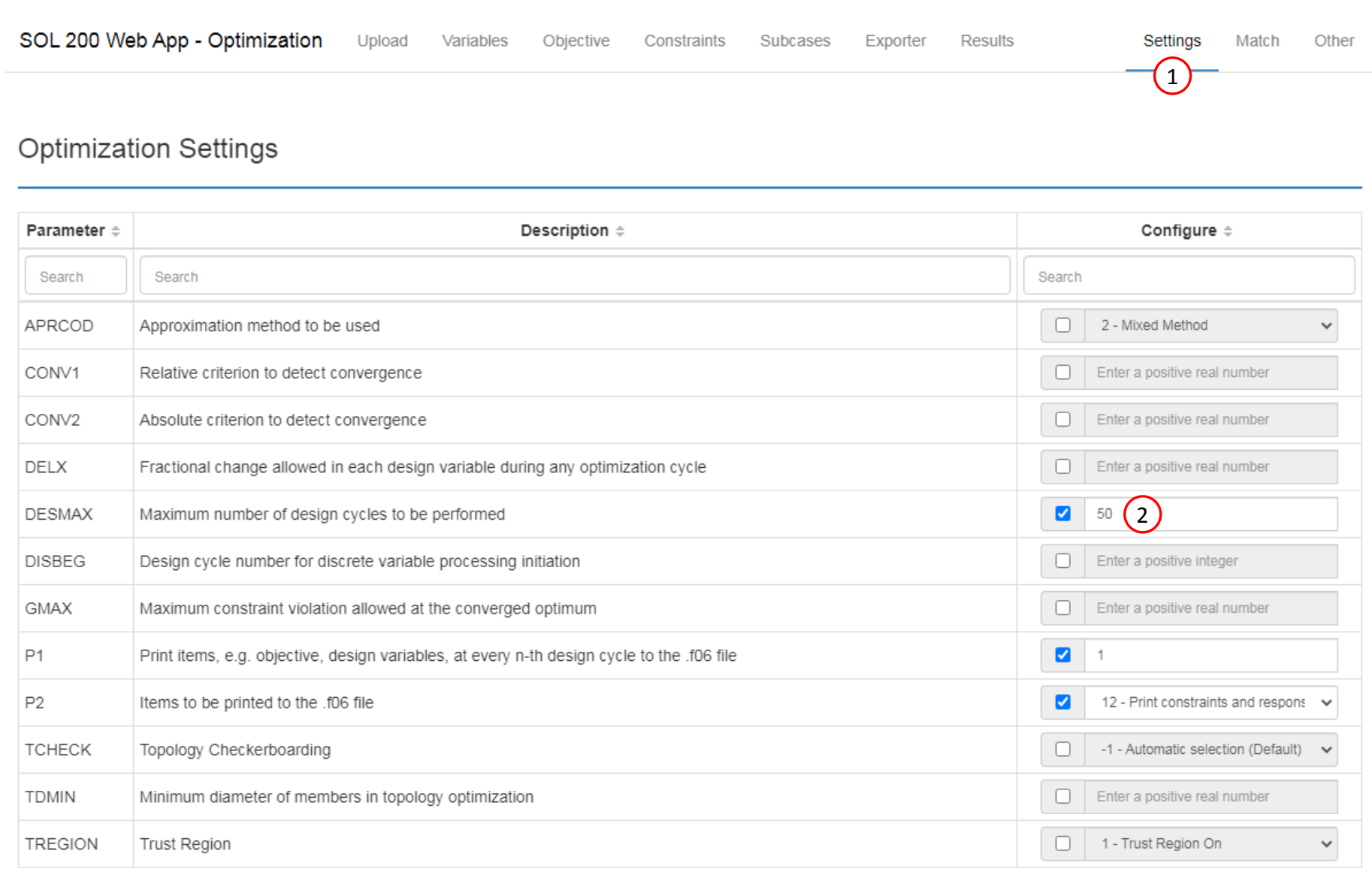
- The reader may realize that a2 is the denominator in its normalized term. This is done for the following reason. The goal is to minimize compliance, but to maximize the natural frequency, note the paradox in goals, i.e. minimization and maximization. This paradox is resolved by inverting the a2 term and placing a2 in the denominator. As the natural frequency a2 value is increased or maximized, the term "8.6430E1 / a2" goes to 0.



Configure Optimization Settings

1. Click Settings
2. Set DESMAX to 50

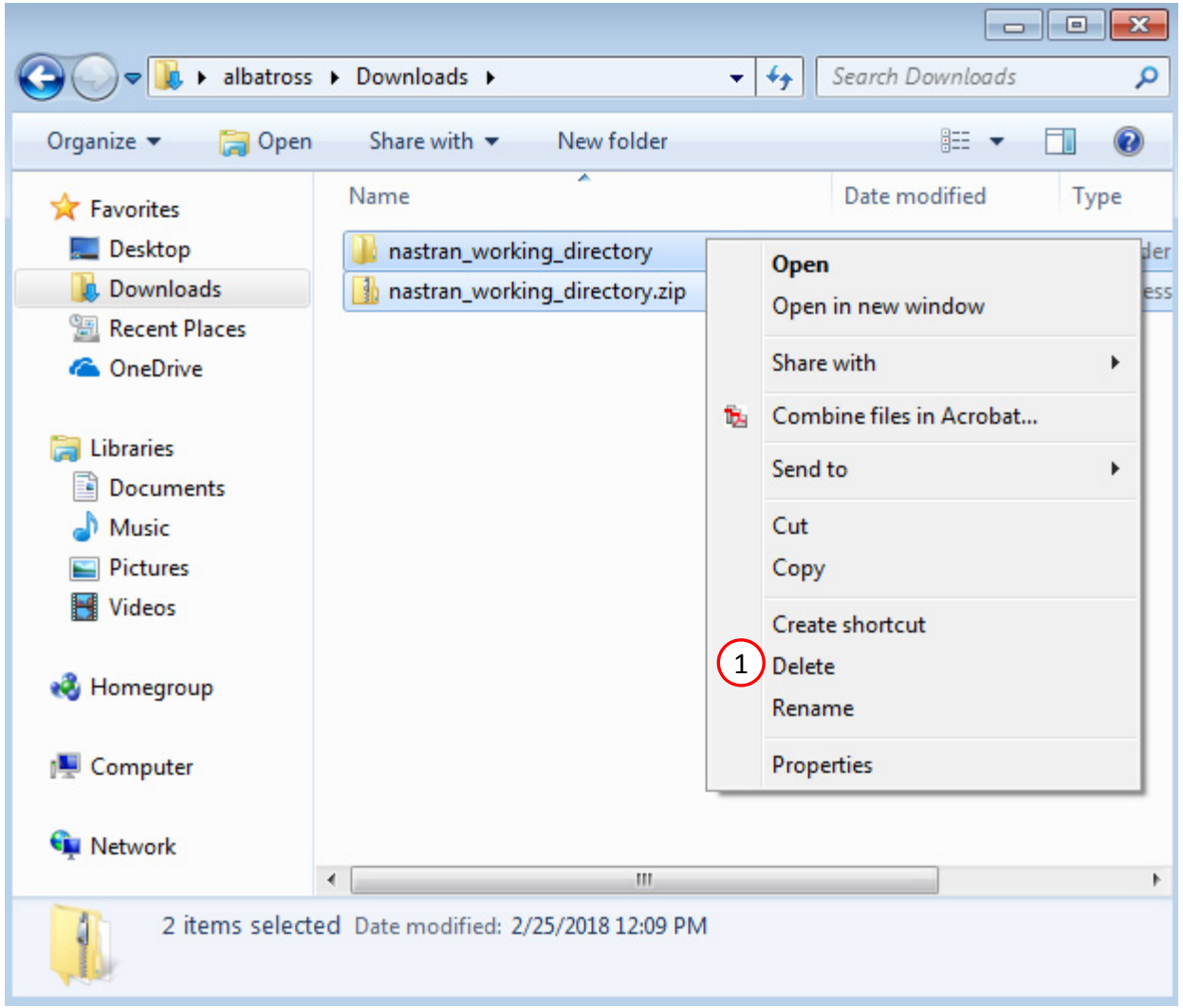
- Previously, the topology optimization was limited to only 1 design cycle. The max is changed to 100 to allow for a normal topology optimization.



Delete old files

1. Select old files and delete them. New files will be downloaded in the next step.

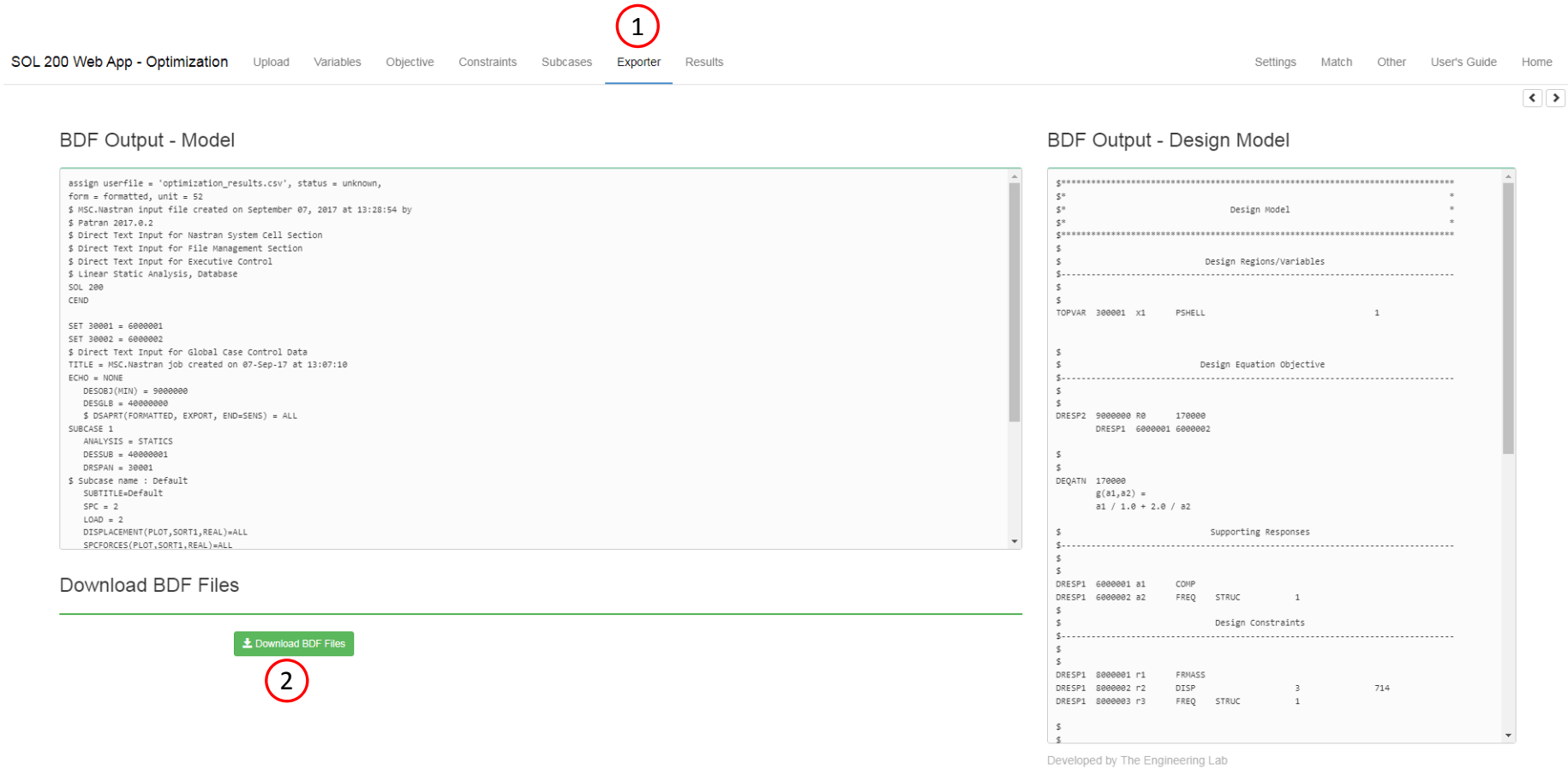
- Deleting the files is optional, but is encouraged to avoid confusion with other files and folders.



Export New BDF Files

1. Click on Exporter
2. Click on Download BDF Files

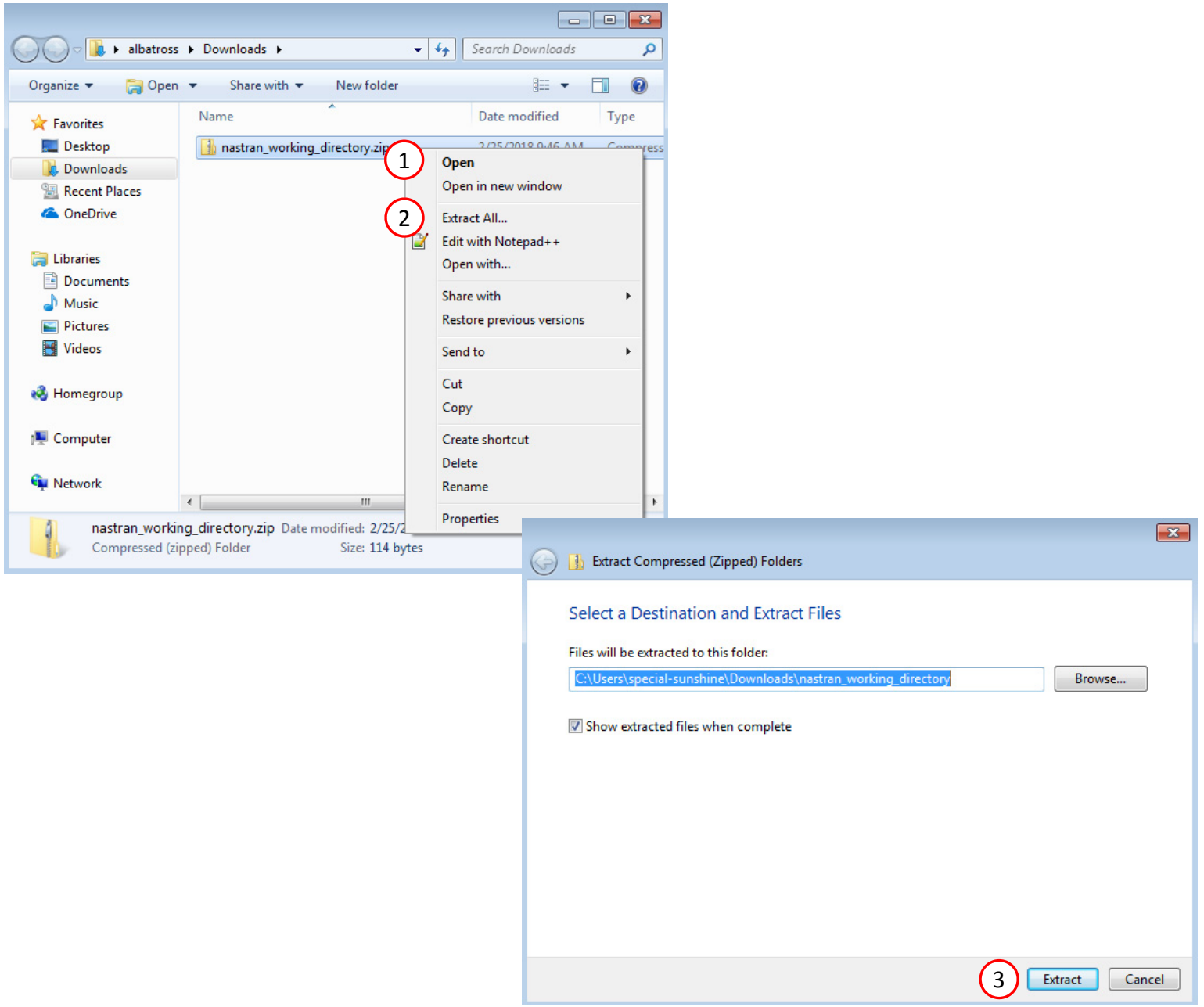
- When the download button is clicked a new file named “nastran_working_directory” is downloaded. If the file already exists in your local folder, the folder name is appended with a number, e.g. “nastran_working_directory (1).zip”



Perform the Optimization with Nastran SOL 200

1. A new .zip file has been downloaded
2. Right click on the file
3. Click Extract All
4. Click Extract on the following window

- Always extract the contents of the ZIP file to a new, empty folder.



Perform the Optimization with Nastran SOL 200

1. Inside of the new folder, double click on Start MSC Nastran
2. Click Open, Run or Allow Access on any subsequent windows
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- One can run the Nastran job on a remote machine as follows:
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Using Linux?

Follow these instructions:
1) Open Terminal
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cd ./nastran_working_directory
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In some instances, execute permission must be granted to the directory. Use this command. This command assumes you are one folder level up.

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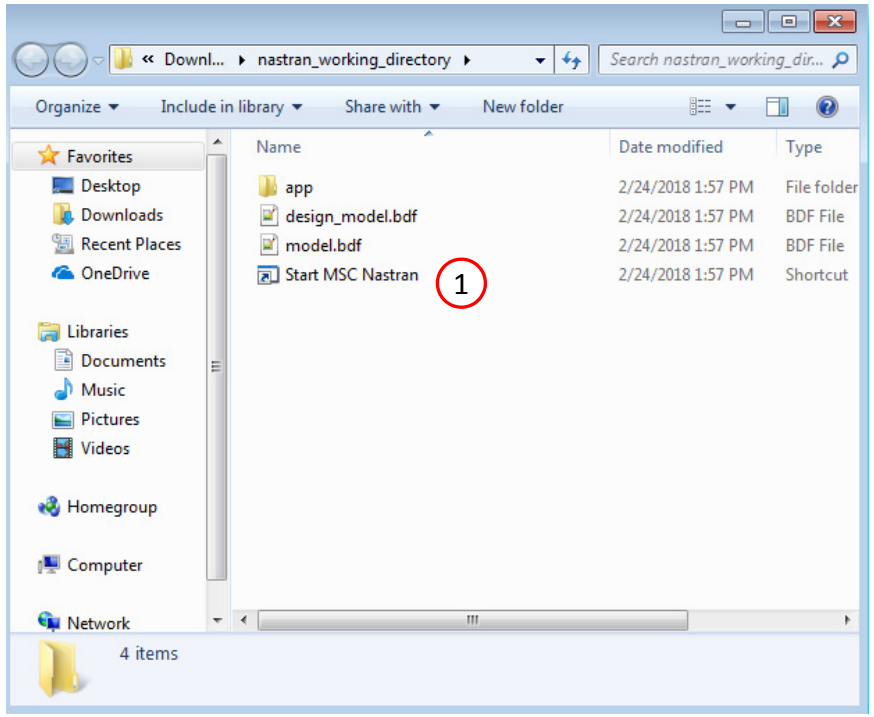

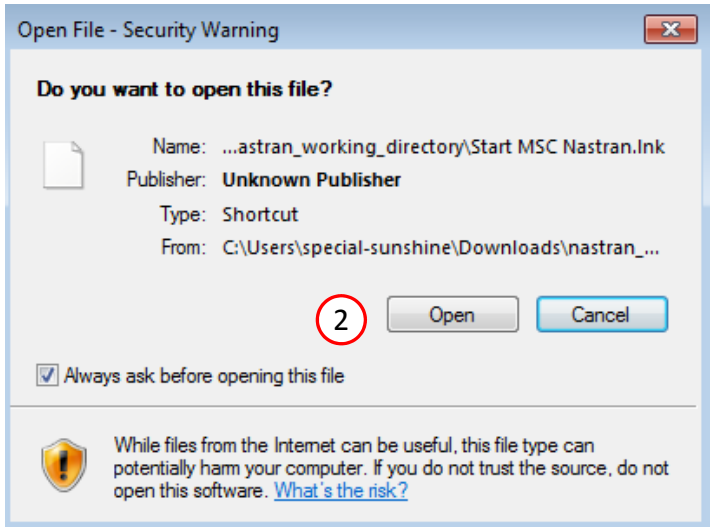

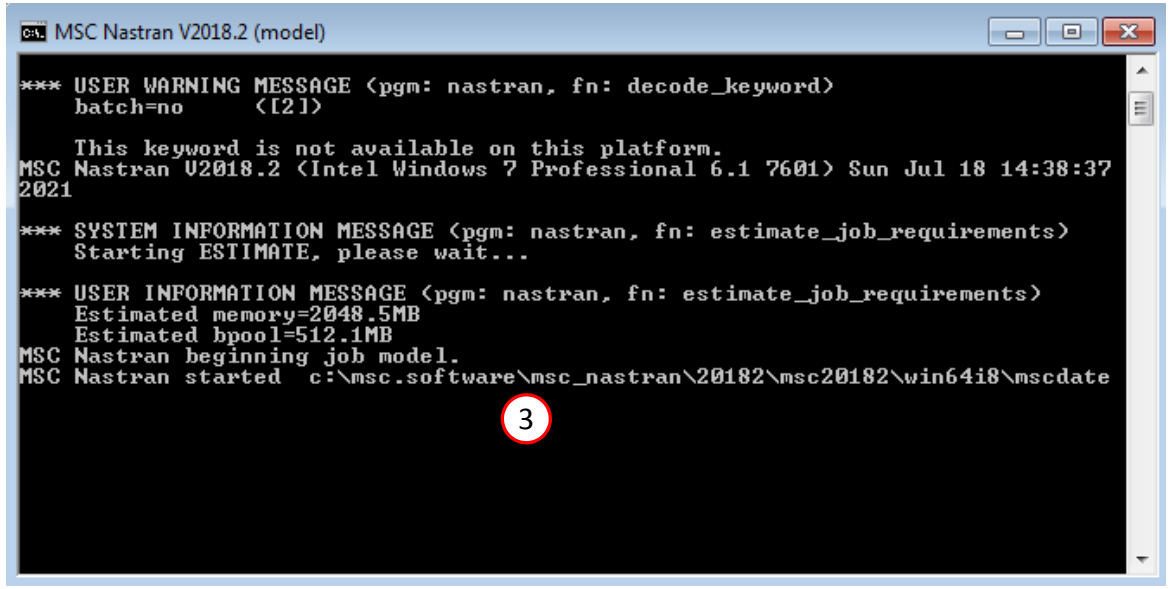

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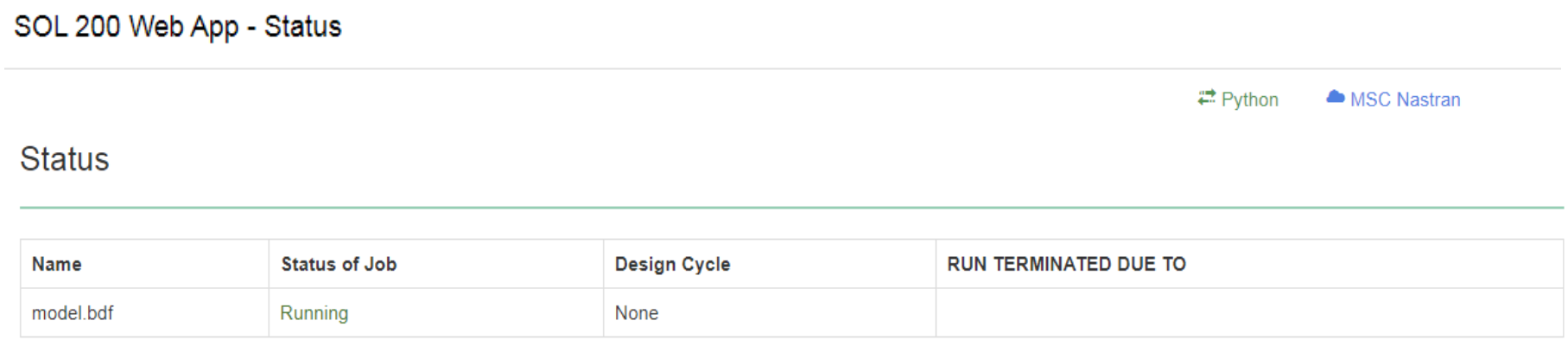


Review Optimization Results

After MSC Nastran is finished, the results will be automatically uploaded.

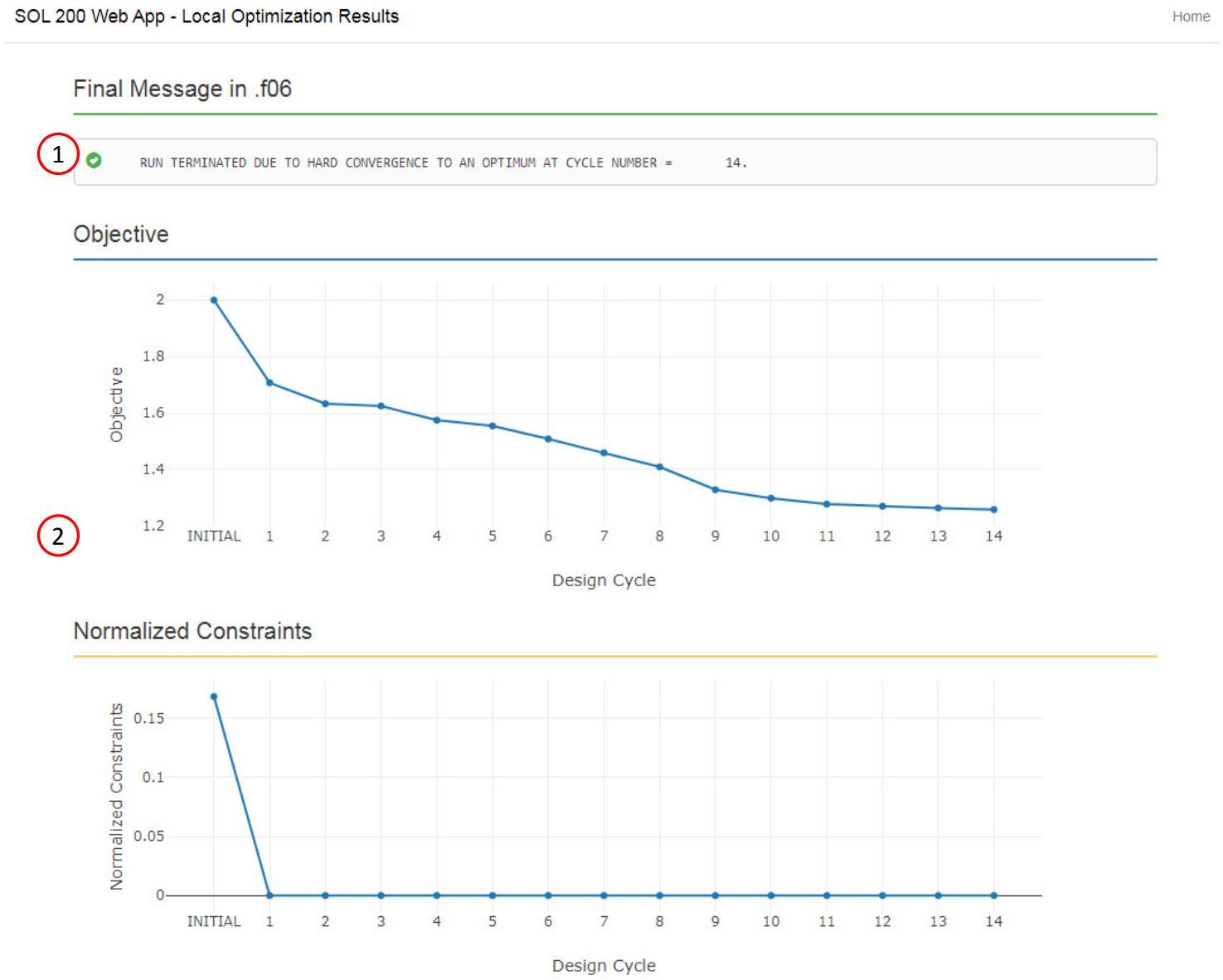
1. Ensure the messages shown have green checkmarks. This is indication of success. Any red icons indicate challenges.
2. The final value of objective and normalized constraints can be reviewed.

- After an optimization, the results will be automatically displayed as long as the following files are present: BDF, F06 and LOG.
- Note that initial value of the objective is 2.0. The Equation Objective has been configured such that the a1 and a2 terms are normalized or 1.0 each. For the initial design, R0 evaluates as follows:

  R0 = a1 / 3.6788E1 + 8.6430E1 / a2

  = 3.6788E1 / 3.6788E1 + 8.6430E1 / 8.6430E1

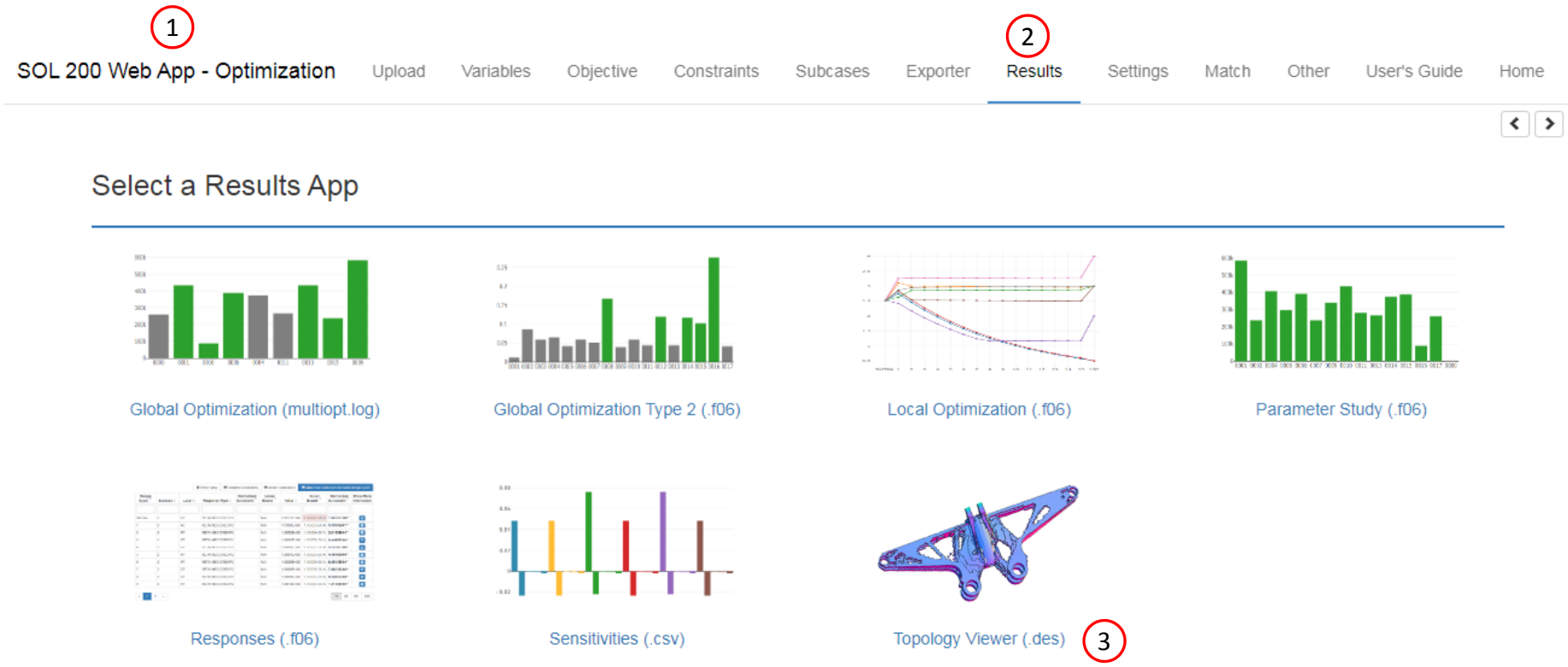
  = 2.0



Review Optimization Results

1. Return to the Optimization web app
2. Go to the Results section
3. Click Topology Viewer

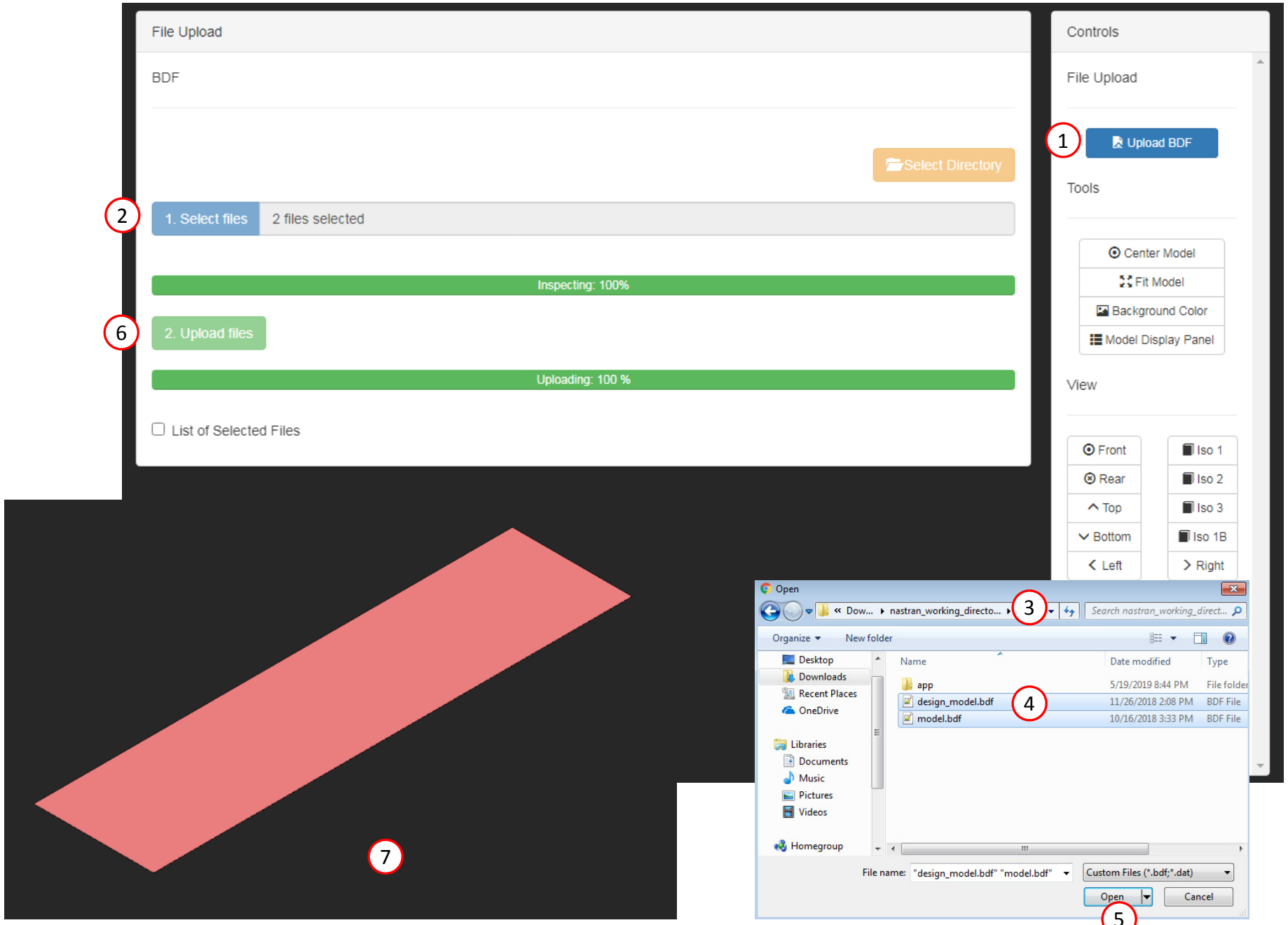
- The Topology Viewer is capable of displaying topology results and is accessed from the Results section of the Optimization web app. The appendix has additional information regarding capabilities of the Topology Viewer.



Review Optimization Results

1. Click Upload BDF
2. Click 1. Select files
3. Navigate to directory nastran_working_directory
4. Select the model.bdf and design_model.bdf files.
5. Click Open
6. Click 2. Upload files
7. The model is displayed

- During file upload, reading and parsing process, the web app does not report the reading progress for large files. Know that the web app parses files at a rate of 10MB every 25 seconds.

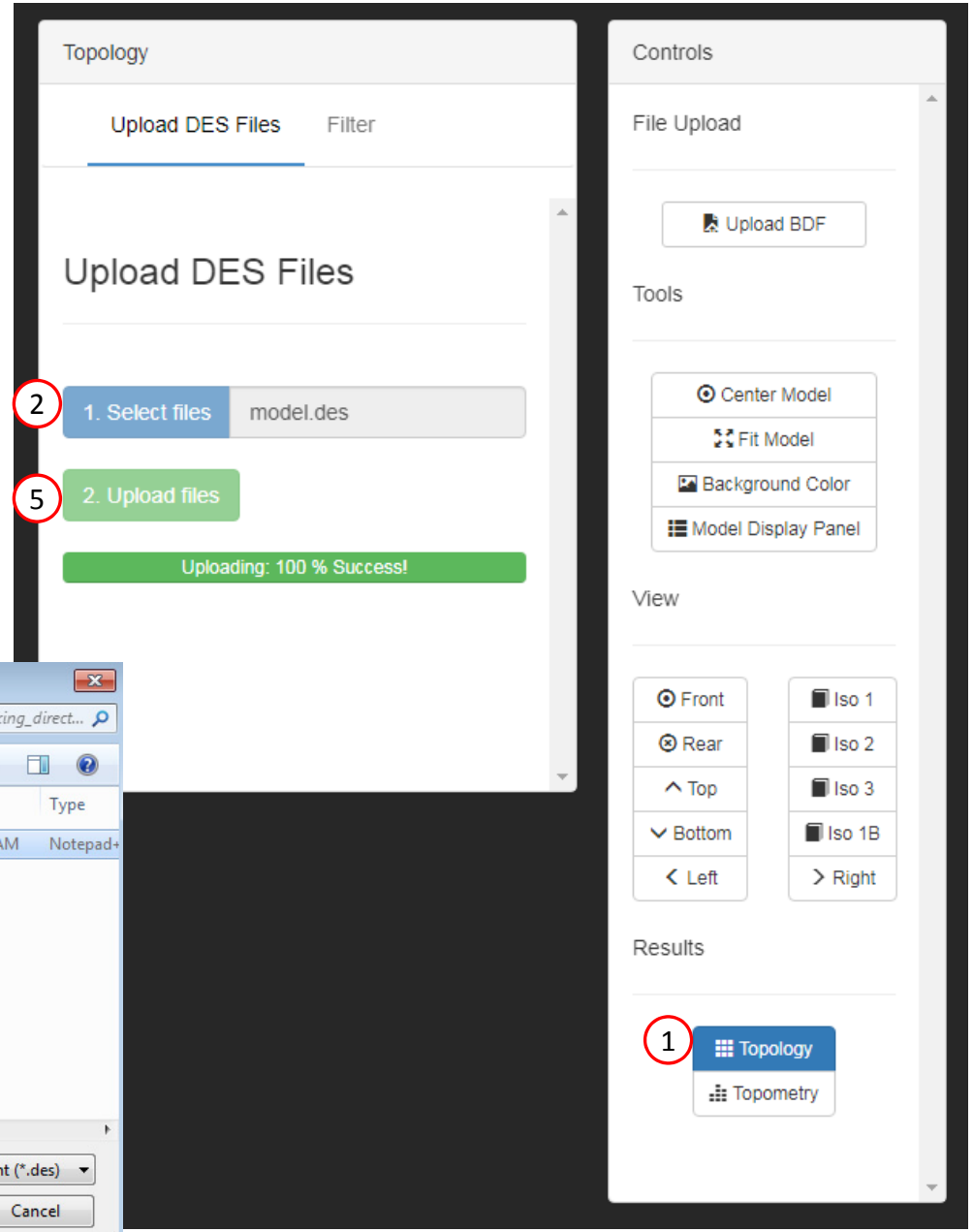


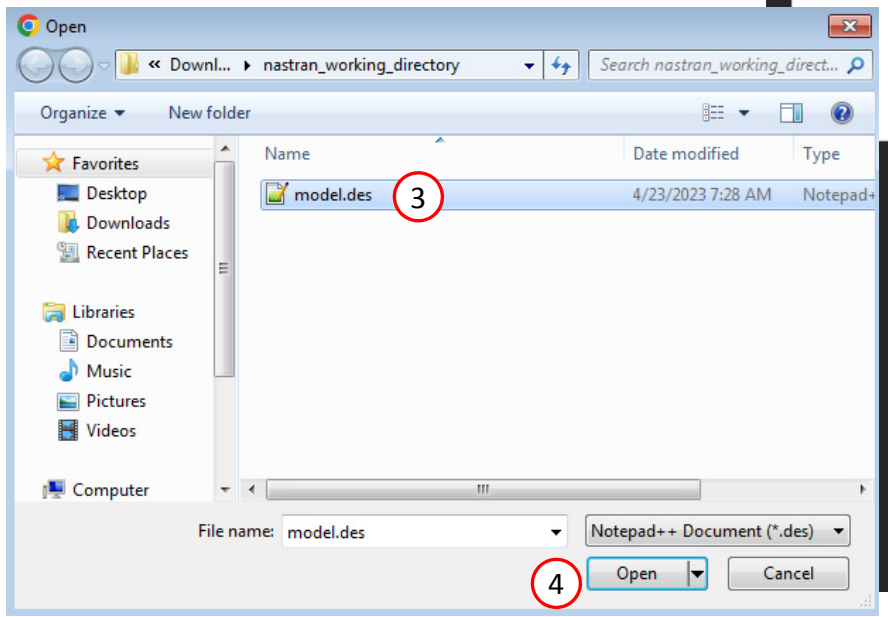
Review Optimization Results

1. Click Topology
2. Click 1. Select files
3. Select the model.des file
4. Click Open
5. Click 2. Upload files

The results of the topology optimization are now accessible within the Viewer web app.

- When the DES file is uploaded, the topology results are automatically displayed. By default, elements with a normalized material density greater than a threshold of .3 are displayed. The threshold can be modified.

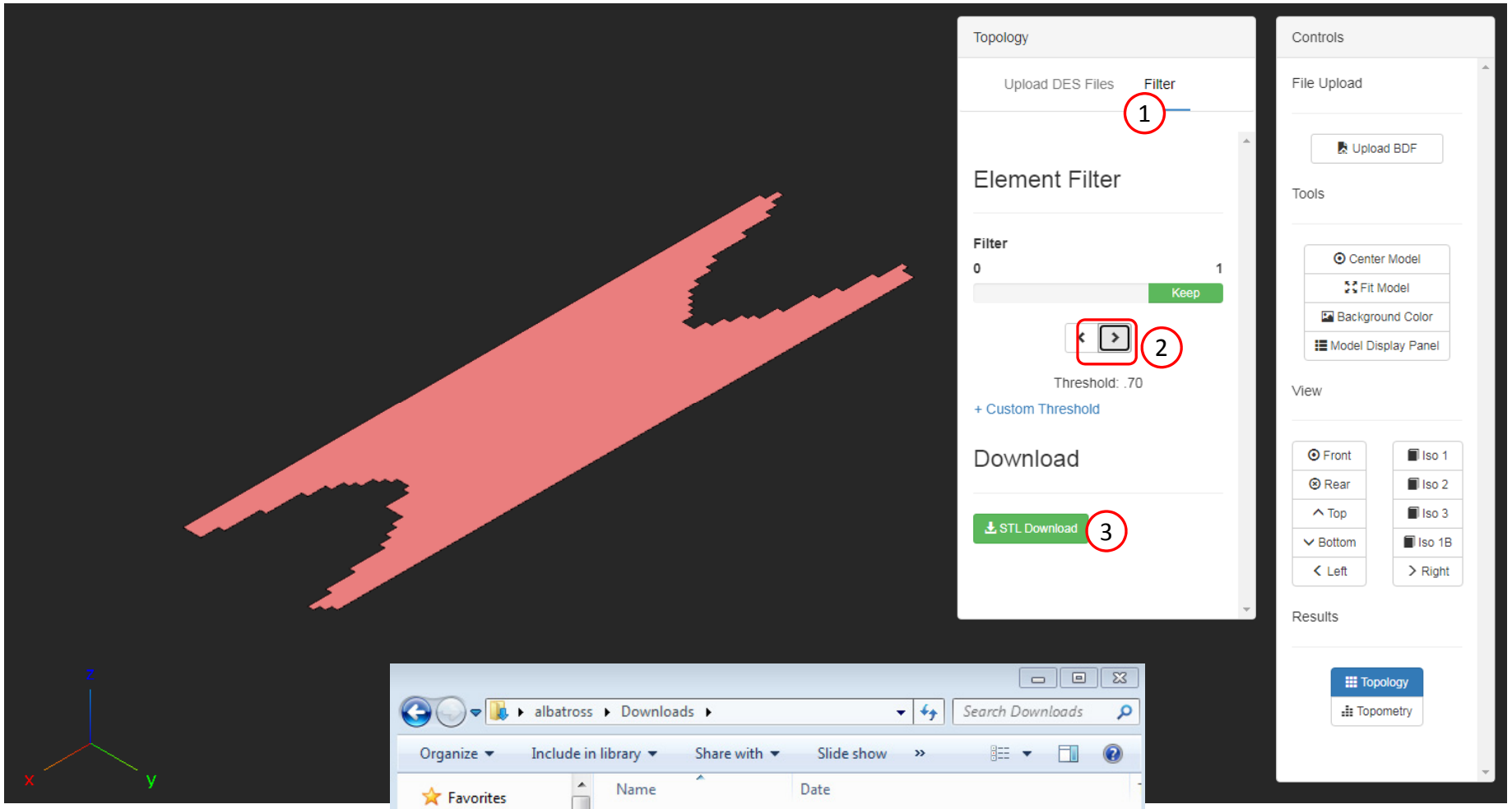


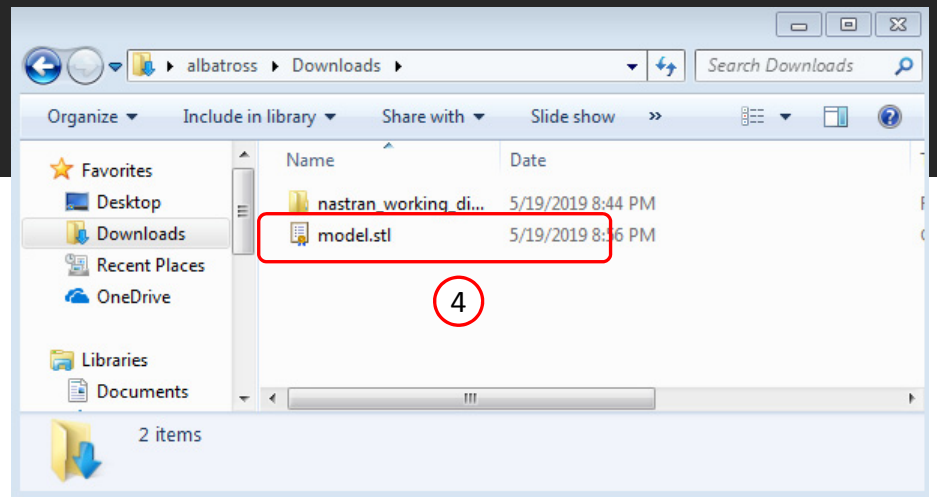


Review Optimization Results

1. Click Filter
2. Click the right arrow to remove elements below the threshold value
3. Click STL Download
4. The displayed model has been downloaded to an STL file and may be imported to separate CAD package or FEA pre processor

- A normalized material density (NMD) close to 1 indicates the element is very important and should be kept in the design. It is not recommended to go beyond a threshold of .7 since very critical elements would be removed. Elements with an NMD close to 0 are not critical and can be removed.
- Common thresholds to use are typically in the range of .3 to .7

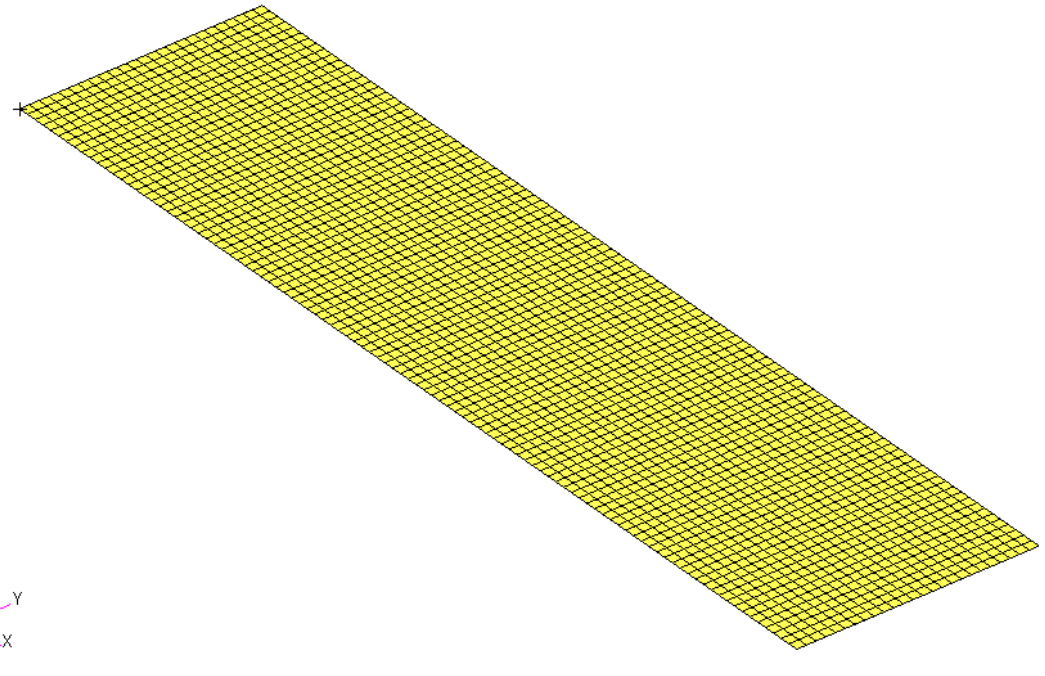




Results

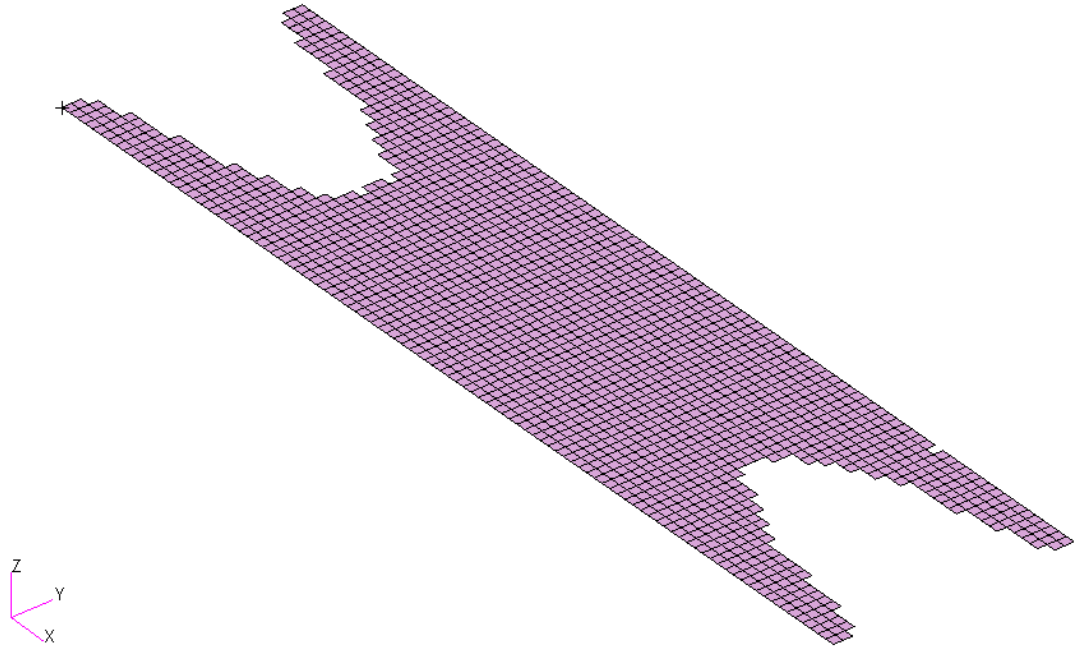
Before Optimization

- Mass: 9.73E-06



After Optimization

- Mass: 7.05E-06 (~25% mass reduction)
- Maximize stiffness
- Maximize first natural frequency



End of Tutorial

Appendix

Appendix Contents

- Frequently Asked Questions
  - What are the design variables in Topology Optimization?
  - What is FRMASS or Fractional Mass?
  - What is compliance?
  - How can non-critical elements be removed from the design?
- Topology Optimization Workflows
- Viewer Web App for Topology Optimization Post Processing

What are the design variables in Topology Optimization?

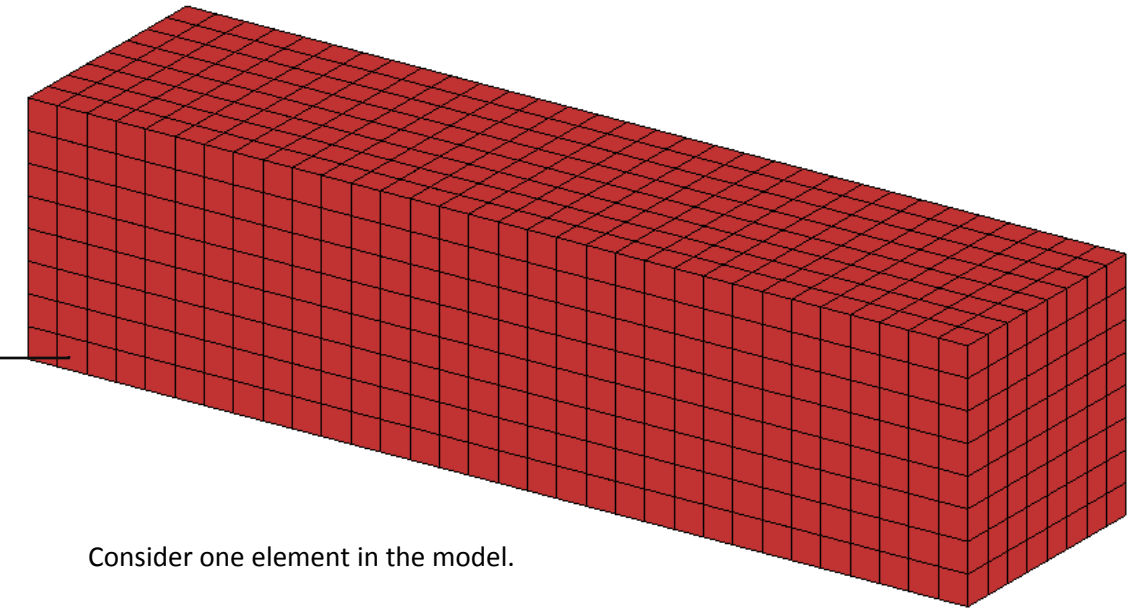
The design variables in a topology optimization are normalized material densities (p_i) of each element.

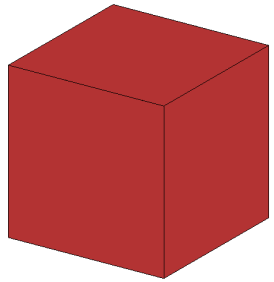
$$p_i = \frac{p_{ci}}{p_0}$$

p_{ci} : The current material density of element i

p_0 : The original material density

p_i : The normalized material density of element i



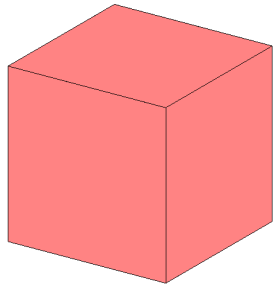


Consider one element in the model.

Suppose the original material density is 8000 kg/m^3.

If during the optimization, the normalized material density of the element is 1.0, then the current material density is

$p_{ci} = p_i \cdot p_0$
= 1.0 * 8000
= 8000



If during the optimization, the normalized material density is .5, then the current material density is

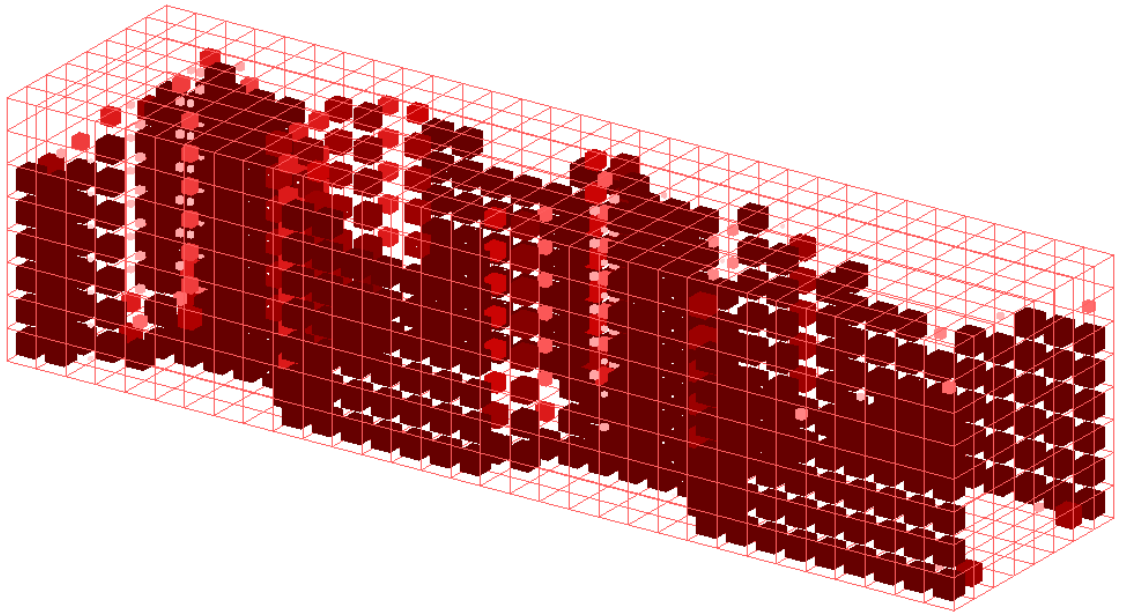
$p_{ci} = p_i \cdot p_0$
= .5 * 8000
= 4000

What are the design variables in Topology Optimization?

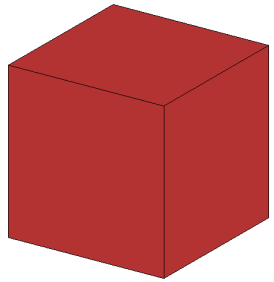
The design variables or normalized material densities can vary between 0 and 1.

- 1 - Normalized density values close to 1 are critical to the design
- 0 - Normalized density values close to 0 are not critical to the design

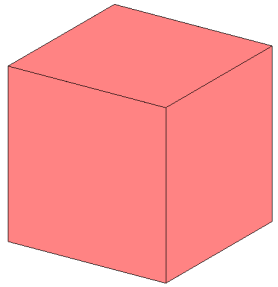
It should be noted that during the optimization, elements are never removed. Instead, the normalized material density values are used to determine which elements should be kept or removed.



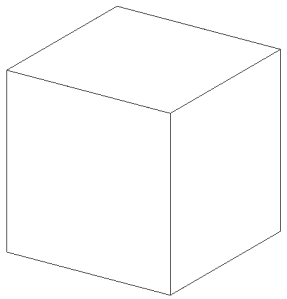
p_i = 1.0



p_i = .50



p_i = 0.0



During the optimization, the normalized material density of each element is allowed to vary between 0 and 1 ($0 < p_i \leq 1$)

What is FRMASS or Fractional Mass?

Since the design variables or normalized material densities can range between 0 and 1, the final mass will be some fraction of the original mass. This is known as the fractional mass or FRMASS.

$$\text{FRMASS} = \frac{\Sigma\, p_i \cdot p_0 \cdot v_i}{\Sigma\, p_0 \cdot v_i}$$

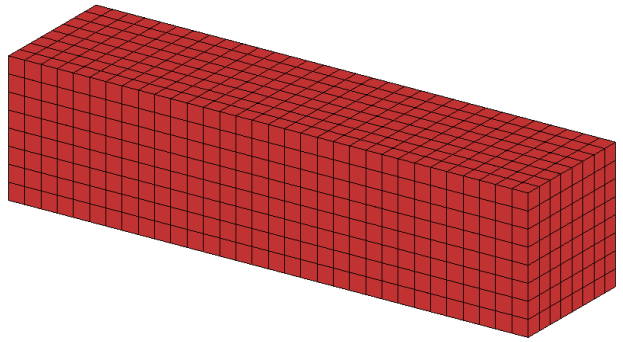
p_0 : The original material density

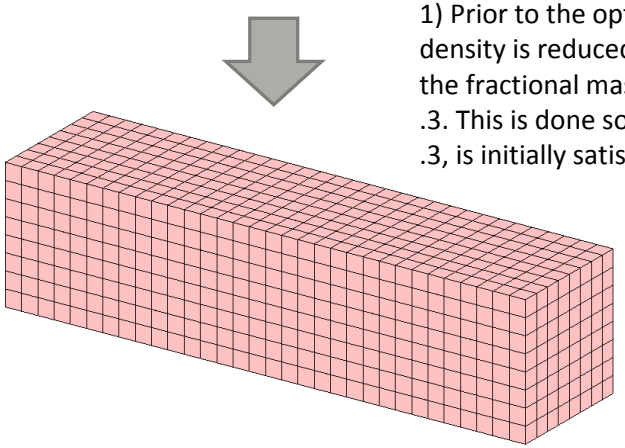
p_i : The normalized material density of the element

v_i : Volume of element

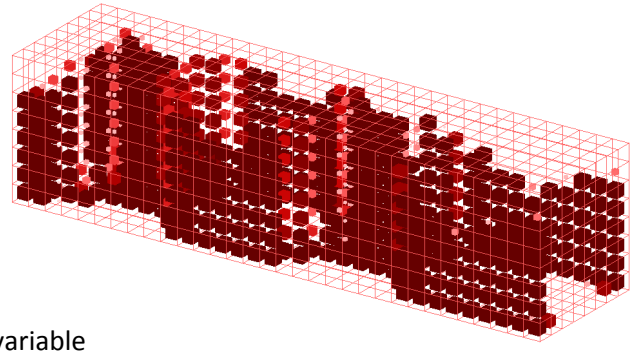
0) Suppose this is the optimization problem statement:

- Objective: Minimize compliance
- Constraint: FRMASS < .3





1) Prior to the optimization start, each material density is reduced from 1.0 to .3, and as a result, the fractional mass (FRMASS) is reduced from 1.0 to .3. This is done so the design constraint, FRMASS < .3, is initially satisfied.



2) During the optimization, each variable (normalized material density) is allowed to range between 0 and 1.0, but the constraint that the FRMASS < .3 should ultimately be satisfied.

What is compliance?

Compliance is defined in many ways

- “Compliance is simply the product of the displacement times the applied load” (MSC Nastran Design Sensitivity and Optimization User’s Guide)
- For linear elastic solids, the work is twice the total strain energy

```
                                E L E M E N T   S T R A I N   E N E R G I E S

ELEMENT-TYPE = HEXA                * TOTAL ENERGY OF ALL ELEMENTS IN PROBLEM     =    9.111034E+03
SUBCASE                1           * TOTAL ENERGY OF ALL ELEMENTS IN SET      -1 =    9.111034E+03

                     ELEMENT-ID          STRAIN-ENERGY          PERCENT OF TO
                             25          8.059148E+02                 8.8455
                             32          8.059148E+02                 8.8455          6.447318E+03
                             33          8.059148E+02                 8.8455          6.447318E+03
                             40          8.059148E+02                 8.8455          6.447318E+03

          TYPE = HEXA     SUBTOTAL       9.111034E+03                100.0000
```

Total Strain Energy

```
                        ********************************************************************
                        S U M M A R Y   O F   D E S I G N   C Y C L E   H I S T O R Y
                        ********************************************************************

                                        (HARD CONVERGENCE ACHIEVED)

                                  NUMBER OF FINITE ELEMENT ANALYSES COMPLETED          56
                                  NUMBER OF OPTIMIZATIONS W.R.T. APPROXIMATE MODELS    55

                                  OBJECTIVE AND MAXIMUM CONSTRAINT HISTORY
-------------------------------------------------------------------------------------------------------------------------
 CYCLE          OBJECTIVE FROM          OBJECTIVE FROM          FRACTIONAL ERROR          MAXIMUM VALUE
 NUMBER          APPROXIMATE               EXACT                     OF                       OF
                 OPTIMIZATION              ANALYSIS              APPROXIMATION            CONSTRAINT
-------------------------------------------------------------------------------------------------------------------------

 INITIAL                                1.822207E+04                                      -4.625929E-15

       1          5.076533E+03          1.32                    6.163140E-01             9.999972E-09

       2          5.721454E+03          1.12                    4.893855E-01             6.604279E-09

       3          4.220301E+03          1.016538E+04           -5.848357E-01             1.000032E-08

       4          3.996396E+03          9.769504E+03           -5.909315E-01             9.983010E-09
```

Compliance

What is compliance? Continued

The .f06 file reports the value of compliance and strain energy. **The following applies if and only if minimizing the compliance is the design objective.**

1. Make sure this statement is in the Case Control Section of the .bdf file.

   ESE(THRESH=.99)=ALL

2. Search the .f06 file for the initial design's

   E L E M E N T S T R A I N E N E R G I E S

3. *Note the value of TOTAL ENERGY OF ALL ELEMENTS IN PROBLEM*

4. *Search the .f06 for the*

   S U M M A R Y O F D E S I G N C Y C L E H I S T O R Y

5. Note the value for OBJECTIVE FROM EXACT ANALYSIS for the INITIAL cycle number

6. The Compliance of 1.8222E4 is twice the TOTAL STRAIN ENERGY of 9.11E3.

E L E M E N T S T R A I N E N E R G I E S

ELEMENT-TYPE = HEXA * TOTAL ENERGY OF ALL ELEMENTS IN PROBLEM = 9.111034E+03
SUBCASE 1 * TOTAL ENERGY OF ALL ELEMENTS IN SET -1 = 9.111034E+03

ELEMENT-ID	STRAIN-ENERGY	PERCENT OF TOTAL	STRAIN-ENERGY-DENSITY
25	8.059148E+02	8.8455	6.447318E+03
32	8.059148E+02	8.8455	6.447318E+03
33	8.059148E+02	8.8455	6.447318E+03
40	8.059148E+02	8.8455	6.447318E+03
TYPE = HEXA SUBTOTAL	9.111034E+03	100.0000	

S U M M A R Y O F D E S I G N C Y C L E H I S T O R Y

(HARD CONVERGENCE ACHIEVED)

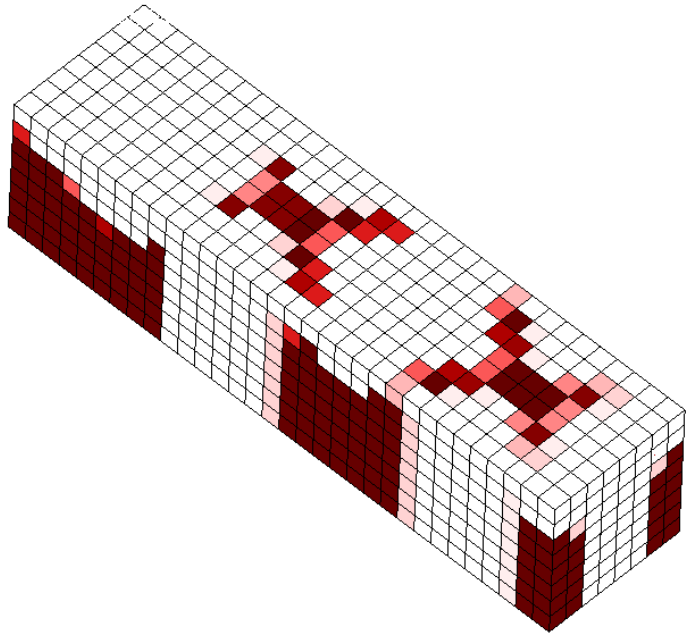
NUMBER OF FINITE ELEMENT ANALYSES COMPLETED 56
NUMBER OF OPTIMIZATIONS W.R.T. APPROXIMATE MODELS 55

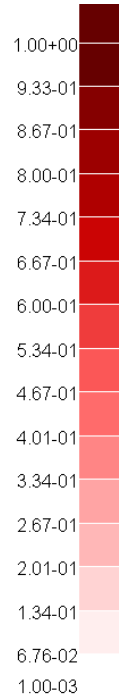
OBJECTIVE AND MAXIMUM CONSTRAINT HISTORY

CYCLE NUMBER	OBJECTIVE FROM APPROXIMATE OPTIMIZATION	OBJECTIVE FROM EXACT ANALYSIS	FRACTIONAL ERROR OF APPROXIMATION	MAXIMUM VALUE OF CONSTRAINT
INITIAL		1.822207E+04		-4.625929E-15
1	5.076533E+03	1.323096E+04	-6.163140E-01	9.999972E-09
2	5.721454E+03	1.120504E+04	-4.893855E-01	6.604279E-09
3	4.220301E+03	1.016538E+04	-5.848357E-01	1.000032E-08
4	3.996396E+03	9.769504E+03	-5.909315E-01	9.983010E-09

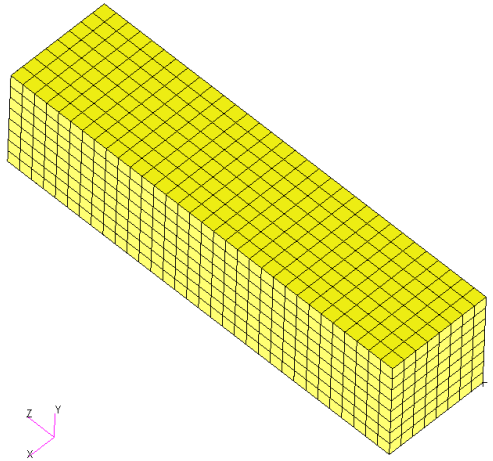
How can non-critical elements be removed from the design?

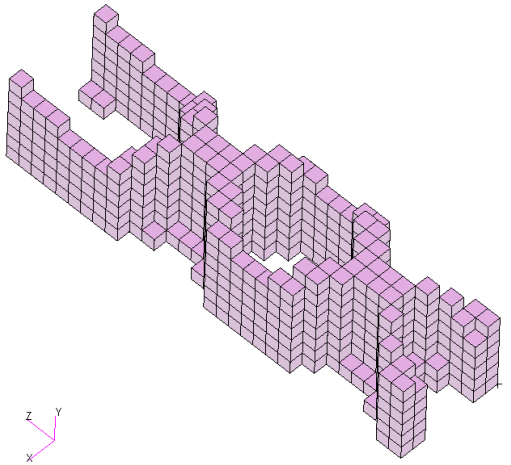
- Use the threshold to suppress non-critical elements
- The threshold means: *'Keep every element that has a normalized density greater than the threshold'*
- Recall from before:
  - 0 - Normalized density values close to 0 are not critical to the design
  - 1 - Normalized density values close to 1 are critical to the design

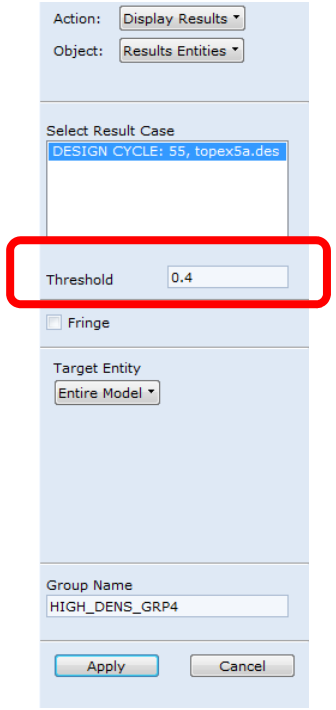




The normalized densities are plotted for each element. Note that all the elements are present.







Topology Optimization Workflows

There are 2 common optimization problem statements for topology optimization

METHOD A

Objective:

- Minimize Compliance

Constraint:

- FRMASS < Upper Bound

Comments:

- Multiple optimizations at different bounds for FRMASS are necessary. The best solution is selected from the multiple optimizations.

METHOD B

Objective:

- Minimize FRMASS

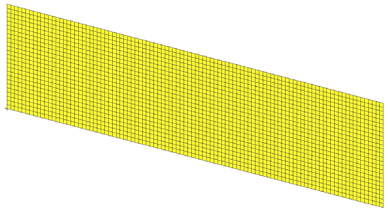
Constraint:

- Von Mises Stress < Upper Bound

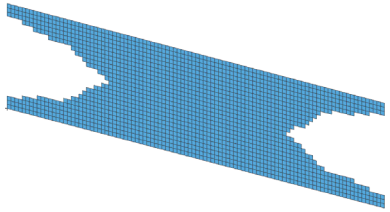
Traditional Topology Optimization

Objective: Minimize Compliance (Maximize Stiffness)
Constraint: Fractional Mass < .## (Target Mass)

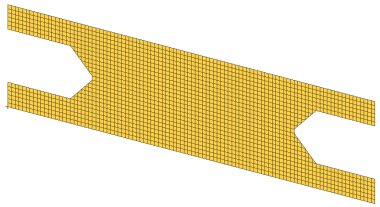
Original Design



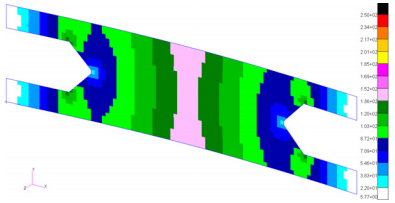
Mass: 9.737 grams



FRMASS < .75
Mass: 7.186 g
Optimization B



Mass: 7.739 g

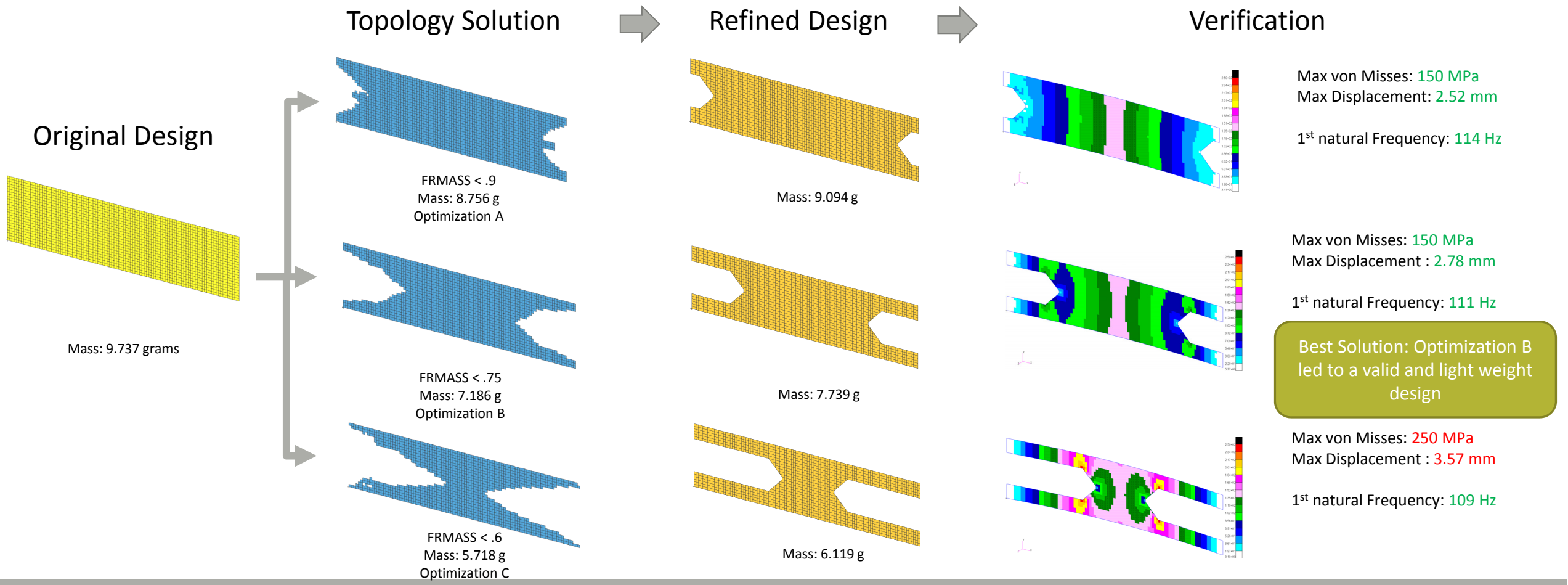


Max von Misses: 150 MPa
Max Displacement : 2.78 mm

1st natural Frequency: 111 Hz

Traditional Topology Optimization

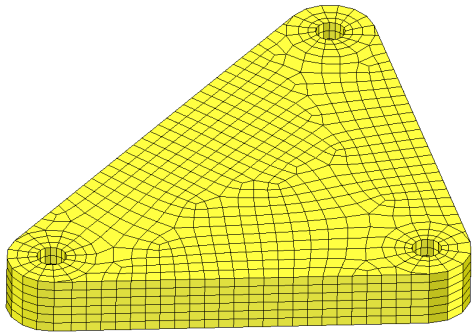
Objective: Minimize Compliance (Maximize Stiffness)
Constraint: Fractional Mass < .## (Target Mass)

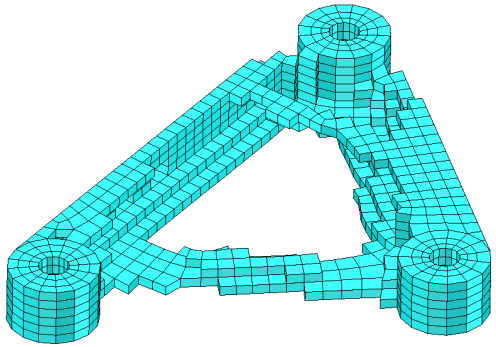


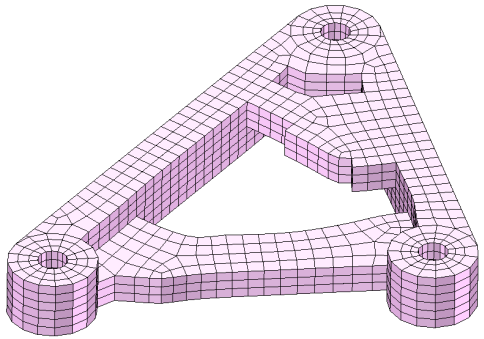
Latest Topology Optimization

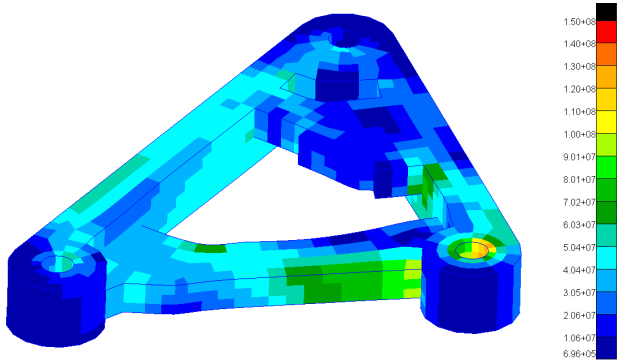
Objective: Minimize Fractional Mass (Minimize Mass)
Constraint: Stress Constraint

Original Design → Topology Solution → Refined Design → Verification









Viewer Web App for Topology Optimization Post Processing

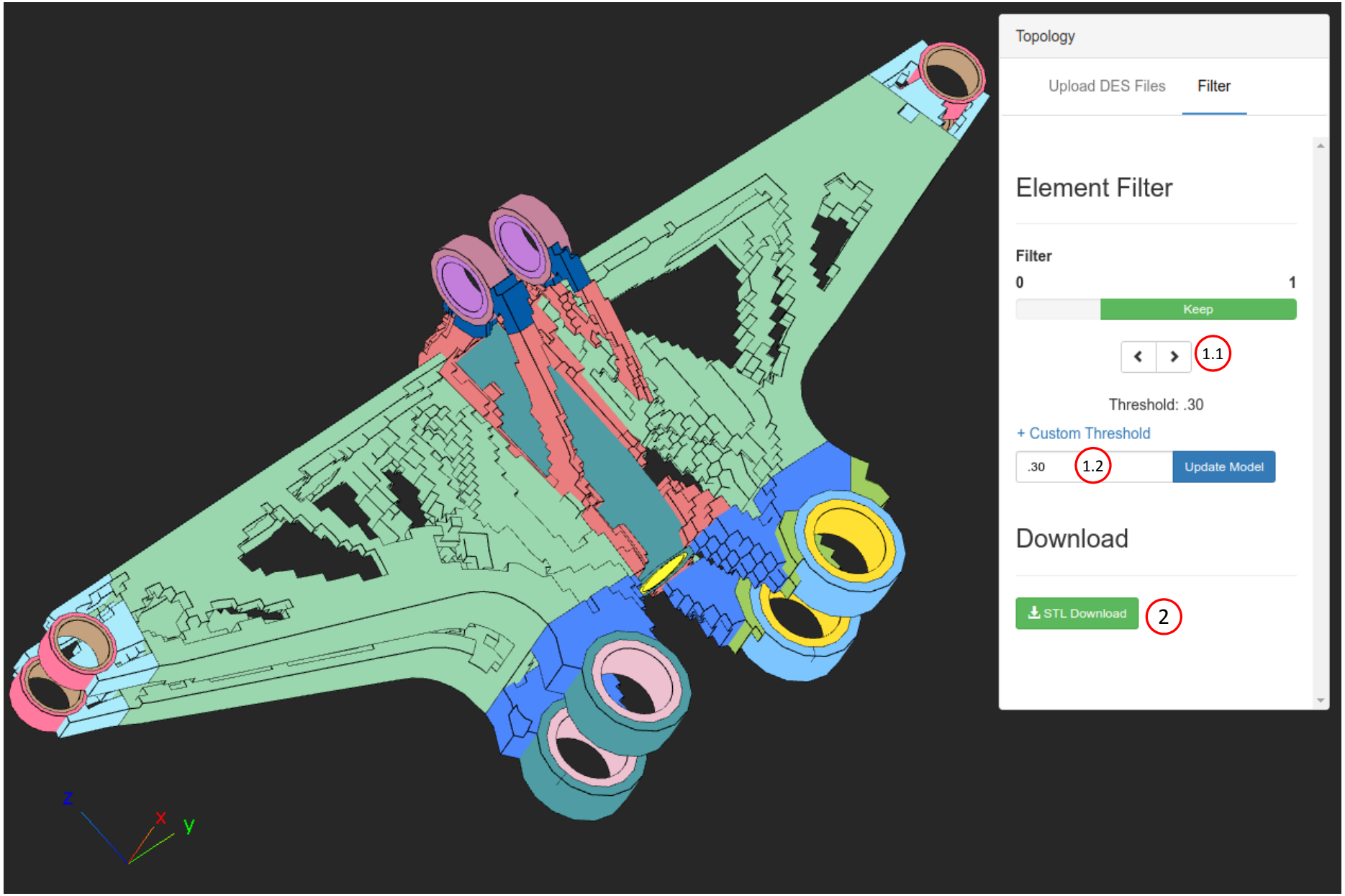
Review Optimization Results

The Viewer web app supports post processing topology optimization results.

Filtering of topology optimization results is controlled by one of 2 different ways:

1. The arrows can be used to move the threshold to values of 1.0, .3, .4, .5, .6 and .7
2. If a specific threshold is necessary, do the following:
    1. Click Custom Threshold
    2. Supply the custom threshold
    3. Click Update Model

1. STL Download – This downloads an STL file containing the model as displayed. This is useful for moving the topology results to a CAD package or FEA pre processor



Viewer
Supported Capabilities

Supported Element Types

- CTRIA3
- CTRIA6
- CTRIAR
- CQUAD4
- CQUAD8
- CQUADR
- CQUAD4
- CQUAD8
- CQUADR
- CHEXA
- CTETRA
- CPENTA
- All other elements are not supported

Coordinate Systems Supported

- Only the basic coordinate system (CID=0) is supported for GRIDs. This is a rectangular Cartesian system and is also known as the default coordinate system.
- All other coordinate systems are not supported. This includes cylindrical, spherical and other cartesian systems (CID=1, 2, 3…).

STL Download/Export is Supported

Performance

- When uploading BDF or DES files, there are many operations performed, e.g. reading, parsing, and displaying data. This is the first release of the Topology Viewer and future improvements to performance will be made. At the time of writing this, the viewer is capable of fully parsing and displaying 10MB of BDF files every 25 seconds. The viewer does not provide a progress bar regarding the parsing process, so it was best to document here the expected parsing rate.